

Date: _____

Name:- Ali Hasnain

ID:- 966

Subject:- Numerical Analysis

Submitted:- Mamm Ahonalia Mazhar

Date:- 09-09-2020

Assignment:- 01.

Date: _____

①

Q1: Review of Integration Concept.

Ans: It contains some major concepts of integration, including.

- Substitution method.
- Integration by Parts.
- Integration of Rational function.

* Substitution method:

$$\rightarrow \int f(g(x))g'(x)dx = \int f(u)du.$$

If the function $f(u)$ has an easily identifiable antiderivative then all is well. If not, another substitution method may be needed.

* Integration by parts:

$$\begin{aligned} \rightarrow [u(x)v(x)]' &= u'(x)v(x) + u(x)v'(x) \\ &= u(x)u'(x) = [u(x)v(x)]' - u'(x)v(x) \\ &= \int u(x)v'(x)dx = u(x)v(x) - \int u'(x)v(x)dx \\ &= \int u dv = uv - \int v du \end{aligned}$$

Date: _____

②

In case of definite integrate we use

$$\int_a^b u(x)v'(x) dx = [u(x)v(x)]_{x=a}^{x=b} - \int_a^b u'(x)v(x) dx$$

1) "Integrating Rational Function."

$$\Rightarrow \frac{3x+2}{2x^2+x-3} = \frac{3x+2}{(2x+3)(x-1)}$$

To integrate such a function, we use the method of partial fraction to split the fraction into easily integrable pieces.

$$\frac{3x+2}{(2x+3)(x-1)} = \frac{1}{2x+3} + \frac{1}{x-1}$$

$$\text{Now } \int \frac{3x+2}{2x^2+x-3} dx = \frac{1}{2} \log(2x+3) + \log(x-1) + c$$

Q2:- Application of Trapezoidal Rule & Simpson's Rule in Engineering.

Ans:- "Application of Trapezoidal Rule:-"

- The trapezoidal rule is one of the family member of numerical integration formula.
- The trapezoidal rule has faster convergence.
- Moreover, the trapezoidal rule tends to become extremely accurate when periodic functions.

→ "Application of Simpson's Rule:-"

- Simpson's Rule is a ~~number~~ numerical method for approximating the integral of a function between two limits, a to b . It's based on knowing the area under a parabola, or a plane curve.
- It include the (a) calculation of a vessel's displacement, total wetted surface area, and the calculation of a vessel's displacement, total wetted surface area, the calculation of the longitudinal center of buoyancy of the hull.

It is a weighted average that results in an even more accurate approximation.