

SYED JAWWAD

7386

HYDRAULIC ENGINEERING

# ASSIGNMENT #1

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## VENTURE FLUME:

A Venture flume is a critical-flow open flume with a constricted flow which causes a drop in the Hydraulic grade line, creating a critical depth.

It is used in flow measurement of a very large flow rates, usually given in millions of cubic units. A venturimeter would normally measure in millimeters, whereas a venturine flume measures in meters.

Measurement of Discharge with venturine flume requires two measurements, one upstream and one at throat (narrowest cross-section). If the flow passes in a sub-critical to super-critical state while passing through the flume, a single measurement at the throat (which in this case becomes a critical section) is sufficient for computation of discharge. To ensure the occurrence of critical depth at the throat, the flumes are usually designed in such a way as to form a hydraulic jump on the downstream side of the structure. These flumes are called standing wave flumes.

# Assignment # 1

(2)

## Problem # 2

Given Data:-

$$b = 3\text{m}$$
$$Q = 12\text{m}^3\text{s}^{-1}$$

Solution:-

(a) Discharge per unit width

$$q = \frac{Q}{b} = \frac{12}{3} = 4\text{m}^2\text{s}^{-1}$$

Then for a Rectangular Channel

$$h_c = \left(\frac{q^2}{g}\right)^{1/3} = \left(\frac{4^2}{9.81}\right)^{1/3} = 1.177\text{m}$$

Answer:- Critical Depth = 1.18m

(b) For a Rectangular channel

$$E_c = \frac{3}{2} h_c = \frac{3}{2} \times 1.177 = 1.766\text{m}$$

Answer:- Minimum Specific Energy = 1.77m

(c) As  $E > E_c$  there are two possible depths for a given Specific Energy

$$E \equiv h + \frac{V^2}{2g} \quad \text{where } V = \frac{Q}{A} = \frac{q}{h} \quad (\text{for a rectangular channel})$$
$$\Rightarrow E \equiv h + \frac{q^2}{2gh^2}$$

Substituting values in Meter-Second Units.

$$y = h + \frac{0.8155}{h^2}$$

(3)

For the Subcritical (slow, deep) Solution, the first term, associated with Potential Energy dominates, So re-arrange

$$h = y - \frac{0.8155}{h^2}$$

Iteration (from e.g.  $h=4$ ) gives  $h=3.9248\text{m}$

For the Supercritical (fast, shallow) Solution, the second term, associated with kinetic Energy, dominates So re-arrange.

$$h = \sqrt{\frac{0.8155}{y-h}}$$

Iteration (from e.g.  $h=0$ ) gives  $h=0.4814\text{m}$

Answer:- Alternate depths are  $3.95\text{m}$  and  $0.481\text{m}$ .

# Assignment #2

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## Problem #1

Solution:-

Check Froude Number

$$Fr = \frac{V}{\sqrt{gy}} = \frac{6 \text{ m/s}}{\sqrt{9.81/\text{s}^2 \cdot 0.1 \text{ m}}} = 6.06 > 1$$

So the flow is supercritical

$$E = y + \frac{V^2}{2g} = 0.1 \text{ m} + \frac{(6 \text{ m/s})^2}{2 \cdot 9.81 \text{ m/s}^2} = 1.935 \text{ m}$$

Solving for alternate depth for an  $E = 1.935 \text{ m}$   
Fields  $y_{alt} = 1.93 \text{ m}$

# Assignment #2

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## Problem: 2

SOLUTION:-

$$\Sigma_1 = y_1 + \frac{v_1^2}{2g} = 3\text{m} + \frac{(2\text{m/s})^2}{2 \cdot 9.81\text{m/s}^2} = 3.20\text{m}$$

$$\Sigma_2 = \Sigma_1 - \Delta z = 3.20\text{m} - 0.60\text{m} = 2.60\text{m}$$

Also

$$\Sigma_2 = y_2 + \frac{v_2^2}{2gy_2} = y_2 + \frac{(6\text{m}^2/\text{s}/\text{m})^2}{2 \cdot 9.81\text{m/s}^2 \cdot y_2} = 2.60\text{m}$$

So  $y_2 = 2.24\text{m}$ .  $\Delta y = y_2 - y_1 = 0.76\text{m}$  & water surface drops 0.16m  
For a downward step of 15cm we have

$$\Sigma_2 = \Sigma_1 - \Delta z = 3.20\text{m} - (-0.15\text{m}) = 3.35\text{m}$$

Giving  $y_2 = 3.17\text{m}$  and  $\Delta y = y_2 - y_1 = 0.17\text{m}$  & water surface rises 0.02m

The maximum upstep possible before affecting stream water surface less is for  $y_2 = y_c$

$$y_c = \sqrt{\frac{v^3}{g}} = \sqrt{\frac{(6\text{m}^2/\text{s}/\text{m})^3}{9.81\text{m/s}^2}} = 1.54\text{m}$$

# Assignment #3

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## Problem #1

Given Data:-

$$y_1 = 3.6 \text{ m}$$

$$b = 3.9 \text{ m}$$

$$y_2 = 0.9 \text{ m}$$

Sol:-

As we know that

$$\epsilon_1 = \epsilon_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \quad \text{--- (1)}$$

Also

$$Q = A_1 v_1 = A_2 v_2$$

$$b_1 y_1 \cdot v_1 = b_2 y_2 \cdot v_2$$

$$(b = b_1 = b_2)$$

$$b \cdot y_1 \cdot v_1 = b \cdot y_2 \cdot v_2$$

$$y_1 \cdot v_1 = y_2 \cdot v_2$$

$$v_2 = y_1 / y_2 \times v_1$$

$$\boxed{v_2 = 4v_1} \quad \text{--- (2)}$$

Putting in Eq

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$\Rightarrow 3.6 + \frac{v_1^2}{2g} = 0.9 + \frac{(4v_1)^2}{2g}$$

$$3.6 + \frac{v_1^2}{2g} = 0.9 + \frac{16v_1^2}{2g}$$

$$\frac{v_1^2}{2g} - \frac{16v_1^2}{2g} = 0.9 - 3.5$$

$$\frac{v_1^2 - 16v_1^2}{2g} = -2.7$$

$$\frac{15v_1^2}{2g} = +2.7$$

$$v_1^2 = \sqrt{\frac{2.7 \times 2(9.81)}{15}}$$

$v_1 = 1.879 \text{ m/sec}$  → putting it in Eq (2)

$$v_2 = 4v_1$$

$$v_2 = 4(1.879) \rightarrow v_2 = 7.516 \text{ m/sec}$$

$$Q_1 = A_1 v_1 = b \cdot y_1 \cdot v_1 = 3.9 \times 3.6 \times 1.879$$

$$Q_1 = 26.38 \text{ m}^3/\text{sec}$$

$$Q_2 = A_2 v_2 = b \cdot y_2 \cdot v_2 = 3.9 \times 0.9 \times 7.516$$

$$Q_2 = 26.38 \text{ m}^3/\text{sec}$$

$$Q = Q_1 = Q_2 = 26.38 \text{ m}^3/\text{sec}$$

① FRAUD NUMBER → At upstream side

$$Fr_1 = \frac{v_1}{\sqrt{g y_1}} = \frac{1.879}{\sqrt{9.81 \times 3.6}} = 0.31$$

Sub-critical flow



② Froude Number  $\rightarrow$  At Downstream Side

⑧

$$Fr_2 = \frac{V_2}{\sqrt{gy_2}} = \frac{7.516}{\sqrt{9.81 \times 0.92}} \rightarrow \text{At Downstream Side}$$

$$= 2.52$$

$\rightarrow$  Super Critical flow.