

Sec A

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ID# 7549

Summer 2020

Q no 1

Lightest W-shape Column

A36 Steel

DL = 60k

L.L = 110k

Pin supported at top and bottom

 $K_x L_x = 36 \text{ ft}$ $K_y L_y = 18 \text{ ft}$

AISC/LRFD Method

Sol

Required Capacity = $(1.2 \times 60) + (1.6 \times 110)$ $= 248 \text{ k}$ Enter design strength table of manual
with $KL = 18 \text{ ft}$ and $P = 248 \text{ k}$

Some possible section are

W14 x 16

 $P = 364$ $\lambda_n / \lambda_y = 2.44$

W12 x 53

 $P = 320$ $\lambda_n / \lambda_y = 2.11$

W10 x 49

 $P = 301$ $\lambda_n / \lambda_y = 1.71$

W8 x 58

 $P = 300 \text{ k}$ $\lambda_n / \lambda_y = 1.74$

Now

$$\frac{K_x L_x}{K_y L_y} = \frac{36}{18} = 2$$

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Try $W_{12} \times S3$ $r_x / r_y = 2.11$

$$r_x / r_y > \frac{I_x / I_y}{k_y l_y}$$

$$r_x = 5.23 \quad r_y = 2.48 \quad A = 15.6 \text{ in}^2$$

$$\frac{I_x / I_y}{r_x} = \frac{36 \times 12}{5.23} = 82.6$$

$$\frac{k_y l_y}{r_y} = \frac{18 \times 12}{2.48} = 87.09$$

$$\frac{kL}{r} = 87.09$$

$$\lambda_c = \frac{kL}{r} \sqrt{\frac{F_y}{\pi^2}}$$

$$= \frac{87.09}{\pi} \sqrt{\frac{36}{29,000}}$$

$$= 0.097 < 1.5$$

$$F_{cr} = 0.658 \lambda^2 \times F_y$$

$$0.658^{(0.097)^2} \times 36$$

$$F_{cr} = 24.28$$

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$$P_n = A_g F_{cr}$$

$$= 15.6 \times 24.28$$

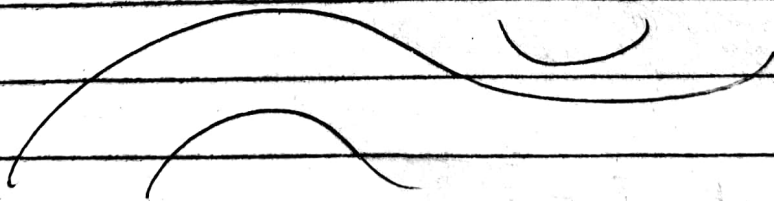
$$P_n = 378.781 \text{ k}$$

$$\phi P_n = 0.85 \times 378.78$$

$$= 321.96 > 248 \text{ k} \quad \text{OK}$$

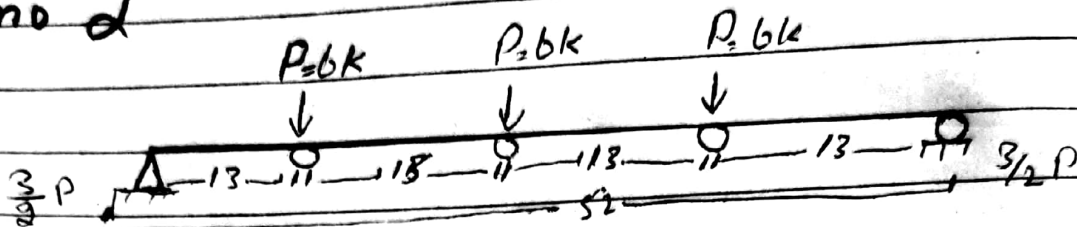
So

Use $W_{12} \times 53$



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Q no 2



Lightest W-Section

$$D.L = 1.5 \text{ k} \quad L.L = 4.5 \text{ k}$$

At each quarter point

$$\rightarrow \text{Total length} = 57'$$

$$\rightarrow \text{Live load deflection} = \frac{1}{360} \text{ of span}$$

\Delta_{lim}

$$\rightarrow F_y = 36 \text{ ksi}$$

AISC/ASD method

Sol

$$\text{Design load} = 4.5 + 1.5 = 6 \text{ k}$$

$$P = 6 \text{ k}$$

$$\Delta = \frac{5}{48} \frac{ML^2}{EI} \rightarrow \text{①}$$

\Delta by this equation is method multiplied by the factor from table 5.7

$$M = \left(\frac{3}{2} \times 6 \times 26 \right) - (6 \times 13) = 156 \text{ k}\cdot\text{ft}$$

$$Eqn \Rightarrow I = \frac{5}{48} \times \frac{ML^2}{EA} \times 0.95$$

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$$I = \frac{5}{48} \left(\frac{156 \times 12}{99,000} \right) \left(\frac{152 \times 12}{360} \right)^2$$

$$I = 1576.51 \text{ in}^4$$

Try $12 \times 24 \times 62$

$$I_x = 1550 \text{ in}^4$$

$$b_f = 7.04 \text{ in} \quad d/A_f = 5.72$$

$$L_c = \frac{7667}{\sqrt{F_y}} \Rightarrow \frac{76 \times (7.04)}{\sqrt{36}} = 89'' = 7.41$$

$$L_c = \frac{20,000}{F_y \frac{d}{A_f}} \Rightarrow \frac{20,000}{36 \times 5.72} = 97.12'' = 8.09'$$

$L > L_c$

from table S.2

$$C_b = 1.13$$

$$\sqrt{\frac{102,000 C_b}{F_y}} = \sqrt{\frac{102,000 \times 1.13}{36}} = 57$$

$$\sqrt{\frac{510,000 C_b}{F_y}} = \sqrt{\frac{510,000 \times 1.13}{3.6}} = 127$$

$$\frac{L}{r_T} = \frac{13 \times 12}{1.71} = 91.22$$

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Condition

$$\sqrt{\frac{162,000 \text{ lb}}{F_y}} \leq \frac{L}{r_T} \leq \sqrt{\frac{570,000 \text{ lb}}{F_y}}$$

So

$$F_b = \left[\frac{2}{3} - \frac{F_y (L/r_T)^2}{1530 \times 10^3 \times C_b} \right] F_y$$

$$= \left[\frac{2}{3} - \frac{36 (91.2)^2}{1530 \times 10^3 \times 1.13} \right] 36$$

$F_b = 17.76 \text{ ksi}$ allowable

The beam self weight = $62 \text{ lb} = 0.062 \text{ k/ft}$
67

$$M = \frac{WL^2}{8} = \frac{1}{8} (0.062)(782)^2$$

$$M = 20.95 \text{ k-ft}$$

$$\text{Total } M = 156 + 20.95$$

$$M = 176.95$$

$$f_b = \frac{M}{S_x} \Rightarrow \frac{176.95 \times 12}{131} = 16.2 \text{ ksi}$$

$$f_b < F_b \quad \text{OK}$$

Use $W_{24} \times 62$

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Q no 3

Given data:-

$$D.L = 50k$$

$$L.L = 150k$$

$$\text{Bolts Dia} = 3/4"$$

$$\text{Length} = 18ft$$

Connection type = Bearing

ASD method

Required

Design A36 Steel double angle
tension member

$$\begin{aligned} \text{Sol Total Load} &= D.L + L.L \\ &= 50 + 150 \\ &= 200 \text{ or } 100k/\text{Angle} \end{aligned}$$

→ For yielding at the gross area allowed
stress are

$$\begin{aligned} 0.6f_y &= 0.6f_y \times 36 \\ &= 21.6 \text{ ksi} \end{aligned}$$

→ For fracture at the net area allowed
stress are

$$\begin{aligned} 0.5\bar{f} &= 0.5 \times 58 \\ &= 29 \text{ ksi} \end{aligned}$$

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→ Since the connection is bolted so
 $A_g \neq A_n$

Now $A_e = 0.8 A_n$

For yielding

$$A_g \times 22 = 100$$

$$A_g = \frac{100}{22}$$

$$A_g = 4.54 \text{ in}^2$$

For fracture

$$29 \times A_e = 100$$

$$A_e = 3.44 \text{ in}^2$$

$$A_n = A_e / 0.85 \Rightarrow 3.44 / 0.85 \Rightarrow A_n = 4.04 \text{ in}^2$$

Assume 15% deduction in gross area
for holes

So

$$A_g = \frac{A_n}{0.85} \Rightarrow A_g = \frac{4.04}{0.85}$$

$$A_g = 4.76 \text{ in}^2$$

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$$\text{For } L4 \times 4 \times \frac{5}{8} \quad A_g = 4.61 \leq 4.76 \text{ OK}$$

$$K_n = 1.20 \quad Y_g = 1.20 \quad \text{with } \frac{3}{8} \text{ in Gusset Plate}$$

$$L_{\text{min}} = \frac{18 \times 12}{1.20} = 180 \leq 300 \text{ OK}$$

Bolts Design

Using A325 bolts with threads included in Area plan as dia $\frac{3}{4}$ "

$$\text{Area} = \frac{\pi (d)^2}{4} \Rightarrow \frac{\pi (0.75)^2}{4}$$

$$A = 0.441 \text{ in}^2$$

$$\text{Allowable Bolt Shear} \Rightarrow 21 \text{ ksi}$$

Since bolt are double shear so Allowable shear per bolt = $2 \times 21 \times 0.44 = 18.57 \text{ k}$ Allowable bolt bearing stress = $1.9 F_y = 1.9 \times 58 = 69.6 \text{ k}$

Allowable bearing on two $\frac{5}{8}$ " thick angle

$$\text{Less less} = 69.6 \times 2 \times \frac{5}{8} \times 0.75 = 65.25 > 18.5$$

So shear govern

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$$\text{No of bolts} = \frac{200}{18.5} = 10.81$$

Use 10 bolts

Design of gusset Plate

$$\text{Bearing stress} = 1.2 f_u$$

$$1.2 \times 58 = 69.6 \times 58$$

So

$$\text{Allowable bearing} = 69.6 \times 10 \times 0.75 \times = 200$$

$$t = 0.38 \text{ in}$$

$$\text{Use} = \frac{3}{4} \text{ B.P.}$$

Checking various limit states

$$\text{Yield} = 0.6 F_y A_g$$

$$= 0.6 F_y A_g$$

$$= 0.6 \times 36 \times (8 \times 0.75)$$

$$= 129.6 \text{ k} < 200 \text{ k} \text{ (Not ok)}$$

$$\text{Try } L_7 \times 4 \times \frac{1}{2} \quad A_g = 15.25$$

$$V_u = 2.25 \quad V_y = 1.11 \text{ with } \frac{3}{8} \text{ B.P.}$$

$$\frac{L}{r_{min}} = \frac{18 \times 12}{1.11} = 194.59 < 300 \text{ (ok)}$$

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Allowable bearing on two $\frac{1}{2}$ thick
Angles along legs

$$= 69.6 \times 2 \times \frac{1}{2} \times 0.75$$
$$52.2 > 18.5$$

So shear governs

Check various limit state

Yielding = $0.6 F_y A_g$

$$0.6 \times 36 \times (14 \times 0.75)$$

$$200.14$$

Fracture = $0.5 F_u A_e$

$$0.5 \times 58 \times \left[14 - \left(\frac{3}{4} \right) \times 2 \right] \times \frac{3}{4}$$

$$211.4 > 200.14 \text{ OK}$$

Check for bearing stress

$$L_e = \frac{2P}{F_u t}$$

$$1.25 = \frac{2P}{58 \times 0.5}$$

$$(1.25 \times (58 \times 0.5)) = 2P$$

$$P = 18.125 \text{ k}$$

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$$L = \frac{2P}{F_{ut}} + \frac{d_n}{2}$$

$$2 = \frac{2P}{58 \times 0.5} + \frac{3/4}{2}$$

$$2(58 \times 0.5) = 2P + 0.375$$

$$116.1 - 0.375 = 2P$$

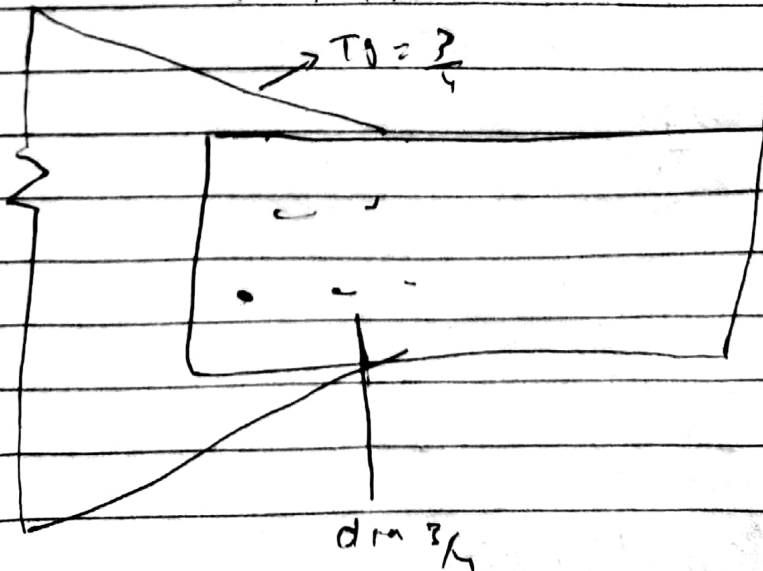
$$115.72 = 2P$$

$$P = 57.861 \text{ k}$$

Capacity since 10 bolts & 4 rows
bolts per row

$$2 \times (10 \times 115.72) + 4 \times 57.861$$

$$499.131 \text{ k} > 200 \text{ (ok)}$$



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