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SECTION = A

PAPER = PRCD I

QUESTION NO = 01

GIVEN DATA:-

$$\text{Width } (b) = 10'$$

$$\text{Height } (h) = 20''$$

$$\text{Live load (L.L)} = 2.47 \text{ Kips/ft}$$

$$\text{Dead load} = 1.05 \text{ Kips/ft}$$

$$\text{Span} = 18'$$

$$f_c = 4000 \text{ psi} = 4 \text{ ksi}$$

$$f_y = 60000 \text{ psi} = 60 \text{ ksi}$$

SOLUTION:-STEP# 01:-

Finding Effective depth (d)

$$d = h - 3 \Rightarrow 20 - 3 = 17''$$

$$(d) = 17''$$

$$\text{Effective cover} = 2.5''$$

REINFORCEMENT RATIO:-

We have

$$\rho_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$\rho_{max} = 0.85 \times 0.85 \times 4/60 \times \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$\rho_{max} = 0.04816 \quad (0.375)$$

$$\rho_{max} = 0.0180$$

STEP # 02

Now we have to find Area of steel

We know that

$$\rho_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = \rho_{max} (b \times d)$$

$$A_{st} = 0.0180 (10 \times 17) \Rightarrow 0.0180 (170)$$

$$A_{st} = 3.06 \text{ in}^2$$

Step#03:-

Design Moment formula
we know that

$$M_{u2} = \phi \times A_{st} \times f_y \times (d - a/2)$$

$$\text{Where } a = \frac{A_{st} \times f_y}{0.85 \times f_c \times b} = \frac{3.06 \times 60}{0.85 \times 4 \times 10} = 5.4''$$

$$a = 5.4''$$

$$M_{u2} = 0.90 \times 3.06 \times 60 \times (17 - 5.4/2)$$

$$M_{u2} = 2362.93 \text{ kip-inch}$$

$$M_{u2} = 2362.93 \text{ kip-in}$$

MOMENT DUE TO GIVEN LOAD:-

$$\text{Beam self weight} = 10/12 \times 20/12 \times 150$$

$$= 208.33 \text{ lb/ft}$$

$$\text{Total factored load} = 1.2(1050 + 208.33)$$

$$+ 1.6(2470) \Rightarrow 5461.99 \text{ lb/ft}$$

$$\Rightarrow 5.46 \text{ kips/ft}$$

ultimate factored Moment

We have

$$wL^2/8 \Rightarrow \frac{5.46 \times (18)^2}{8} \times 12 = 2653.56$$

$$MU = 2653.56$$

Now as, $MU_2 < MU$

$2362.92 < 2653.56$ (Doubly Reinforcement Required)

STEP # 04:-

$$MU_1 = MU - MU_2$$

$$MU_1 = 2653.56 - 2362.92$$

$$MU_1 = 290.64 \text{ Kip}^2\text{-inch}$$

STEP # 05:-

Steel Area in compression Zone is;

$$MU_1 = \phi \times A_{st} \times f_y \times (d - d_1)$$

$$\text{So, } A_{st} = \frac{MU_1}{\phi \times f_y \times (d - d_1)}$$

$$= \frac{290.64}{0.90 \times 60 \times (17 - 2.5)} = 0.37 \text{ in}^2$$

$$A_{st} = 0.37 \text{ in}^2$$

STEP # 06:-

$$A_s = A_{st} + A_{s'} \Rightarrow 3.06 + 0.37 = 3.43 \text{ in}^2$$

$$A_s = 3.43 \text{ in}^2$$

STEP # 07:-

We can use #8 bar. (Dia = 8/8 = 1"

Area = 0.785 in²

No. of bars = $\frac{A_{st}}{\text{Area of 1 bar}}$

= 3.43 / 0.785 => 4.36 ≈ 5 bars

5 # 8 bars (Tensile Zone)

For compression steel:

use #6 bars (dia 6/8 = 0.75)

Area = 0.44 in²

No. of bars = $\frac{A_{st}}{\text{Area of 1 bar}} = \frac{0.377}{0.44} = 0.84$

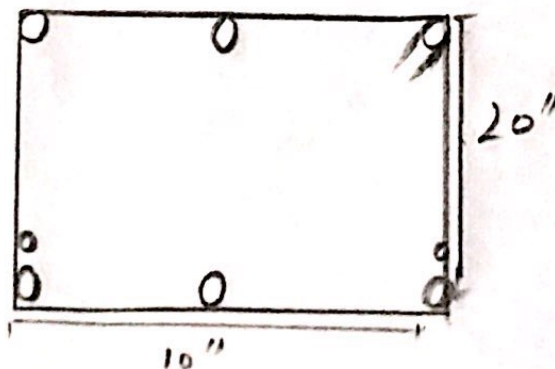
=> 0.84 ≈ 1 bar

1 # 6 bars (compression Zone)

STEP # 08:-

Minimum beam width

$b_{min} = 2(1.5) + 2(3/8) + 5(8/8) + 4(8/8)$
 $= 12.75 > 10''$ (Multiple layer)



$$\text{Effective depth } (d) = 20 - 1.5 - 3/8 - 8/8 - 1/2 (8/8)$$

$$d = 16.62''$$

$$\text{Effective cover } (d') = 1.5 + 3/8 + 1/2 (6/8)$$

$$d' = 2.25''$$

STEP # 09:-

We have to given design moment

$$M_d = \phi \times \left[A_{st} \times f_y \times (d - d') + (A_{st} - A_{s't}) \times f_y \times (d - a/2) \right]$$

$$a = \frac{(A_{st} - A_{s't}) \times f_y}{0.85 \times f_c \times b}$$

$$= \frac{(5 \times 0.785 - 1 \times 0.44) \times 60}{0.85 \times 4 \times 16} = 6.15''$$

$$a = 6.15''$$

$$M_d = 0.90 \times \left[(1 \times 0.44) \times 60 \times (16.62 - 2.25) + (5 \times 0.785 - 1 \times 0.44) \times 60 \times (16.62 - 6.15/2) \right]$$

$$M_d = 2890.46$$

$$M_d = 2890.46 > 2653.56$$

(Design is OK)

QUESTION NO = 02 (Part = A)⇒ BOND STRESS:-

The stress which is acting on the outer interface of steel to the surrounding concrete is called bond stress.

This stress help in keeping the bond b/w Reinforcement and concrete together.

Bond stress resist any force that tries to pull out the rods from the concrete.

When we try to pull out the Reinforcement bar from hardened concrete, then this bond stress resists the bar to come out.

DEVELOPMENT LENGTH:-

The development length can be defined as the amount of Reinforcement (bar) length needed to be embedded or projected into the column to established

the desired bond stress between the concrete and steel.

To develop a safe bond between the bar surface and the concrete so that no failure due to slippage of bars occurs during the ultimate load condition.

QUESTION NO=2 (part=B)

We provided doubly Reinforced beam due to the following. Which are given below.

- 1) When the cross sectional of the beam is fixed.
- 2) When there is a torsion on the beam.
- 3) When Moment to be carried by the beam is more than the balanced Moment.
- 4) Doubly Reinforced beam is always used for safety Reason, To counter wind force and temperature stresses.

QUESTION NO = 02 (part = C)

T-BEAM:-

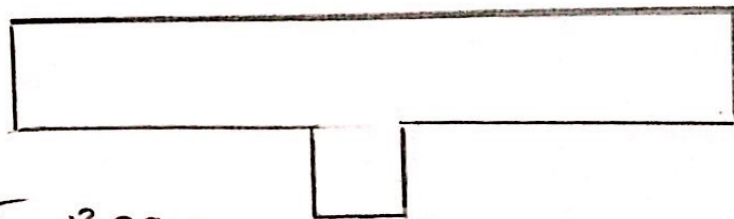
When slab are monolithically casted with beams in a positive Moment Zone, part of the slab act as a part of the beam and Resists the longitudinal compression.

⇒ T-Beam are Mostly used in heavy duty and large space such as bridges.

⇒ T-Beam are more economical than Rectangular beam.

⇒ The design procedure of T-beam depend on the location of Moment as the case of it's flexural strength

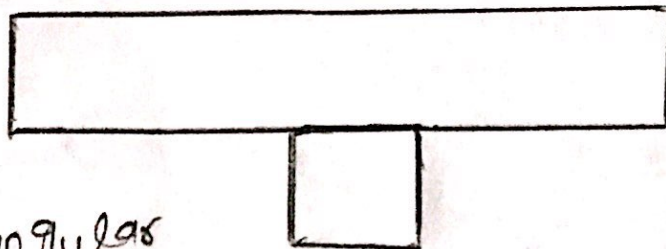
⇒ Shape of the T-beam is;



T-Beam

RECTANGULAR BEAM:-

- ⇒ The Rectangular beam is generally used as compression in top fibre and tension in bottom fibre of that beam.
- ⇒ Rectangular beams are mostly used in commercial building.
- ⇒ Rectangular beam are less economical as compared to T-beam.
- ⇒ In case of Rectangular beam, slab has been placed on the beam, so there is no connection b/w slab and beam.
- ⇒ Shape of Rectangular beam is;



Rectangular beam

QUESTION NO# 02 (part#1)

EFFECT OF STRENGTH REDUCTION FACTOR ON FLEXURAL STRENGTH:-

In the design of flexural strength, the strength reduction factor decreases from tension controlled section to compression.

controlled section to increase safety with decreasing ductility. This shows that to determined the reduction factor for flexural strength of reinforced concrete beam according to ACI. In the reliability based design the Reliability prediction of the f_{cr} flexural strength of Reinforced concrete member is assured by the use of the reduction factor corresponding to different target Reliability Index.

DESIGNING METHOD:-

There are two methods of designing of concrete.

1) ALLOWABLE STRESS DESIGN:-

Allowable stress design is referred as the service load design or working stress design.

The basic concept of this method is that the maximum stress in a structural member is always smaller than a certain allowable stress in bridge working.

The allowable stress of a material determined according to its normal strength over the safety factor.

2) ULTIMATE STRENGTH DESIGN METHOD

ultimate strength design method is also known as factor method or ultimate load factor.

ultimate strength design method produces a more rational and economical design compared to working stress design method.

The ultimate strength design method utilize a more realistic factor of safety.

In this method, the Reinforced concrete structure is design beyond the elastic region.

QUESTION NO = 03GIVEN DATA:-

c/c distance = 10'

Span = 32'

Web width = 14"

Effective depth = 28" - 3" = 25"

Total depth = 28"

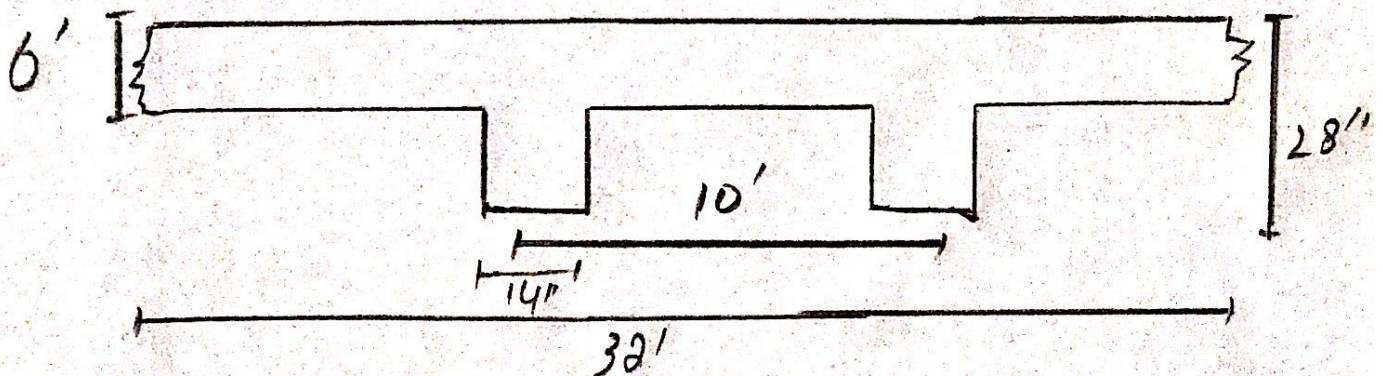
Slab thickness = 6"

D.L = 50 lb/ft²

S.S = 225 lb/ft²

$\psi_f = 60000 \text{ psi}$

$\psi'_c = 4000 \text{ psi}$

SOLUTION:-

STEP#01:-

We know that

$$MU = \frac{w_u \times L^2}{8}$$

Beam self weight per feet

$$wt = b \times t \times \rho c = 14/12 \times 28/12 \times 150$$

$$wt = 1.666 \times 2.333 \times 150 \Rightarrow 408.33$$

$$wt = 408.33 \text{ lb/ft}$$

Total factored load:-

$$\Rightarrow 1.2(50 + 408.33) + 1.6(225)$$

$$= 909.99 \text{ lb/ft} = 0.909 \text{ kip/ft}$$

MOMENT:-

We have to given that

$$wL^2/8 \Rightarrow \frac{0.909(32)^2 \times 12}{8} = 1396.23 \text{ kip-m}$$

Effective Breadth:-

1) $b(h_f) + bw = (16)(6) + 14 = 110''$

2) c/c distance = $10(12) = 120''$

3) span/4 = $32/4 \times 12 \Rightarrow 96''$

so $b_e = 96''$

STEP# 03:- (Rectangular OR T-beam)

Trial #01:- let $a = hf = 6''$

We know that

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{1396.23}{0.90 \times 60 \times (25 - 6/2)}$$

$$A_{st} = 1.17 \text{ in}^2$$

Trial #02:- Where

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{1.17 \times 60}{0.85 \times 4 \times 96}$$

$\Rightarrow 0.2'' < 6''$ (Rectangular beam design)

$$A_{st} = \frac{1396.23}{0.90 \times 60 \times (25 - 0.2/2)}$$

$$A_{st} = 1.03 \text{ in}^2$$

Trial #03:-

$$a = \frac{1.03 \times 60}{0.85 \times 4 \times 96} = 0.18''$$

$$A_{st} = \frac{1396.23}{0.90 \times 60 \times (25 - 0.18/2)} = 1.03 \text{ in}^2$$

$$A_{st} = 1.03 \text{ in}^2$$

STEP # 04:-Finding f_{max} And f_{min}

$$f_{max} = 0.85 \times 0.85 \times 4 / 60 \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$f_{max} = 0.018$$

 f_{min} is given by;

$$200 / 60000 = 200 / 60000 = 0.003$$

$$f_{min} = 0.003$$

$$f = \frac{A_{st}}{b \times d} = 1.03 / 14 \times 25 = 0.0029$$

$$f = 0.0029$$

$$f_{min} < f < f_{max}$$

$$0.003 < 0.0029 < 0.018$$

As we know that
 f is less than f_{min}

$$f = A_{st} / b \times d \Rightarrow A_{st} = f_{min} \times b \times d$$

$$A_{st} = 0.003 \times 14 \times 25 \Rightarrow 1.05 \text{ in}^2$$

$$A_{st} = 1.05 \text{ in}^2$$

STEP#05:- SELECTION OF BAR

We use #8 bars; then

$$\text{dia}(8/8) = 1'' \text{ and Area} = 0.785 \text{ in}^2$$

$$\text{No. of bars} = \frac{1.05}{0.785} = 1.31 \approx 2$$

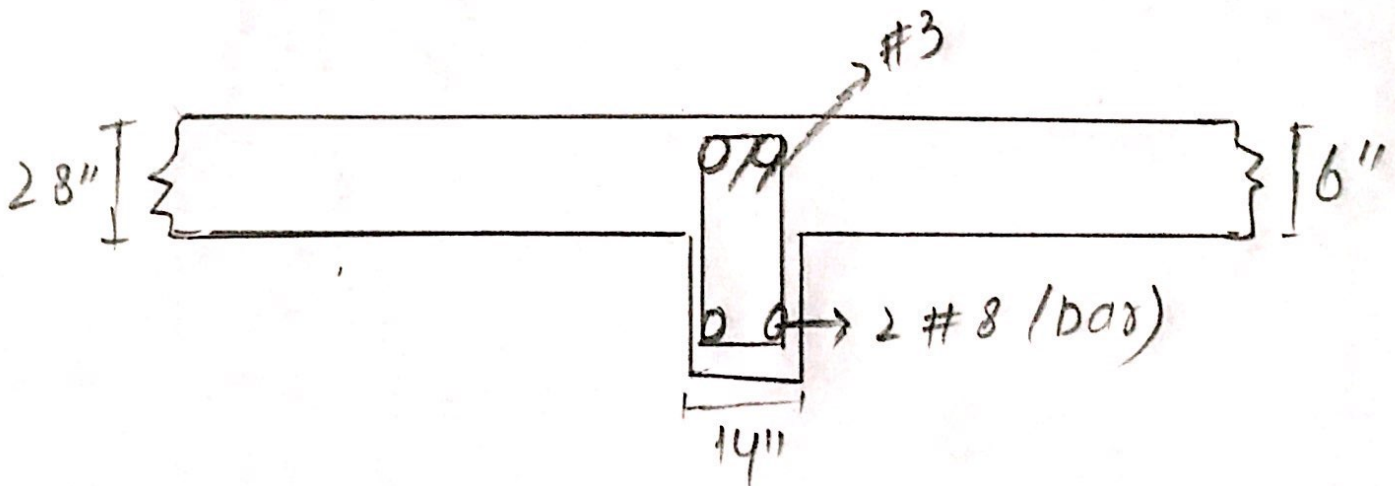
So we use 2 #8 bars.

STEP#06:-

NOW we have to find
Minimum width

$$b_{\text{min}} = 2(1.5) + 2(3/8) + 2(8/8) + 1(8/8)$$

$$\Rightarrow 6.75'' < 14'' \text{ (Good in one layer)}$$



STEP#07:- Design Moment

We have

$$M_d = \phi \times D \times A_{st} \times (d - a/2)$$

$$\begin{aligned} \text{Area of steel} &= \text{Area of 1 bar} \times \text{No. of bar} \\ &= 0.785 \times 2 \Rightarrow 1.57 \text{ in}^2 \end{aligned}$$

Where

$$d = \frac{1.57 \times 60}{0.85 \times 4 \times 96} = 0.2''$$

$$\begin{aligned} \Rightarrow Md &= 0.90 \times 60 \times 1.5 \times (25 - 0.2/2) \\ &= 2111.02 \text{ kip-in} \end{aligned}$$

As; $2111.02 > 1396.23$

(Design is OK),