

Name

Number

Column

Ad

14455

depth

Bees

Assign

probability

Q 1:-

$$np = 4$$

1) variance = 3

2) dividing the LHS & RHS = $\frac{3}{4} = 1 - \frac{3}{4} = \frac{1}{4}$
we have $N = 16$

$$p = \frac{1}{4}$$

B :-

A critical region also known as the rejection region is a set of values for the test statistics for which the null hypothesis is rejected. If the observed test statistics is in the critical region then we reject the null hypothesis & accept the alternative hypothesis.

C

• The mean of the distribution is equal to 0.

• The variance is equal to $\frac{v}{(v-2)}$ where v is the degree of freedom.

• The variance is always greater than 1.

D :-

Analysis of variance or ANOVA is a statistical method that separates observed variance

data into diff components to use for additional test. A one way ANOVA is used for three or more groups of data to gain info about the relationship between the dependant & independent variables.

E:-

A diagram that gives the relationship b/w the component states & the success or of a specified system function. The logical layout in our RBD can be of series system parallel or a combination.

F:-

Statistical quality control: the use of statistical method in the monitoring and maintaining of the quality of products.

G:-

Chance cause: A process that is operating with only chance causes of variation present.

Assignable cause:-

is a type of variation in which a specific identity or event can be linked to inconsistency in a system.

H:-

Traffic intensity:-

A measure of the average occupancy of the facility during a specified period of time, normally a busy hour measured in traffic units during which a facility is occupied to the time the facility is available for occupancy.

I:-

A queuing system is specified completely by the following five basic characteristics. The input process it expresses the mode of arrival the customer at the service facility governed by some probability law the no of customer finite or infinite sources.

QNO # 2

(A)

$$\begin{aligned} E(X) &= \sum_{x=0}^n x \binom{n}{x} p^x (1-p)^{n-x} \\ &= \sum_{x=0}^n x \frac{n!}{x(n-x)!} p^x (1-p)^{n-x} \\ &= \sum_{x=0}^n \frac{n!}{(x-1)(n-x)!} p^x (1-p)^{n-x} \end{aligned}$$

Since there $x=0$ term variables. let $y = x-1$
& $m = n-1$ Subbing $x = y+1$ & $n = m+1$
into the last sum (& using the fact that
the limits $x=1$ & $x=n$ correspond to $y=0$
& $y = n-1 = m$, respectively)

$$\begin{aligned} E(X) &= \sum_{y=0}^m \frac{(m+1)!}{y(m-y)!} p^{y+1} (1-p)^{m-y} \\ &= (m+1)p \sum_{y=0}^m \frac{m!}{y!(m-y)!} p^y (1-p)^{m-y} \\ &= mp \sum_{y=0}^m \frac{m!}{y!(m-y)!} p^y (1-p)^{m-y} \end{aligned}$$

The binomial theorem say that

$$(a+b)^m = \sum_{y=0}^m \frac{m!}{y!(m-y)!} a^y b^{m-y}$$

Setting $a = p$ & $b = 1-p$

$$\sum_{y=0}^m \frac{m!}{y!(m-y)!} p^y (1-p)^{m-y} = \sum_{y=0}^m \frac{m!}{y!(m-y)!} a^y b^{m-y} = (a+b)^m = (p+1-p)^m = 1$$

So that

$$E(x) = np$$

Similarly but this time using $y = x-2$ $\{m = n-2$

$$E(x(x-1)) = \sum_{x=0}^n x(x-1) \binom{n}{x} p^x (1-p)^{n-x}$$

$$= \sum_{x=0}^n x(x-1) \frac{n!}{x!(n-x)!} p^x (1-p)^{n-x}$$

$$= \sum_{x=2}^n \frac{n!}{(x-2)!(n-x)!} p^x (1-p)^{n-x}$$

$$= n(n-1)p^2 \sum_{x=2}^n \frac{(n-2)!}{(x-2)!(n-x)!} p^{x-2} (1-p)^{n-x}$$

$$= n(n-1)p^2 \sum_{y=0}^{m} \frac{m!}{y!(m-y)!} p^y (1-p)^{m-y}$$

$$= n(n-1)p^2 (p + (1-p))^m$$

$$= n(n-1)p^2$$

So the variance of x is

$$E(x^2) - E(x)^2 = E(x(x-1)) + E(x) - E(x)^2 = n(n-1)p^2 + np - (np)^2$$

$$= np(1-p)$$

part (b)

let x denote numbers of cars hired out per day

Poisson distribution mean = $m = 1.5$

$$P(x=x) = \frac{(e^{-m} m^x)}{x!} = \frac{(e^{-1.5} 1.5^x)}{x!}$$

1) $P(\text{neither car is used})$

$$= \frac{(e^{-1.5} 1.5^0)}{0!} = 0.2231$$

$$P(x=0) = \frac{(e^{-1.5} 1.5^0)}{0!} = 0.2231$$

2) $P(\text{Some demand is refused}) = P(\text{Demands is more than 2 cars per day})$

$$\begin{aligned}
 &= P(x > 2) \\
 &= 1 - P(x \leq 2) \\
 &= 1 - [P(x=0) + P(x=1) + P(x=2)] \\
 &= 1 - \left[\frac{(e^{-1.5})(1.5^0)}{0!} + \frac{(e^{-1.5})(1.5^1)}{1!} + \frac{(e^{-1.5})(1.5^2)}{2!} \right] \\
 &= 1 - e^{-1.5} [1 + 1.5 + (2.25/2)] = 0.1912 \text{ proportion of} \\
 &\text{days on which neither car is used} \\
 &= 0.2231 = 22.31\% \\
 &\text{proportion of days on which some demands} \\
 &\text{is refused} = 0.1912 = 19.12\%
 \end{aligned}$$

QNO#3

