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Section ————— A

Semister ————— 2nd

Department ————— BE (civil)

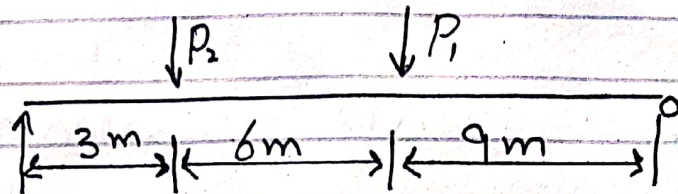
Subject ————— Engineering mechanics

Date ————— 27 June 2020

P-①

Q(1) Find the support reactions, show all your calculations.

($P_1 = 200 + \text{Student ID No}$) $P_2 = 500 + \text{Student ID No}$



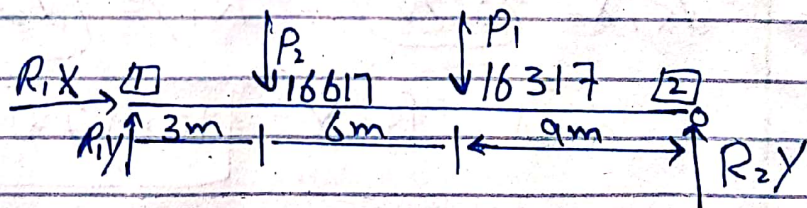
Ans:

Sol: $P_1 = 200 + 16117$

$$P_1 = \boxed{16317 \text{ N}}$$

$$P_2 = 500 + 16117$$

$$P_2 = \boxed{16617 \text{ N}}$$



$$R_{1x} = 0 \quad \text{summation of } f_x = 0$$

$$R_{1y} + R_{2y} - 16317 - 16617 = 0 \quad \text{summation of } f_y = 0$$

$$R_{1y} + R_{2y} = 16317 + 16617$$

$$R_{1y} + R_{2y} = \boxed{32,934} \quad \text{--- eq (1)}$$

P - (2)

$$R_1 Y = \frac{[(16317 \times 9) + (16617 \times 15)]}{18}$$

$$R_1 Y = \frac{146853 + 249255}{18}$$

$$R_1 Y = \boxed{22,006 \text{ N}} \quad \text{--- eq (2)}$$

Put eq (2) in eq (1)

$$R_1 X + R_2 Y = 32,934$$

$$22,006 + R_2 Y = 32,934$$

$$R_2 Y = 32,934 - 22,006$$

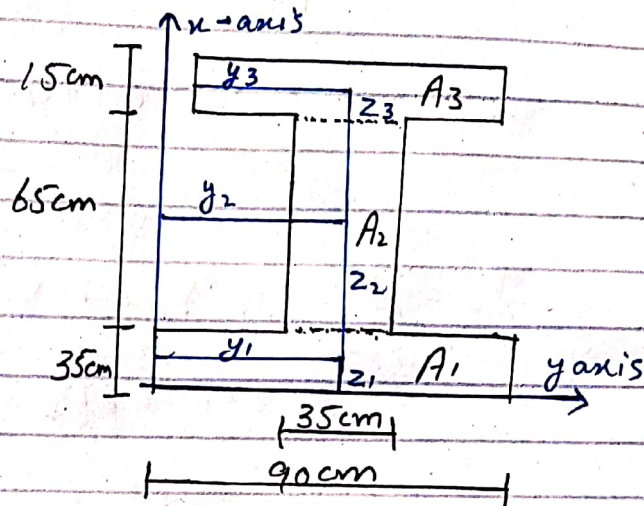
$$R_2 Y = 10,928 \text{ N}$$

$$R_1 X = \boxed{0 \text{ N}}, \quad R_1 Y = \boxed{22,006 \text{ N}}$$

$$\text{and } R_2 Y = \boxed{10,928 \text{ N}}$$

P-3

Q(4) a) Find the centroid of the given shape, show all your calculation.



Sol. * Establish the coordinate system
 * Divide the composite area into different simple areas.

$$A_1 = 0.35 \times 0.9 = 0.315 \text{ m}^2$$

$$A_2 = 0.65 \times 0.35 = 0.2275 \text{ m}^2$$

$$A_3 = 0.65 \times 0.15 = 0.0975 \text{ m}^2$$

Finding center area point of each area from the origin

$$y_1 = 0.9/2 = 0.45 \text{ m}$$

$$y_2 = 0.9/2 = 0.45 \text{ m}$$

$$y_3 = 0.9/2 = 0.45 \text{ m}$$

P-4

$$Z_1 = 0.35/2 = 0.175 \text{ m}$$

$$Z_2 = 0.35 + (0.65/2) = 0.675 \text{ m}$$

$$Z_3 = 0.35 + 0.65 + 0.15/2 = 1.075 \text{ m}$$

$$Y_c = \frac{A_1 Y_1 + A_2 Y_2 + A_3 Y_3}{A_1 + A_2 + A_3}$$

$$= \frac{(0.315 \times 0.45) + (0.2275 \times 0.45 \text{ m}) + (0.0975 \times 0.45)}{0.315 + 0.2275 + 0.0975}$$

$$= \frac{0.1417 + 0.10237 + 0.04387}{0.43525}$$

$$= \frac{0.28794}{0.43525}$$

$$Y_c = 0.6615 \text{ m}$$

$$Z_c = \frac{A_1 Z_1 + A_2 Z_2 + A_3 Z_3}{A_1 + A_2 + A_3}$$

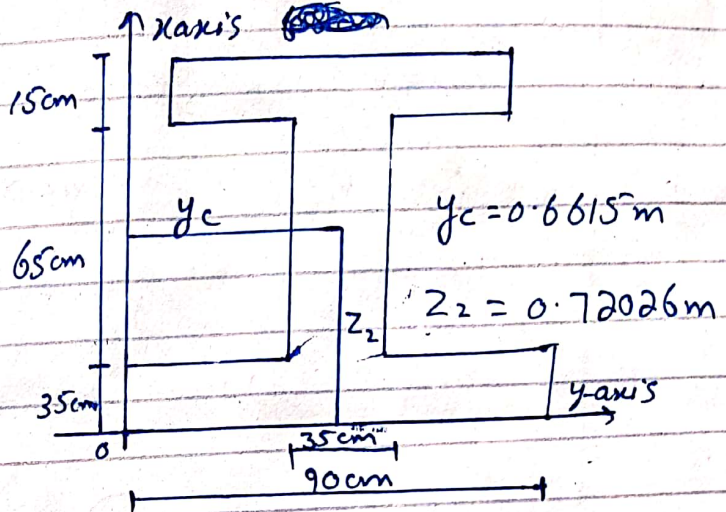
$$Z_c = \frac{(0.315 \times 0.175) + (0.2275 \times 0.675) + (0.0975 \times 1.075)}{0.43525}$$

$$= \frac{0.05512 + 0.153562 + 0.104812}{0.43525}$$

$$= \frac{0.313494}{0.43525}$$

P-5

$$Z_c = 0.72026 \text{ m}$$



Q(5) Explain work, energy and power in details along with practical examples from daily life.

Ans:

Work :

The application of a force through certain distance is known as work. It is measured in Joules.

Work = Force \times Distance travelled in direction of force.

$$W = F \cdot d$$

When force is exerted on an object. The amount of energy transferred is called the work done on the object. Mathematically

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work done is defined as the scalar product of force and displacement, thus it is a scalar quantity.

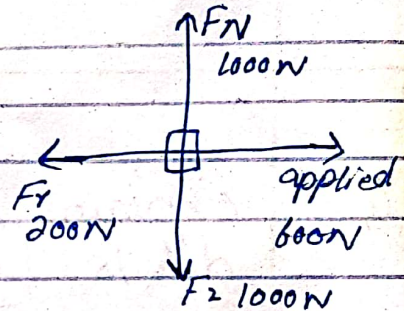
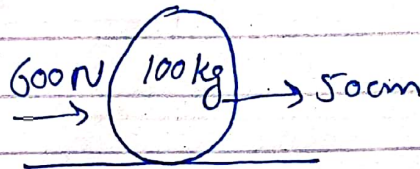
$$W = F \cdot d$$

W = work done (J)

F = Force applied (N)

d = the distance (m).

Work Done by friction.



$$\text{Work} = -200 \text{ N} \times 50 \text{ cm}$$
$$= -10,000 \text{ J}$$

Mathematically:

Work is the result of a force on a point that follows a curve x with a velocity v at each instant. The small amount of work δw that occurs over an instant of time dt is calculated as

$$\delta W = F \cdot ds = F \cdot v dt$$

Where the $F \cdot v$ is the power over the instant at the sum of those

P-7

small amount of work over the trajectory.

$$W = \int_{t_1}^{t_2} \mathbf{f} \cdot \mathbf{v} dt = \int_{t_1}^{t_2} \mathbf{F} \cdot \frac{d\mathbf{s}}{dt} dt = \int_c \mathbf{F} \cdot d\mathbf{s}$$

where c is the trajectory from $\mathbf{x}(t_1)$ to $\mathbf{x}(t_2)$. This integral is computed along the trajectory of the particle and is therefore said to be path dependent. If the force is always directed along this line and the magnitude of the force is F , then this integral simplifies to $W = \int_c F ds$

where s is the displacement along the line.

$$W = \int_c F ds = F \int_c ds = Fs$$

In this case the dot product of the $\mathbf{F} \cdot d\mathbf{s} = F \cos \theta$ where θ is the angle between the force vector \mathbf{f} and the direction of movement that is

$$W = \int_c \mathbf{F} \cdot d\mathbf{s} = F s \cos \theta$$

$$\text{Dimension} = ML^2T^{-2}$$

$$\text{Unit} = 1 \text{ kg m}^2 \text{ s}^{-2}$$

~~other~~ ~~that~~ ~~is~~ ~~for~~
Daily life examples of work ::

- 1) A horse pulling a plow through the field
- 2) A person pushing a grocery cart down the aisle of a grocery store.

- 3) A freshman lifting a backpack full of books upon her shoulder.
- 4) A weightlifter lifting a barbell above his head. etc.

Energy:

Energy is the measure of the ability of an object or a system to perform work.

Unit = Joule denoted by J.

Types of energy:

1) Kinetic energy:

Energy of an object due to its speed.

2) Gravitational potential energy:

Energy of an object due to position in a gravitational field.

3) Elastic potential energy:

energy stored when an object is stretched or compressed.

4) Chemical energy:

Energy stored in chemical bond

5) Nuclear energy:

Energy stored in nuclei.

6) Heat energy:

Hot things have more

energy than their could counterparts.

Energy can be transferred in a system in a variety of ways e.g. include the transmission of electromagnetic energy via photos, physical collision which transfer kinetic energy.

$$\Delta E = W + Q$$

E is the amount of energy transferred
 W represent the work done on the system.

Q represent the heat flow into the system.

$$\text{Dimension} = ML^2T^{-2}$$

Daily life example of energy:

- 1) Heating and lighting the home
- 2) Running appliances and cooking.
- 3) Use of water pump.
- 4) Washing clothes.

Power:

Power is the rate at which work is done, or the rate at which energy is transferred.

Power = work done / time taken

$$P = W/t$$

P - (10)

- Power is measured in watt.
- Power done as energy transferred is measured in joules (J).
- time is measured in second (s).
- Common symbol of power is (P).

SI unit = watt.

In SI base unit = $\text{kg m}^2 \text{s}^{-2}$

Derivation for other quantities

$$P = E/t$$

$$P = F \cdot v$$

$$P = V \cdot I$$

$$P = T \cdot \omega$$

Dimension = $L^2 M T^{-3}$

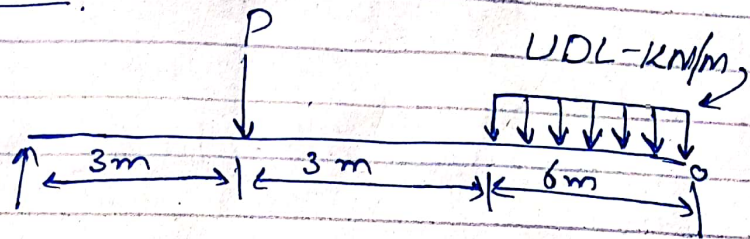
Formula =
$$P = \frac{W}{\Delta t}$$

Daily life example of power.

- * A 60 watt bulb expend 60 J of energy per second.
- * All engines.
- * All electronic appliances etc.

P-16

2) Given loads:



$$\text{Load} = P = 100 + 16117$$

$$= P = 16217 \text{ kN}$$

$$\text{Load 2 UDL} = 150 + 16117$$

$$= 16267 \text{ kN/m}$$

Support reactions

$$\sum m_p = 0 \quad (\text{C.C.})$$

$$-(16217 \times 3) - (16267 \times 6) \times (6+3) + R_B \times 12 =$$

$$-(48651) - (97602)(9) + R_B \times 12 = 0$$

$$-48651 - 878418 + R_B \times 12 = 0$$

$$R_B = \frac{48651 + 878418}{12}$$

$$R_B = 73606.91 \text{ kN}$$

$$\sum F_y = 0 \quad \uparrow + \downarrow -$$

$$R_A + R_B - 16217 - (16267 \times 6) = 0$$

P- (12)

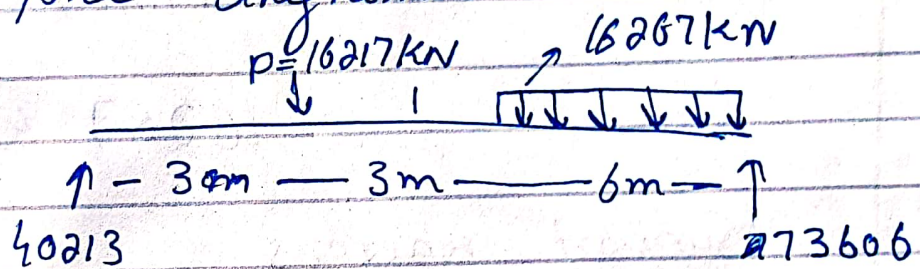
$$R_A + R_B = 113819 \text{ kN}$$

$$R_A = 113819 - R_B$$

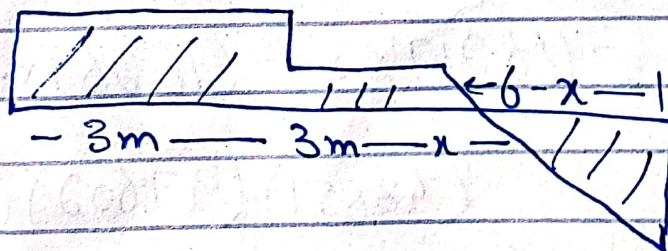
$$= 113819 - 73606.91$$

$$R_A = 40213 \text{ kN}$$

Shear force diagram.



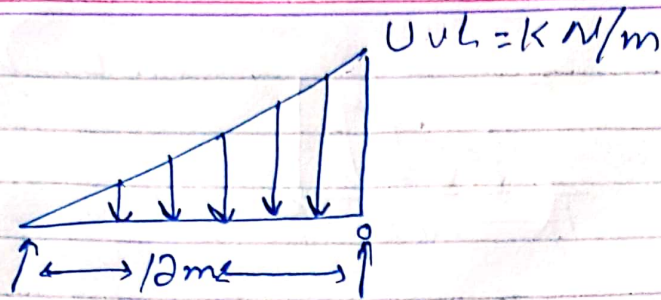
40213 kN



73606 kN

P- (13)

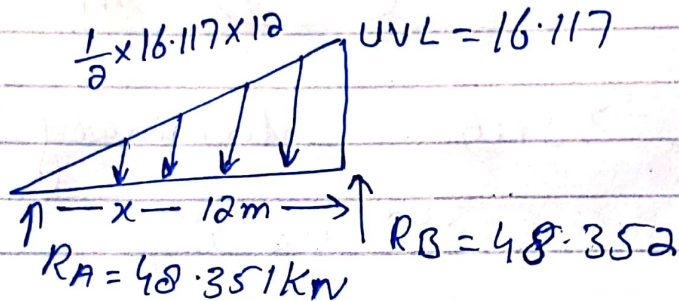
Q (3)



Given

$$\text{Let } UVL = \frac{ID}{1000} = \frac{16117}{1000} = 16.117$$

Find S.F.D and BMD=?



$$\sum M_B = 0 \text{ (clockwise positive)}$$

$$(R_A \times 12) - \left(\frac{1}{2} \times 16.117 \times 12 \times \frac{1}{2} \times 12 \right) = 0$$

$$R_A = \frac{580}{12} = 48.351$$

$$R_A = 48.351$$

$$(\downarrow, \uparrow) \sum F_y = 0$$

$$\Rightarrow 48.351 - \left(\frac{1}{2} \times 16.117 \times 12 \right) + R_B = 0$$

$$R_B = 48.352 \text{ kN}$$

Slope of S.F = intensity of load

P- (14)

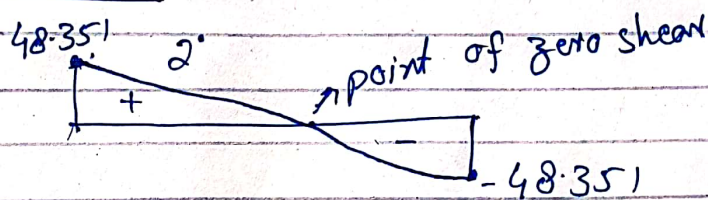
S.F at left of A = 0

S.F at right of A = -48.351

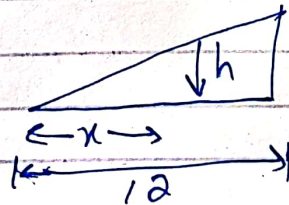
S.F at left of B = $48.351 - \frac{1}{2} \times 16.117 \times 12$
 $= -48.351$

S.F at right of B = $-48.351 = 0$

Now S.F.D:



$(S.F)_c = 0$



$$\frac{16.117}{12} = \frac{h}{x}$$

$$\Rightarrow h = \frac{16.117x}{12}$$

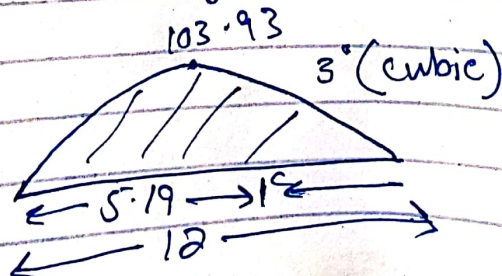
$$48.351 - \frac{1}{2} \times x \times h = 0$$

$$48.351 - \frac{1}{2} \times x^2 \times \frac{16.117x}{12} = 0$$

$$x = 5.19 \text{ m}$$

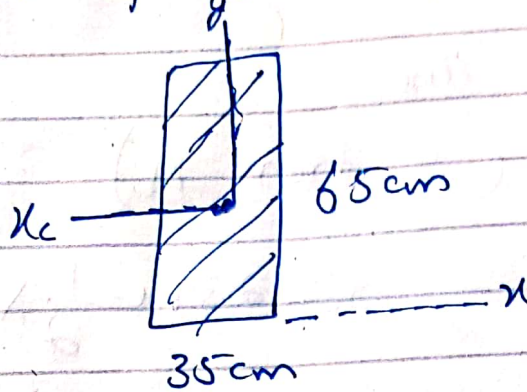
$$h = 11.53 \text{ kN/m}$$

B.M.D By calculation bending movement at A



Q (4) Part (b)

Ans: Moment of inertia for 65cm x 35cm



$$I = \frac{bh^3}{12} = \frac{35(65)^3}{12}$$

$$I = 800,989.58 \text{ cm}^4$$

Radius of gyration

$$r_{x_1} = \frac{h}{\sqrt{12}} = \frac{65}{\sqrt{12}} = 18.76 \text{ cm}$$

$$r_y = \frac{b}{\sqrt{12}} = \frac{35}{\sqrt{12}} = 10.1 \text{ cm}$$

$$r_x = \frac{h}{\sqrt{3}} = \frac{65}{\sqrt{3}} = 37.5 \text{ cm}$$