

NAME ABDUR. REHMAN

Section

A-

I.D

7892

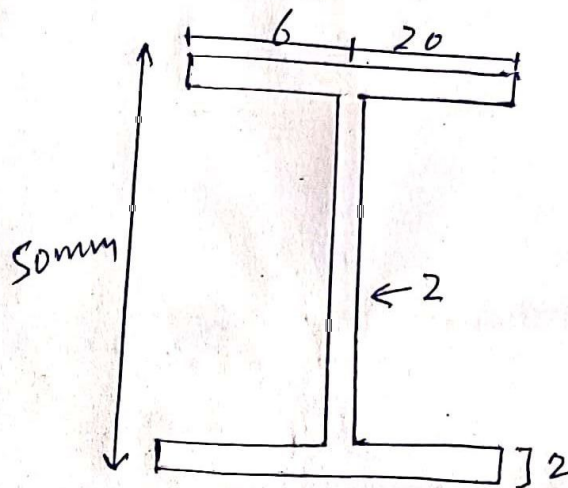
SUBJECT

MOR2

①

→ Question 1

PART 1



⇒ Location of Shear Center = ?

Solution:

As we know.

$$e = \frac{G_T h^2 b^2}{4I}$$

And

$$I = 2 \left(\frac{bh^3}{12} + Ay^2 \right) + \left(\frac{bh^3}{12} + Ay^2 \right)$$

$$= 2 \left(\frac{26(2)^3}{12} + (20 \times 2)(25)^2 \right) + \left(\frac{2(50)^3}{12} + 0 \right)$$

$$I = 50034.66 + 20833$$

$$I = 70867.98 \text{ mm}^4$$

$$e = \frac{2(50)^2(25)^2}{4(70867.98)} = \boxed{11.02 \text{ mm}} \text{ Ans.}$$

(2)

⇒ Question No 1

PART (B)

Data :-

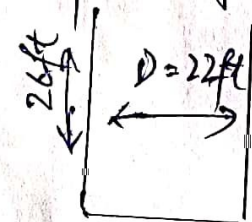
⇒ $H = 26$ ft, we assumed
ft $D = 22$ ft.

⇒ Specific weight of water tank.
 $= 62.4$ lb/ft³.

⇒ Tangential weight of water
tank $= 62.4$ lb/ft³.

⇒ thickness = ?

The pressure developed by water $= p = \gamma h$

$$\sigma_t = \frac{pD}{2t}$$


$$\Rightarrow \sigma_t = \frac{pD}{2t} \Rightarrow \frac{\gamma h D}{2t}$$

$$2t \times \sigma_t = \gamma h D$$

$$2t = \frac{\gamma h D}{\sigma_t}$$

(3)

$$\Rightarrow t = \frac{yhd}{b_t \times 2}$$

$$\Rightarrow t = \frac{(62.4) \times (26 \times 12) \times (22 \times 12)}{(12)^3}$$

$$6000 \times 2$$

$$\Rightarrow t = 0.24''$$

⇒ QNO 2.

(4)

PART (A) :-

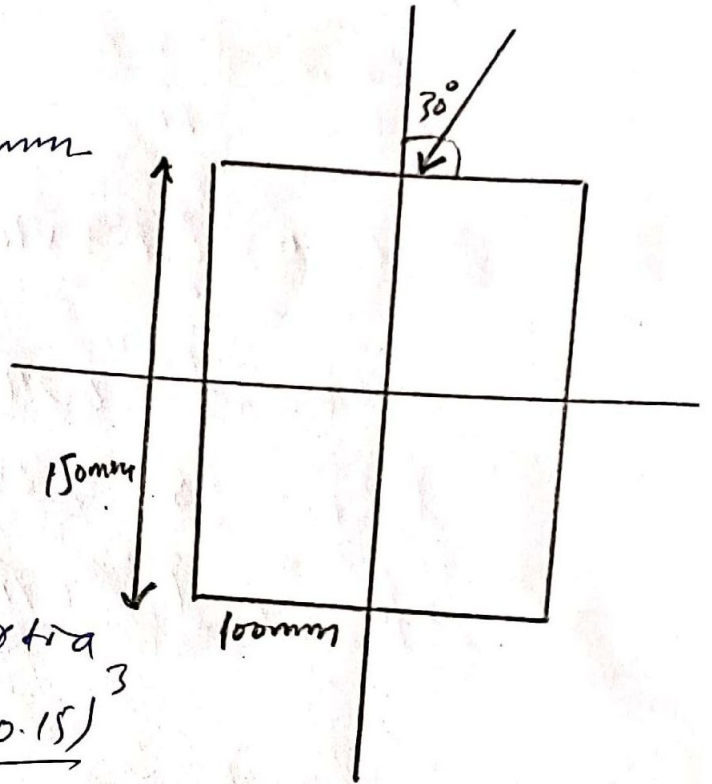
Given Data :-

⇒ Wooden Beam = 150 x 100 mm

⇒ Load = 4K.

⇒ Span = 3m

⇒ Maximum Bending Stress = ?



⇒ Moment of Inertia

$$I_z = \frac{bh^3}{12} \Rightarrow \frac{0.1(0.15)^3}{12}$$

$$I_z = 2.8125 \times 10^{-5}$$

Now $I_y = \frac{bh^3}{12} \Rightarrow \frac{(0.15)(0.1)^3}{12}$

$$I_y = 1.25 \times 10^{-5}$$

$$\sigma = \frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

$$\sigma = \frac{M \cos \theta}{I_z} + \frac{M \sin \theta}{I_y}$$

where $M = P \cos \theta \Rightarrow P \cos \theta = M_z$
 $= 12 \cos 30^\circ$

$$M_z = 1.8510$$

$$M \sin \theta = P \sin \theta = My \quad (5)$$

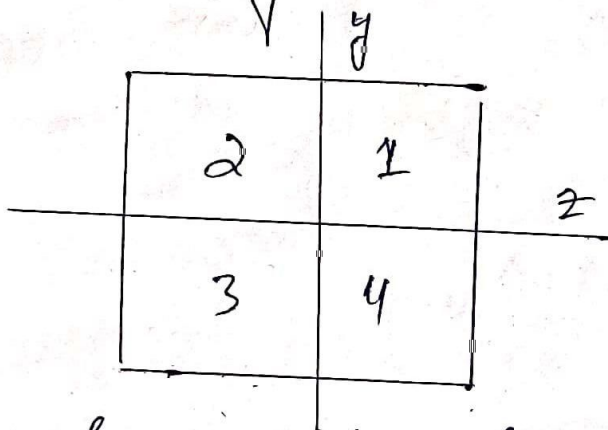
$$\Rightarrow 12 \sin 30^\circ$$

$$My = -11.856$$

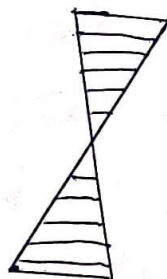
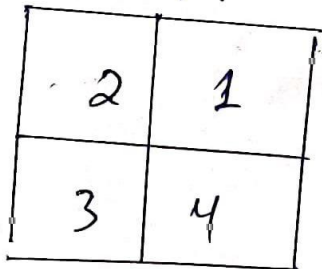
$$C = \left(\frac{Mz}{Iz} \right) + \left(\frac{My}{Iy} \right) \Rightarrow \frac{1.851}{2.812 \times 10^{-5}} + \left(\frac{-11.856}{1.25 \times 10^{-5}} \right)$$

$$C = 882678 \text{ N/m}^2$$

Sign Convention



* If we take compression as negative and tension as positive and the beam is simply supported.



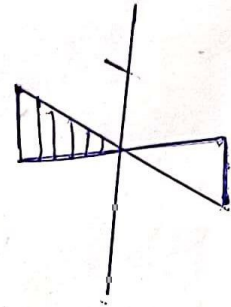
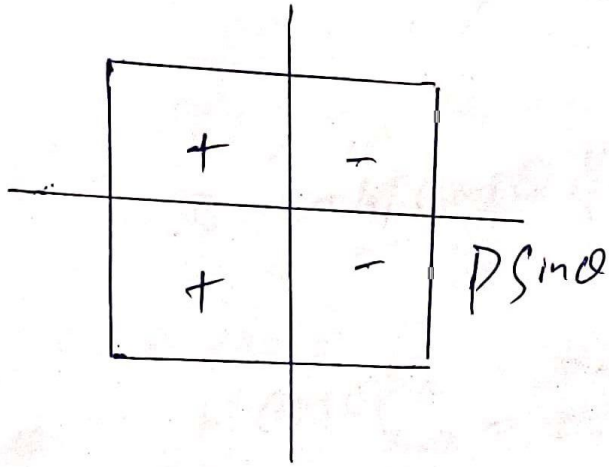
N.A

Quadrant

1-2 -ive

3-4 +ive

(6)



Quadrant

1.4 -ive

2.3 +ive

In case of unsymmetrical loading, the neutral axis lies at an angle of "X". The principle axis and the algebraic sum of stress at N-A is zero.

$$\sigma = \left(\frac{M \cos \theta}{I_z} + y \right) + \left(\frac{M \sin \theta}{I_y} - z \right) \rightarrow 0$$

In this case N-A passes through 2, 4 quadrants.

$$\sigma = \frac{M \cos \theta}{I_z} \cdot y + \frac{M \sin \theta}{I_y} \cdot z$$

Let consider a point "A" on N-A lies in Quadrant 2, where

- Bending stress due to $M \cos \theta$ is compressive
- Bending stress due to $M \sin \theta$ is tensile

(7)

eq ①

$$0 = \frac{-M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\frac{M \cos \theta y_A}{I_z} = \frac{M \sin \theta z_A}{I_y}$$

$$\frac{y_A}{z_A} = \frac{I_z \sin \theta}{I_y \cos \theta}$$

$$\tan \alpha = \frac{I_z}{I_y} \tan \theta \quad \text{--- (2)}$$

Now put values of I_z , I_y and θ
in eq (2)

$$\tan \alpha = \frac{I_z}{I_y} \tan 30^\circ$$

$$\Rightarrow \frac{2.8125 \times 10^{-5}}{1.25 \times 10^{-5}} \tan 30^\circ$$

$$\tan \alpha = -14.4129$$

$$\alpha = \tan^{-1} (-14.4129)$$

$$\alpha = 1.5^\circ$$

$$\alpha = 1^\circ 30' 5''$$

⇒ Question No 2 (8)

PART B

Given Data:-

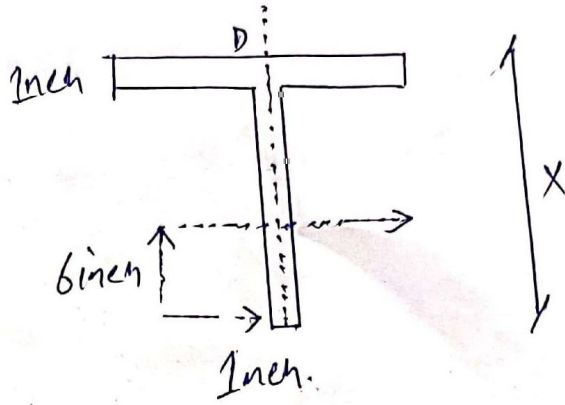
$$Length = L = 16 \text{ ft}$$

$$I_x = 112.6 \text{ inch}^4$$

$$I_y = 18.7 \text{ inch}^4$$

$$\sigma_c = 12000 \text{ psi}$$

$$\sigma_t = 5000 \text{ psi}$$



⇒ Solution:-

By looking at figure we can judge that maximum compression would occur on a axis maximum tension at B. There will be tension as well as compression which will be reduced the effect of each other so we will calculate stress at A and

$$\sigma_A = \frac{Mx}{I_x} + \frac{My}{I_y} \quad (\text{compression})$$

$$\sigma_C = \frac{Mx}{I_x} + \frac{My}{I_y} \quad (\text{Tension})$$

(9)

$$M_x = ?$$

$$\Rightarrow M_x = \frac{P \cos 60 \times (16 \times 12)}{4}$$

$$M_x = 48 P \cos 60$$

$$\Rightarrow M_y = \frac{P \sin 60 (16 \times 12)}{4}$$

$$M_y = 48 P \sin 60$$

Now

$$\delta_A = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$\Rightarrow 1200 = \frac{48 P \cos 60^\circ \times 3.07}{112.6} + \frac{48 P \sin 60 \times 3}{18.7}$$

After solving it.

$$P = 1638.6 \text{ lb}$$

Now

$$\delta_C = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$5000 = \frac{48 P \cos 60 \times (593)}{112.6} + \frac{48 P \sin 60 \times 0.5}{(18.7)}$$

After solving it.

$$P = 2104.9 \text{ lb}$$

So the maximum load "P" Applied should be 1638.6 lb.

→ Question No 3 (10)

Given Data:-

⇒ Length "L" = 10 ft

Both Sides are hinged

$$L_e = L$$

⇒ $E = 10.3 \times 10^6$

⇒ factor of Safety = 2.

⇒ $b = 0.75$ inch

⇒ $h = 2$ inch

⇒ Safe load = ? At hinged
And fixed = ?

→ Solution:

① for hinged columns
 $L_e = L$

$$I = I_x = \frac{(0.75)(2)^3}{12} = 0.5 \text{ inch}^4.$$

$$P_{cr} = \frac{\pi^2 EI \pi^2}{L_e^2} = (1)^2 \frac{(10.3 \times 10^6)(0.5) \pi^2}{(10 \times 12)^2}$$

$$P_{cr} = \frac{50776990}{14400} = 3526.176 \text{ lb}$$

$$\text{Safe load} = \frac{P_{cr}}{\text{factor of Safety}} = \frac{3526.176}{2}$$

$$= 1763.088 \text{ lb Ans.}$$

(B) for fixed ended (11)

$$L_e = \frac{L}{2} \Rightarrow \frac{10}{2} = 5 \text{ ft.}$$

$$I = I_y = \frac{2 \times (0.75)^3}{12} = 0.07 \text{ in}^4$$

$$P_{cr} = \frac{\pi^2 EI \pi^2}{L_e^3} = \frac{(1)^2 (10.3 \times 10^6) (0.07) (3.14)^2}{(5 \times 12)^2}$$

$$P_{cr} = \frac{7108771.6}{(60)^2}$$

$$P_{cr} = 1974.658 \text{ lb}$$

$$\text{Safe load} = \frac{1974.658}{2} = 987.3293 \text{ lb.}$$