

Name :- Mian Zeeshanul Haq

ID :- 7906

Section :- A

Subject :- Structure - I

Assignment :- 03

Engr Amjid Islam

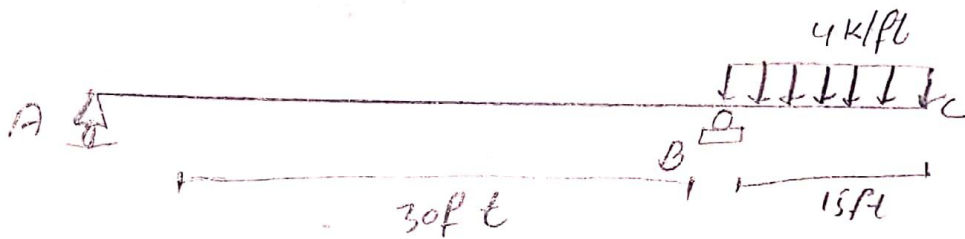
Date :- 13 July - 2020

---

①

## Assignment No: 3

Determine the slope and displacement at C.  $EI$  is constant. Use the moment-area theorems.



Solution:

$$+\uparrow \sum M_A = 0$$

$$-V_B \times 30 + (4 \times 15) \times 3.75 = 0$$

$$V_B = 75 \text{ k}$$

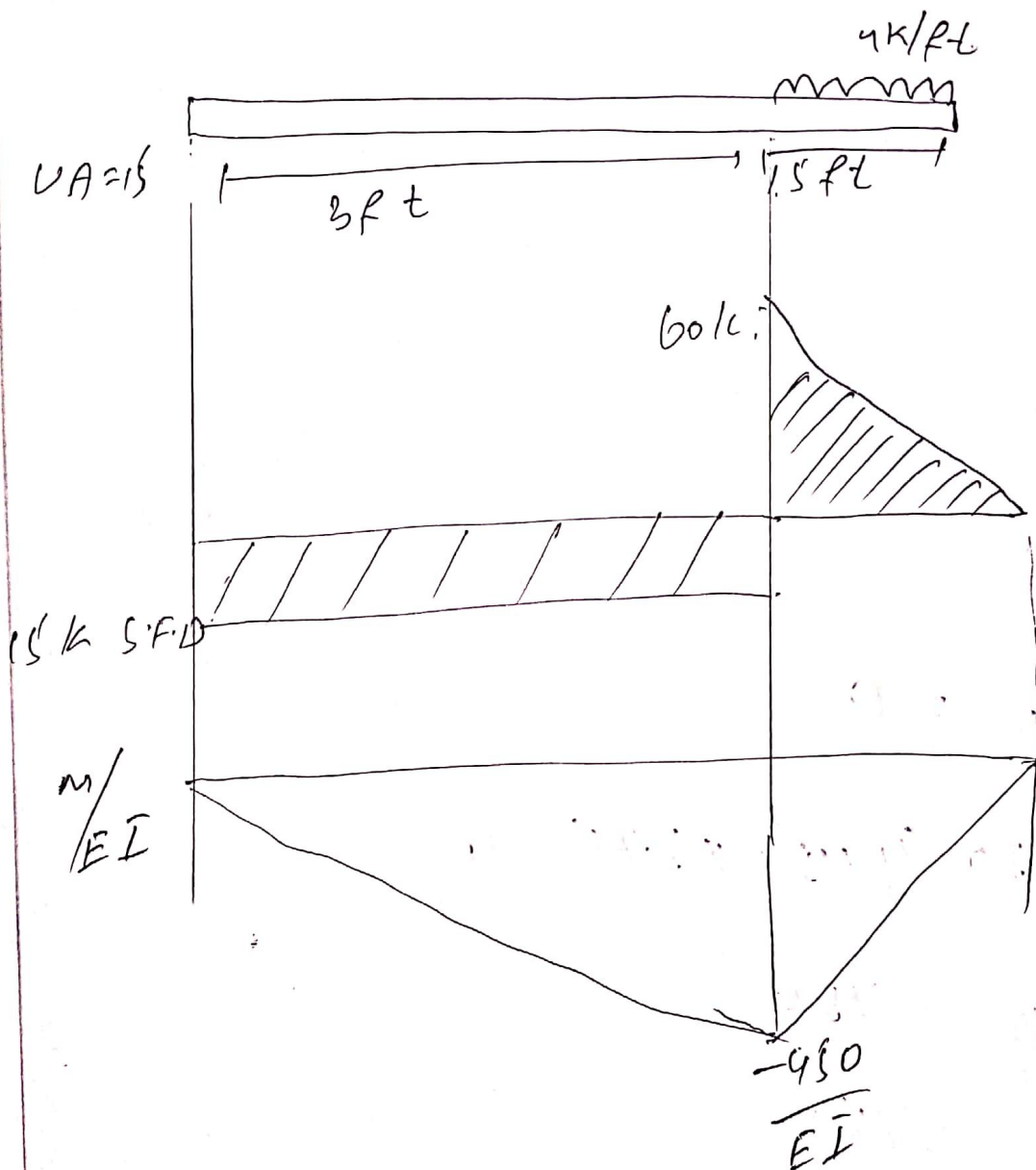
$$V_B = 75 \text{ k}$$

$$\downarrow \sum M_B = 0$$

(2)

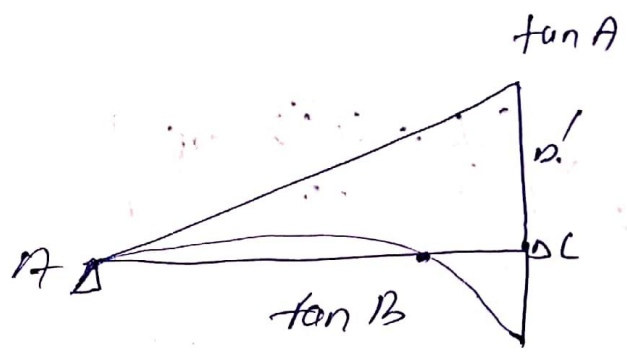
$$U_A \times 30 + (4 \times 15) \times 7.5 = 0$$

$$U_A = -15 \text{ k}$$



Thus  $M/EI$  consist of triangle and parabol segment

For displacement



$$\tan A = DC + D'$$

$$DC = \tan A - D' \rightarrow (1)$$

$$\frac{D'}{45} = \frac{\tan B}{30}$$

$$D' = \frac{3}{4} \tan B$$

eq (1)

$$DC = \tan A - \frac{3}{4} \tan B$$

(4)

$t_c/a :$

$$t_c/A = \left[ \frac{-450}{EI} \times 30 \times \frac{1}{2} \right] \times \left[ 15 + \frac{1}{3} \times 30 \right]$$

$$+ \left[ \frac{3}{4} \times 15 \right] \times \left[ \frac{1}{3} \times \frac{450}{EI} \times 15 \right]$$

$$\frac{t_c}{a} = \frac{168750}{EI} - \frac{25312.5}{EI}$$

$$t_c/a = -194062.5 / EI$$

$$t_c/a = -194062.5 / EI$$

for  $t_B/a :$

$$t_B/A = \left[ \frac{-450}{EI} \times \frac{30}{2} \right] \times \left[ \frac{1}{3} \times 30 \right]$$

$$t_B/A = -67500 / EI$$

(5)

$$DC = \frac{-19406.5}{2} - \left( \frac{67500}{EI} \right) \times \frac{3}{2}$$

$$DC = \frac{-295312.5}{EI} \text{ k}\cdot\text{ft}^3$$

for slope at B

$$\begin{aligned} \theta_B &= \frac{DC}{15} \\ &= \left( \frac{295312.5}{EI} \right) / 15 \end{aligned}$$

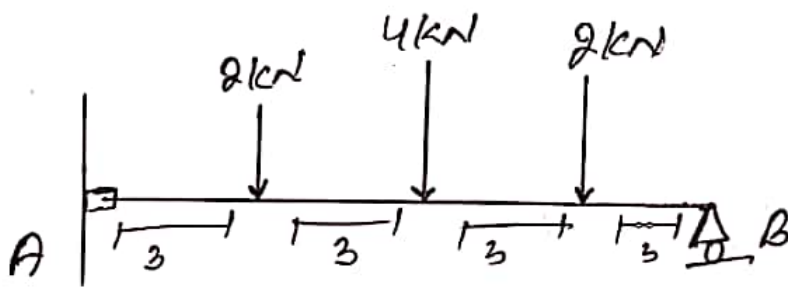
$$\theta_B = \frac{19687.5}{EI} \text{ k/ft}^2$$

slope of the free end at point C.

it nearly equal to zero



Determine the slope  $\theta^A$  and displacement at C of the beam in the figure by moment area theorem. Take  $E = 200 \text{ GPa}$ .  
 $I = 6(10^6) \text{ mm}^4$



Required:-

$$\theta^A = ?$$

$$\Delta_C = ?$$

And in the question we have given the following data.

$$E = 200 \text{ GPa} = 200 \times 10^9 \text{ Pa}$$

$$I = 6 \times 10^6 \text{ mm}^4 = 6 \times 10^{-6} \cdot 10^{-12} \text{ m}^4$$

$$I = 6 \times 10^{-6} \text{ m}^4$$



First we find support Reaction

$$\sum F_y = 0 \uparrow^+ \downarrow^-$$

$$R_A + R_B = 8$$

$$\sum M = 0 \curvearrowright^+ \curvearrowleft^-$$

$$-R_B \times 12 + 2 \times 9 + 4 \times 6 + 2 \times 3 = 0$$

$$-12R_B + 18 + 24 + 6 = 0$$

$$\frac{12R_B}{12} = \frac{48}{12}$$

$$\boxed{R_B = 4}$$

As we know that

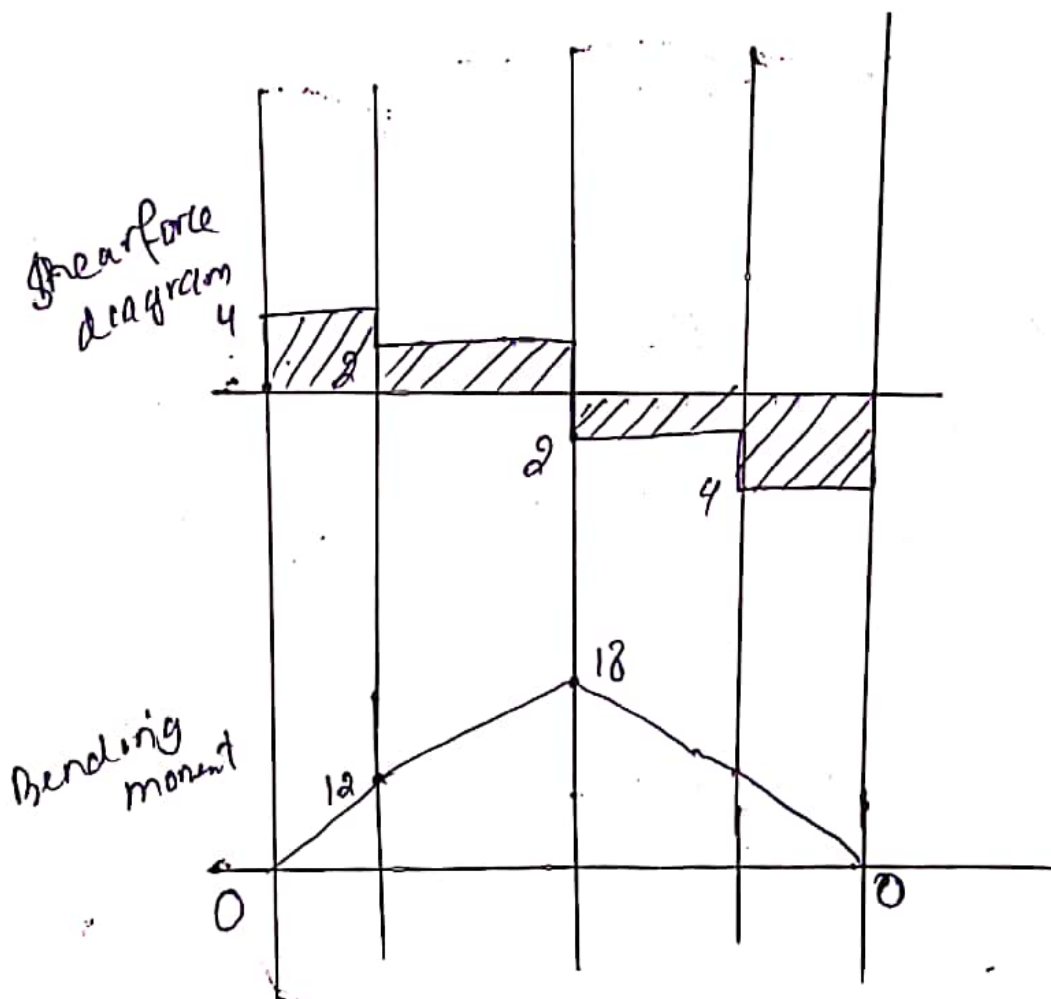
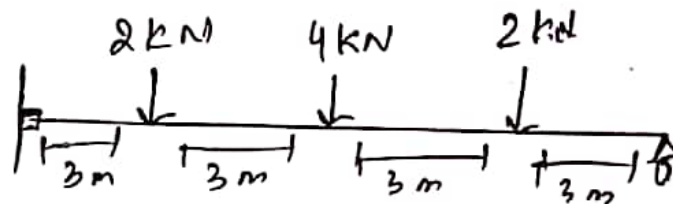
$$R_A + R_B = 8$$

$$R_A + 4 = 8$$

$$\boxed{R_A = 4}$$

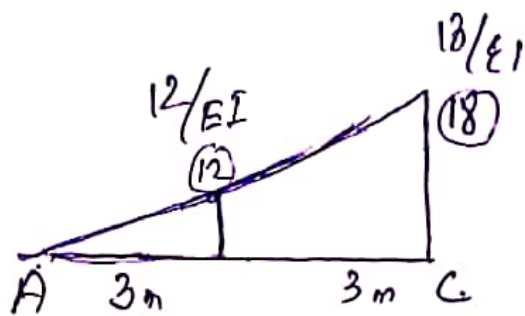


Now we draw the Bending diagram of the following beam.



First we find the slope at point "A" of the beam.

$Q_A \Rightarrow$  Area b/w the points A and C.



$$Q_A = \left( \frac{12 \times 3}{2} \right) + \left( \frac{12 + 18}{2} \right) \times 3 = \frac{63}{EI} \text{ (1/m)}^2$$

As from the question:

$$E = 200 \times 10^9 \text{ Pa}$$

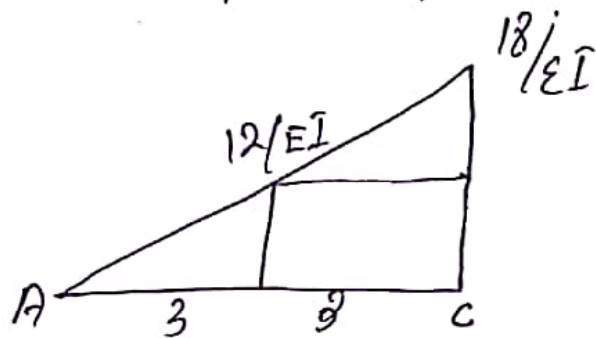
$$I = 6 \times 10^{-6} \text{ m}^4$$

$$Q_A = \frac{63}{200 \times 10^9 \times 6 \times 10^{-6}}$$

$$Q_A = 0.0525 \text{ rad}$$

Now we find the deflection at (2) Point B' of the beam.

So,  $\Delta_c$  (deflection at mid-span) will be equal to first moment of area between point A and C.



$$\Delta_c = \frac{2}{3} \times 3 \left( \frac{12 \times 3}{2} \right) + \left[ \left( 3 + \frac{3}{2} \right) (12 \times 3) \right] + \left[ \left( 3 + \left( \frac{2}{3} \times 3 \right) \right) \left( \frac{2 \times 6}{2} \right) \right]$$

$$\Delta_c = 36 + 162 + 45 \Rightarrow 243 \text{ KN}\cdot\text{m}^3 / EI$$

$$\Delta_c = \frac{243 \times 10^3 \text{ m}^3}{200 \times 10^9 \times 6 \times 10^{-6}}$$

$$\Delta_c = 0.2025 \text{ m}$$

