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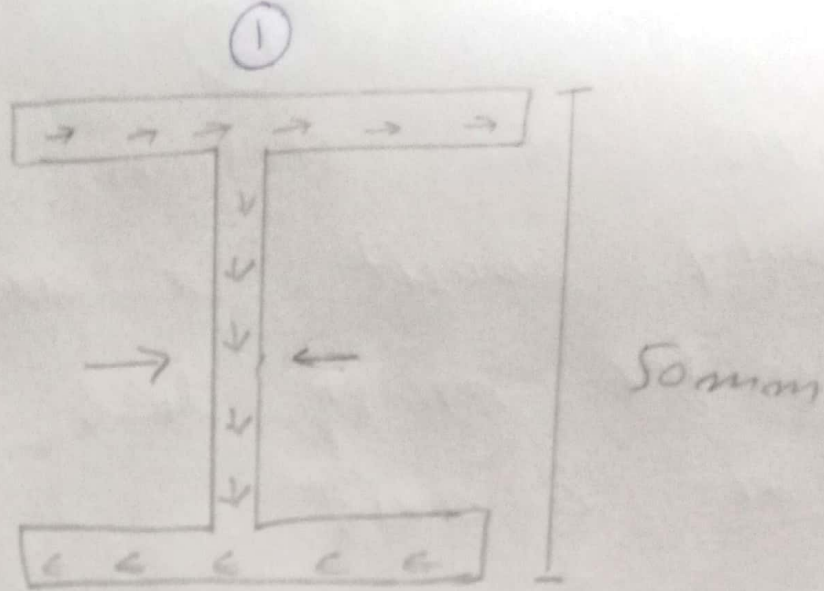
Section = B

Department = Be (C)

Subject = MTO S II

Instructor = Engr. Muhammad  
Saqib

Q No 1



The section is symmetrical about  $x$ -axis & not  $y$ -axis.

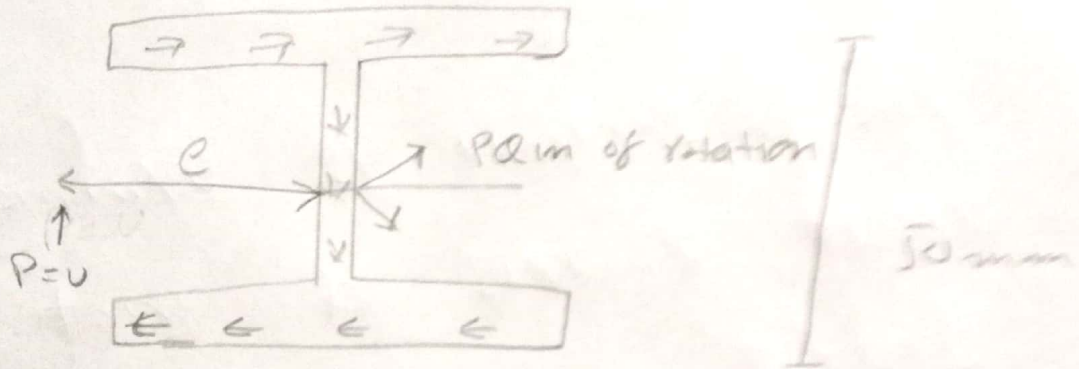
So any external force on section will create twisting in the section.

So in order to avoid twisting we will find out plane where external load will balance the internal shear flow in the section.



(2)

As the section is symmetrical only about x-axis the shear center must lie somewhere on a-axis



$$\sum M_c = 0$$

Clockwise moment = Anticlockwise moment

$$U \times e + f_t \times 50 = f_t \times 50$$

$$e = \frac{f_t \times 50 - f_t \times 50}{U} \rightarrow \textcircled{1}$$

Now we will find out  $I_x$  &  $y$

(3)

$$I = E (I + Ad^2)$$

$$I = 2 \left[ \frac{26 \times 2^3}{12} + 26 \times 2 \times (25-1)^2 \right] \\ + \left[ \frac{2 \times 50^3}{12} + 0 \right]$$

$$I_{xx} = 59938.66 + 20833.34$$

$$I = 80771.99 \text{ mm}^4$$

$$E \quad y = 25 \text{ mm}$$

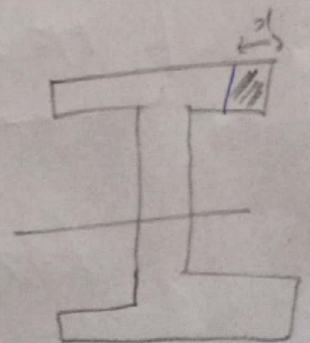
Now For Flange

$$f_f = \int_0^x q_s dx$$

$$= \int_0^x \frac{VQ}{I} dx$$

$$\frac{25V}{40380} \int_0^x x \cdot dx$$

$$Q = A\bar{y}$$





(4)

$$\int_0^x \frac{V}{80772} + 50x \, dx$$

$$= \frac{25V}{40386} \int_0^x x \cdot dx \quad Q = A \bar{y}$$

$$F_H = \frac{25V}{40386} \left[ \frac{x^2}{2} \right]_0^x = (2 \times x) 25 = 50x$$

Now for  $x = 0$  (from right angle)

$$F_H = \frac{25V}{40386} \left( \frac{20^2}{2} - 0 \right)$$

$$F_H = 0.123V$$

From left sides

$$x = 6$$

$$F_H = \frac{25V}{40386} \left[ \frac{x^2}{2} \right]_0^6$$

(3)

$$F_f = \frac{250}{40386} \left( \frac{62}{2} - 0 \right)$$

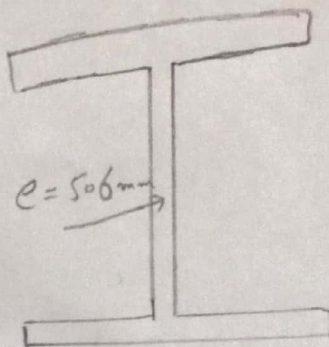
$$F_f = 0.011 \text{ V}$$

Now putting values  
in eq (1)

$$e = \frac{-0.011 \text{ V} \times 50 + 0.123 \times 50}{V}$$

$$e = 5.06 \text{ V/V}$$

$$e = 5.06 \text{ mm}$$





Question No: 01

Part "B" (CLO 2)

Given Data:

Circumferential Stress =  $\sigma_c \leq 6000 \text{ psi}$

Radius =  $62.4 \text{ lb/ft}^3$

Dia =  $22 \text{ ft}$

Height =  $26 \text{ ft}$

Required:

Determine the thickness of the wall of a water tank?

Sol:-

As we know that the pressure developed by water

$$P = \rho h$$

⑦

$$6_c = \frac{PD}{2t}$$

$$6_c = \frac{\delta h \times D}{2t}$$

$$t = \frac{\delta h \times D}{2 \times 6_c}$$

$$t = \frac{(62.4 \times 26) \times 22}{2 \times (6000 \times 12^2)}$$

$$t = 0.02 \text{ ft}$$

$t = 0.24 \text{ inches}$
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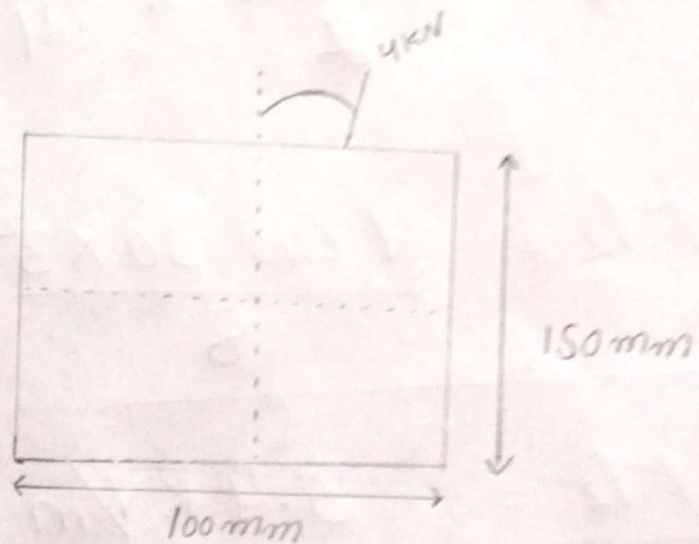
Q2 : Part (a) (CLO-3)

Given Data :

$$W = 4 \text{ kN}$$

$$L = 3 \text{ m}$$

$$\theta = 30^\circ$$

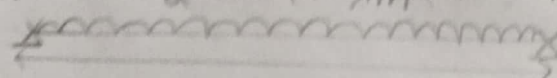


Required :-

(a) Max bending stresses at Mid Span = ?

(b) Locate neutral axis = ?

Sol:-  $12 \cos 30^\circ$   $4 \text{ kN/m}$   $12 \sin 30^\circ$



$$\frac{4 \times 3 \cos 30}{2}$$

$$\frac{4 \times 3 \sin 30}{2}$$

For UDL Max moment  
max Mid Section.

$$M_2 = \frac{wL}{2} \times \frac{L}{4} = \frac{wL^2}{8}$$

$$M_2 = \frac{4 \cos 30 \times 3^2}{8}$$

$$M_2 = 3.9 \text{ kN/m}$$

Now For  $M_y$

$$M_y = \frac{4 \sin 30 \times 3^2}{8}$$

$$M_y = 2.25 \text{ kN.m}$$

$$M_y = 2.25 \text{ kN.m}$$



(10)

$$I_y = \frac{0.150 \times 0.1^3}{12}$$

$$I_y = 1.25 \times 10^{-5} \text{ m}^4$$

$$I = \frac{0.100 \times 0.150^3}{12}$$

$$I = 2.81 \times 10^{-5} \text{ m}^4$$

As we know that total bending stress at mid span

$$\sigma_c = \frac{M_x}{I_x} y + \frac{M_y}{I_y} z$$

$$y = 0.075 \text{ m}$$

$$z = 0.05 \text{ m}$$

$$I_x = 2.81 \times 10^{-5} \text{ m}^4$$

$$I_y = 1.25 \times 10^{-5} \text{ m}^4$$

$$\sigma_2 = \frac{M_2 y}{I_2}$$

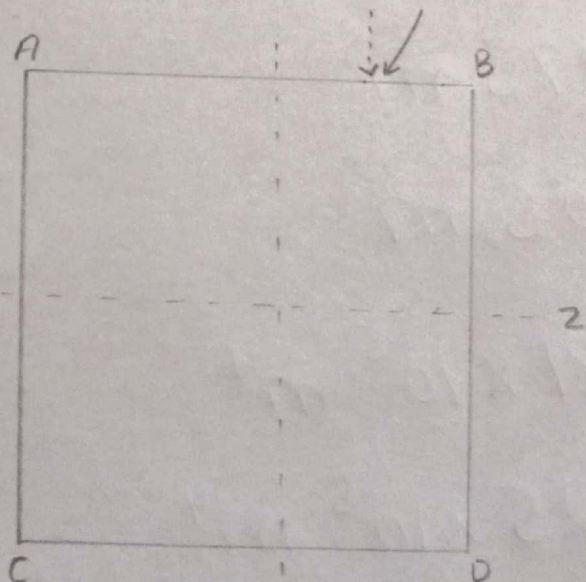
$$\sigma_2 = \frac{3.9 \times 0.075}{2.81 \times 10^{-5}}$$

$$\sigma_2 = 10409.25 \text{ KN/m}^2$$

$$\sigma_y = \frac{M_y \cdot z}{I_y}$$

$$\sigma_y = \frac{2.25 \times 0.05}{1.25 \times 10^{-5}}$$

$$\sigma = 9000 \text{ KN/m}$$





(12)

Maximum bending stress at the extreme fibers

$$\sigma_A = -\sigma_2 + \sigma_y$$

$$\sigma_B = -\sigma_2 - \sigma_y$$

$$\sigma_C = +\sigma_2 + \sigma_y$$

$$\sigma_D = -\sigma_2 - \sigma_y$$

Note  $\rightarrow \sigma_2 = 10409.25 \text{ KN/m}^2$

$$\sigma_y = 9000 \text{ KN/m}^2$$

Now

$$\sigma_A = -10409.25 + 9000 = (-1409.25 \text{ KN/m}^2)$$

$$\sigma_B = -10409.25 + (-9000) = (-19409.25 \text{ KN/m}^2)$$

$$\sigma_C = 10409.25 + 9000 = (19409.25 \text{ KN/m}^2)$$

$$\sigma_D = 10409.25 + (-9000) = (1409.25 \text{ KN/m}^2)$$

Question No. 02 :- Part (b) CLO-3

Given Data:

$\bar{y} = 3.07 \text{ in}$

$x = 3 \text{ in}$

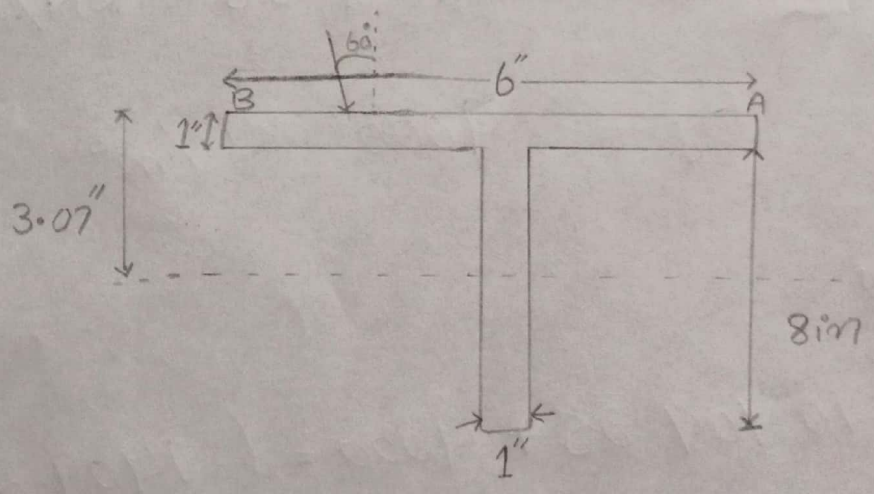
$I_x = 112.6 \text{ in}^4$

$I_y = 18.7 \text{ in}^4$

Compressive stress  $\leq 12000 \text{ PSI}$

Tensile stress  $\leq 5000 \text{ PSI}$

Figure:-



Required:- Max load that will not overstress the beam?



Sol:- The maximum bending stresses occur at the mid section due to the maximum bending moment, so that the critical section is the mid section where the compressive and tensile stresses can exceed the limiting values.

"we also know that at any given section the maximum stress occurs at the extreme fibers.

For ~~example~~ A, B, C, & D

we know that for point load at mid section is:

$$M = \frac{PL}{4}$$

$$M_x = \frac{P \cos 60 \times 16 \times 12}{4}$$



(15)

$$M_y = \frac{P \sin 60 \times (16 \times 12)}{4}$$

$$M_y = 41.57 P$$

Stresses at Point A, B, C & D

Point A:

$$\sigma_2 = \frac{M_x \cdot y}{I_x} + \frac{M_y \cdot x}{I_y}$$

$$= \frac{24 \times 3.07}{112.6} + \frac{41.57 \times 3}{18.7}$$

$$\sigma_2 = -0.654 + 6.667$$

$$\sigma_2 = 6.014 \text{ (Tension)}$$

$$\sigma \text{ Tension} \leq 5000 \text{ Psi}$$



$$P = \frac{5000}{6.014}$$

$$P = 831.94 \text{ lb}$$

For Point B:-

$$\sigma_B = \frac{M_x \cdot y}{I_x} + \frac{M_y \cdot x}{I_y}$$

$$\sigma_B = -0.554 + (6.667)$$

$$\sigma_B = -7.231 \text{ (compression)}$$

El compression  $\leq 12000 \text{ psi}$

$$P = \frac{12000}{7.231}$$

$$P = 1659.52$$

So, controlling values b/w A & B is  $\boxed{831.94 \text{ lb}}$

(17)

For Point C:

$$G_C = 0.654 + 6667$$

$$G_C = 7.321 \text{ (Tension)}$$

Tension  $\leq 5000$

$$P = \frac{5000}{7.321}$$

$$P = 682.97 \text{ lb}$$

For Point D

$$G_D = +0.654 + (6.667)$$

$$G_D = -6.013 \text{ (Compression)}$$

{ Compression  $\leq 12000$

$$P = \frac{12000}{6.013}$$

$$P = 1995.67 \text{ lb}$$

So, controlling value b/w

C, D is

682.97 lb

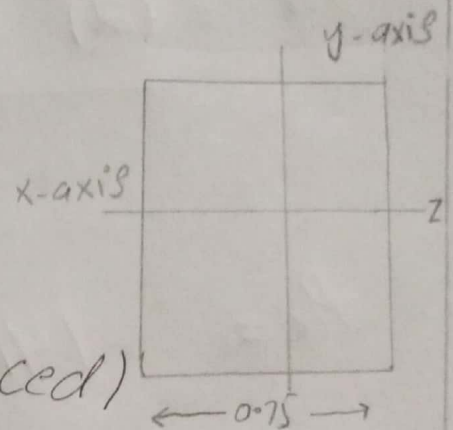


Q No 4:-

Given Data

$$L = 10 \text{ ft}$$

$n = 2$  (~~fixed~~ <sup>center</sup> braced)



Case I:-

Struct act as a  
column about an axis  
perpendicular to the 2<sup>nd</sup>  
dimension

$$I_x = \frac{0.75 \times 2^3}{12}$$

As we know that

$$P_u = \frac{n^2 E I A^2}{L_e}$$

For winged ended column

$$L_e = L$$

$$P_c = \frac{(2)^2 \times 10.3 \times 10^6 \times (0.5) (3.14)^2}{(10 \times 12)^2}$$

$$P_c = 14104.70 \text{ lb}$$

$$\text{Now } P_{\text{safe}} = \frac{P_c}{\text{FOS}}$$

$$P_{\text{safe}} = 7052.35$$

Case II

Struct & column acts  
as a fixed end column  
about an parallel to 2in  
side

$$\text{So } I_y = \frac{2 \times 0.75^3}{12} = 0.0703 \text{ in}^4$$

$$L_e = L/2 \text{ (For Fixed ended column)}$$



Then

$$P_{cr} = \frac{n^2 EI \pi^2}{L_e^2}$$

$$= \frac{(2)^2 \times 10.3 \times 10^6 \times (0.0703) \times (3.14)^2}{\left(\frac{10}{2} \times 12\right)^2}$$

$$P_{cr} = 7932.48$$

$$P_{safe} = \frac{P_{cr}}{FOS}$$

$$P_{safe} = \frac{7932.48}{2}$$

$$P_{safe} = 3966.24 \text{ lb}$$

OK both cases

(21)

we will take smaller  
values of  $P_{safe}$

$$P_{safe} = 3966.24 < 7052.35$$

So will consider

$$P_{safe} = 3966.24 \text{ lb}$$