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Subject : Linear ^{circuit} ~~Control~~ Analysis

Program : BE (Electrical)

Exam : Summer (2020) Final

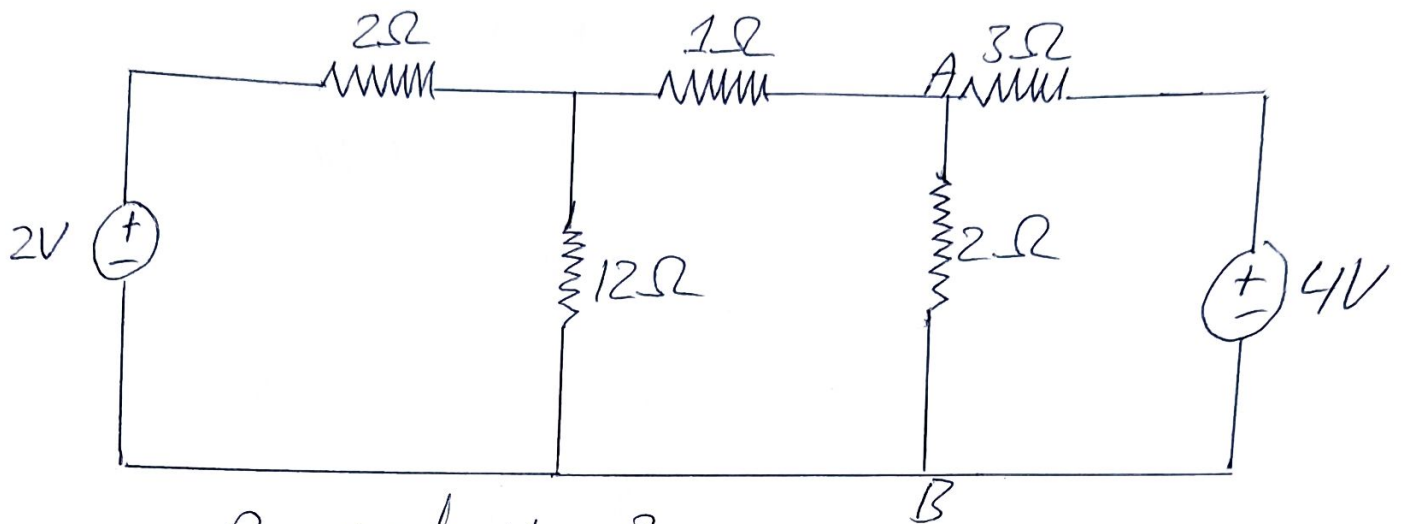
Date : 24/09/2020

Submitted to : Engr. WALEED JAN

Q#1

①

Using superposition principle determine the current through 2Ω resistor connected between terminal A & B in given circuit

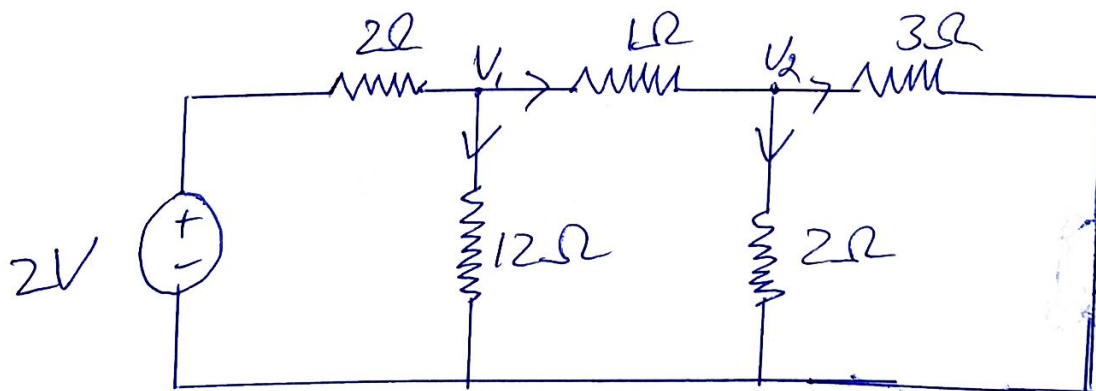


Required $V_{AB} = ?$

Sol:

Using superposition principle:

Suppose we use 2V Volt source & short the 4V source



For find V_{AB} using Nodal Analysis.

V_1 :

②

$$\frac{V-2}{2} + \frac{V_1}{2} + \frac{V_1-V_2}{1} = 0$$

$$6V_1 - 12 + V_1 + 12V_1 - 12V_2 = 0$$

$$19V_1 + 12V_2 = 12 \text{ ———— } \textcircled{1}$$

V_2 :

$$\frac{V_2-V_1}{1} + \frac{V_2}{2} + \frac{V_2}{3} = 0$$

$$6V_2 - 6V_1 + 3V_2 + 2V_2 = 0$$

$$-6V_1 + 11V_2 = 0$$

$$V_2 = \frac{6V_1}{11} \text{ ———— } \textcircled{2}$$

put in eq(1)

$$19V_1 - 12\left(\frac{6V_1}{11}\right) = 12$$

$$19V_1 - \frac{72V_1}{11} = 12$$

$$19V_1 - 6.5V_1 = 12$$

$$12.45V_1 = 12$$

$$V_1 = \frac{12}{12.45}$$

$$\boxed{V_1 = 0.963 \text{ V}}$$

(2)b

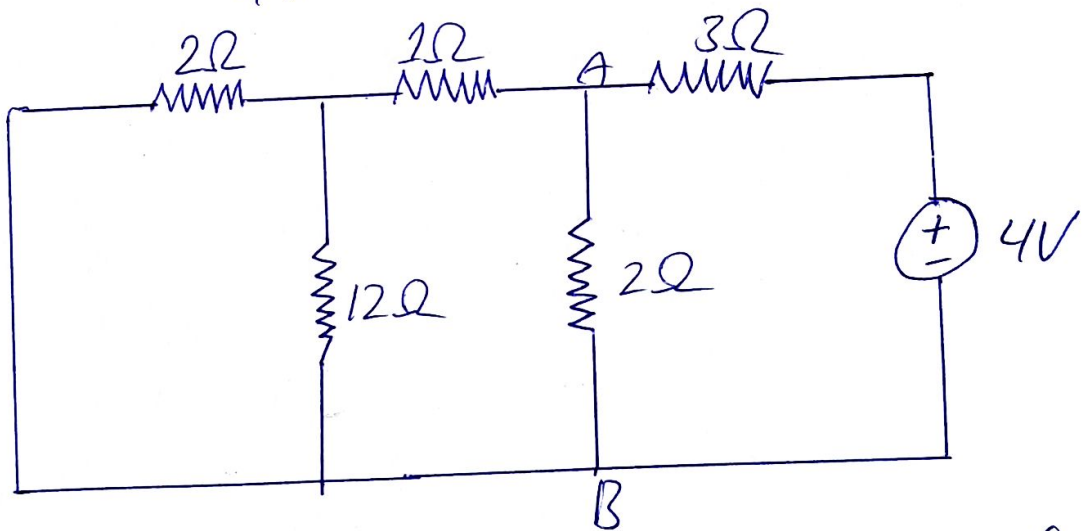
$$V_2 = \frac{6V_1}{11}$$
$$= \frac{6(0.963)}{11}$$

$$V_2 = 0.525V$$

$$V_{AB}' = V_2 - 0$$

$$V_{AB}' = 0.525V$$

Now 2V source is to be short &
4V is to be use source.



after parallel & series simplification

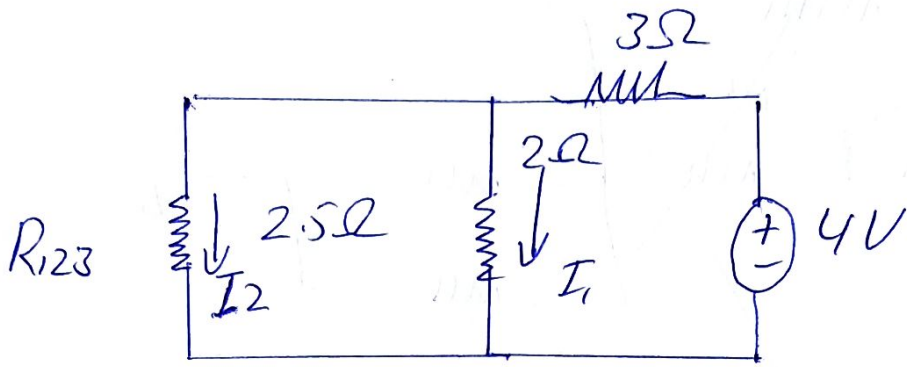
$$R_{12} = 2 // 12$$

$$R_{123} = 2 // 12 + 1$$

(3)

$$R_{123} = 1.5 + 1$$

$$R_{123} = 2.5 \Omega$$



$$V_{AB}'' = \frac{I_1(2)}{4} = \frac{2.5 // 2 + 3}{4} A$$

Using current division Rule.

$$I_1 = \left(\frac{2.5}{2+2.5} \right) I$$

$$I_1 = 0.5405 A$$

$$V_{AB}'' = I_1(2) = (0.5405)(2)$$

$$V_{AB} = 1.081 V$$

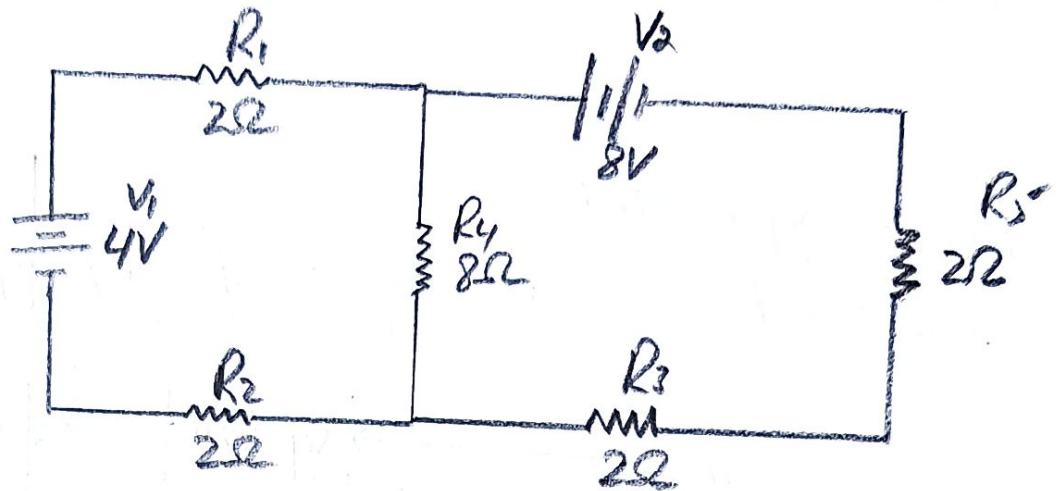
So Net Voltage

$$V_{AB} = V_{AB}' + V_{AB}'' \Rightarrow (0.5225 + 1.081) V$$

$$V_{AB} = 1.6035$$

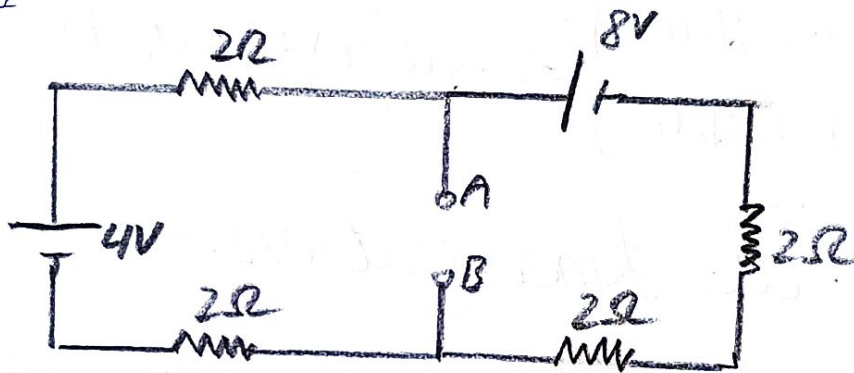
①

Q#02

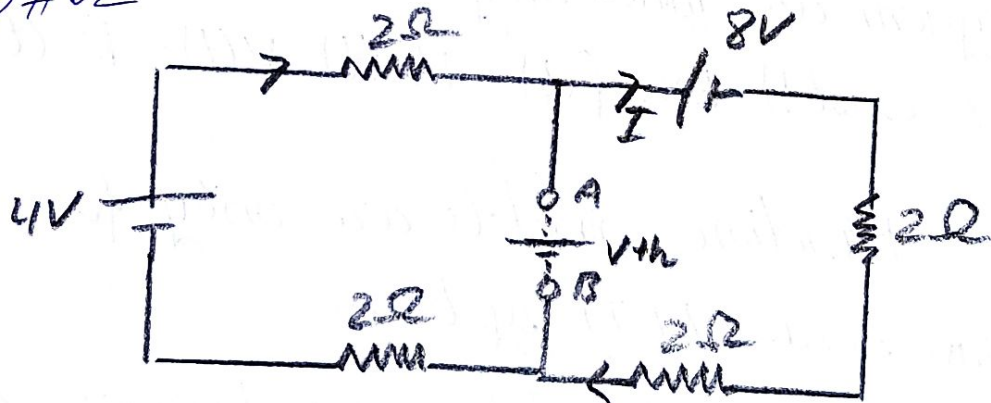


Sol:-

Step#01



Step#02



$$4 - 2I - 8 - 2I - 2I - 2I = 0$$

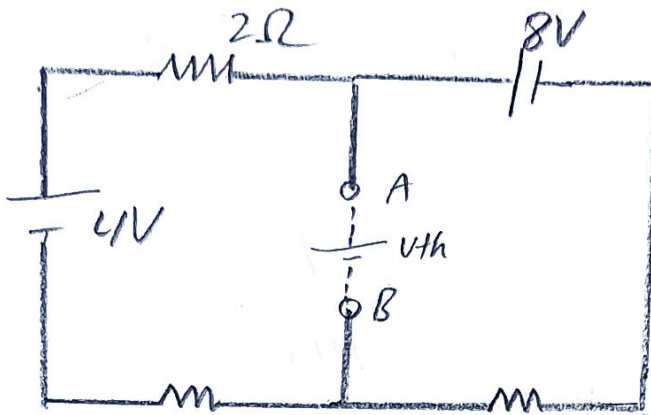
$$-8I - 4 = 0$$

$$I = \frac{-4}{8}$$

$$I = -\frac{1}{2}$$

(5)

Step#03

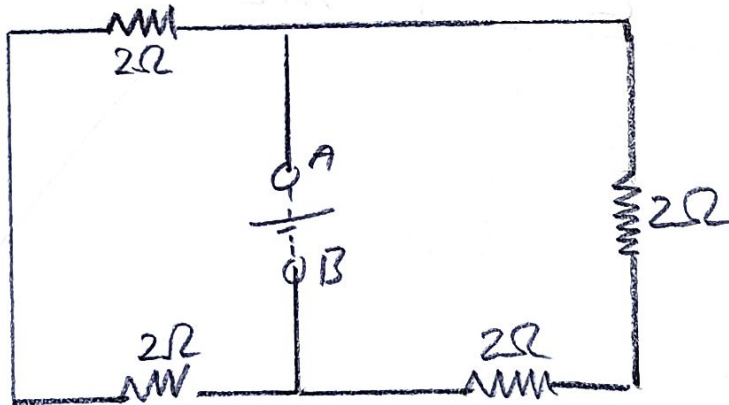


$$4 - 2I - V_{th} - 2I = 0$$

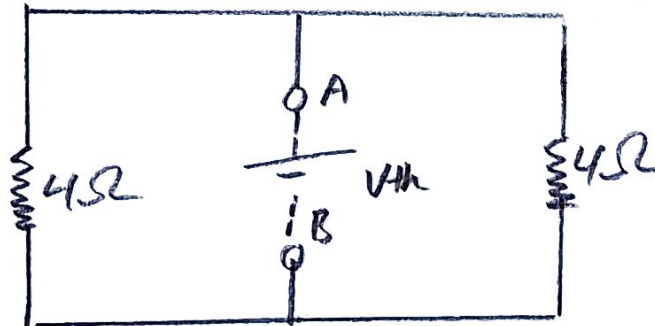
$$V_{th} = -4I + 4$$

$$V_{th} = 6V$$

Step#04



⇓

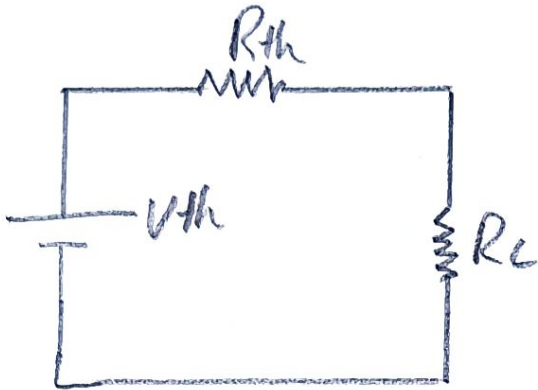


$$R_{th} = \frac{4 \times 4}{4 + 4} = \frac{16}{8} = 2\Omega$$

(6)

$$R_{th} = 2\Omega$$

Step # 02



$$I = \frac{V_{th}}{R_{th} + R_L}$$

$$= \frac{6}{2+8}$$

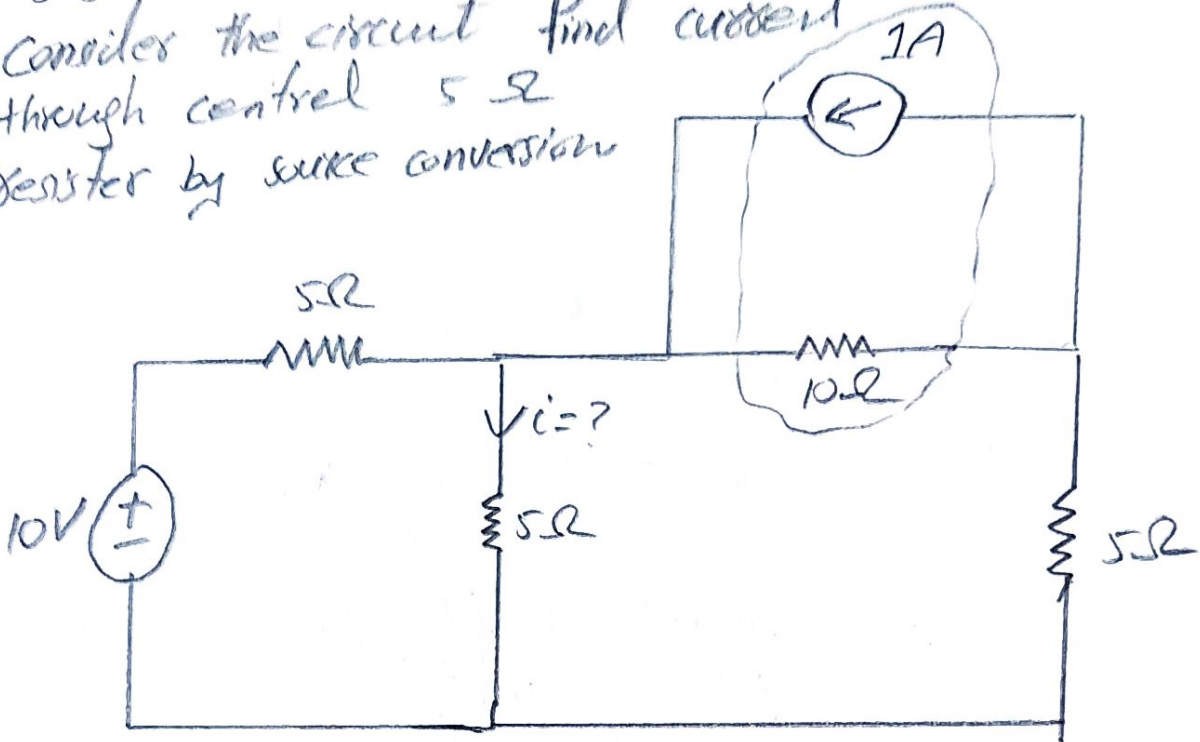
$$= \frac{6}{10}$$

$$I = 0.6A$$

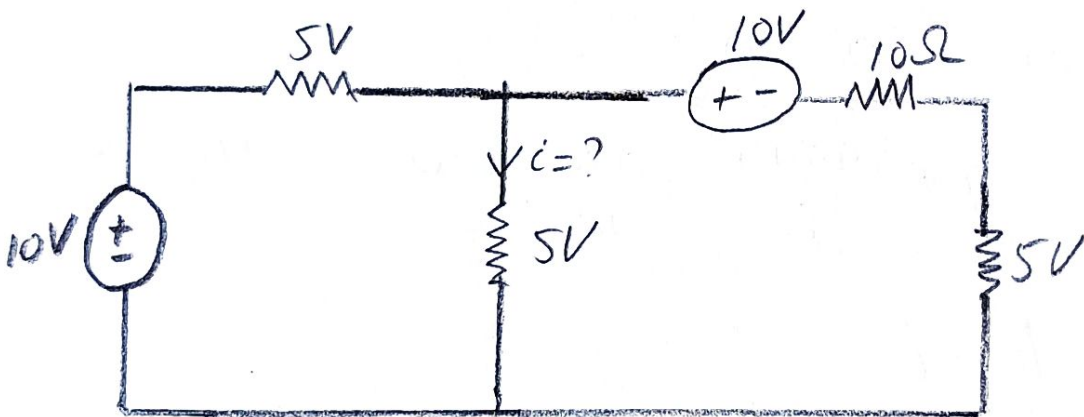
(7)

Q#03

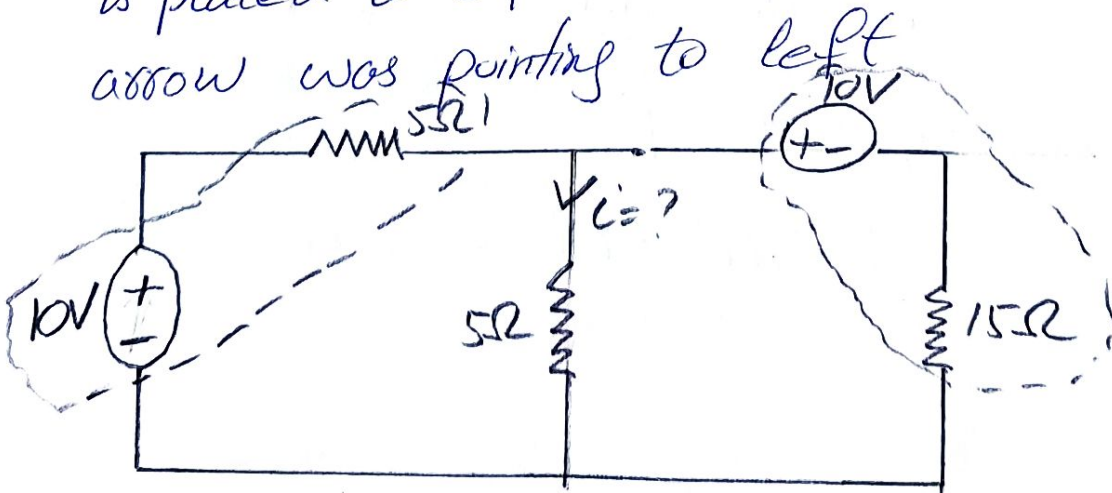
consider the circuit find current through central 5Ω resistor by source conversion



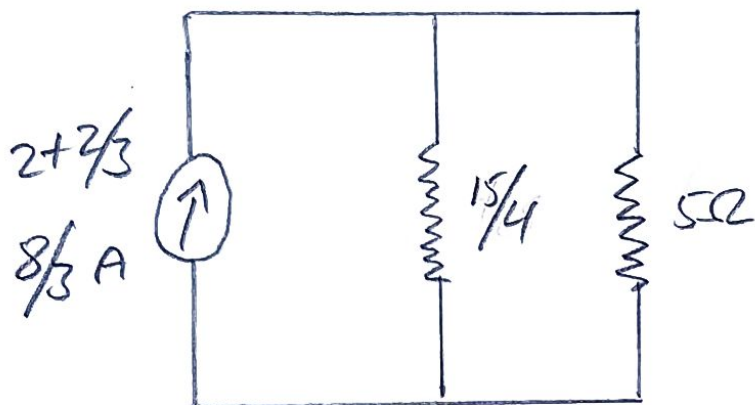
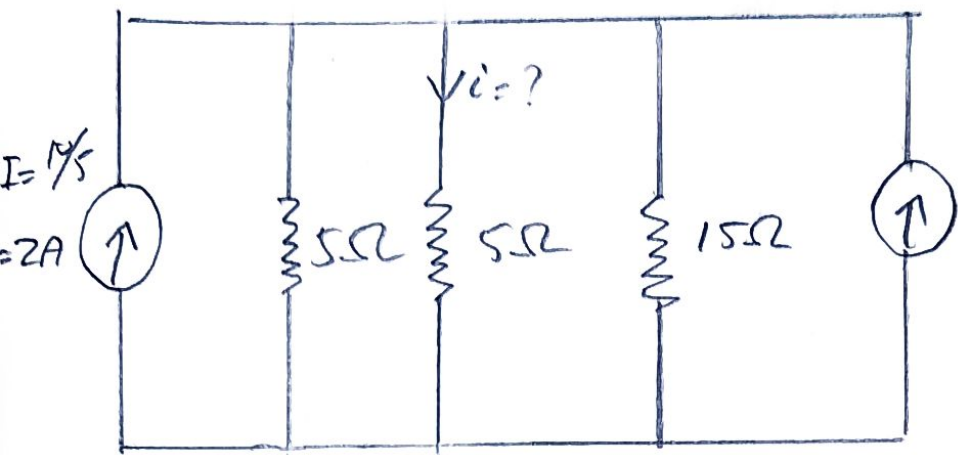
Sol:-



Note that the positive terminal of 10V source is placed to left because the current source arrow was pointing to left



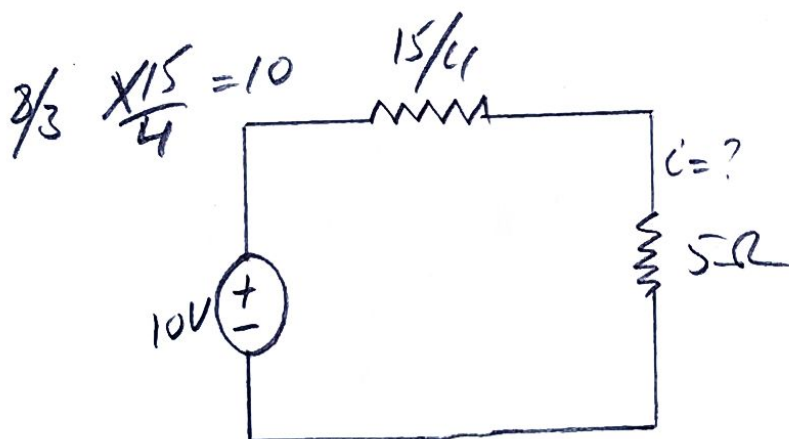
78



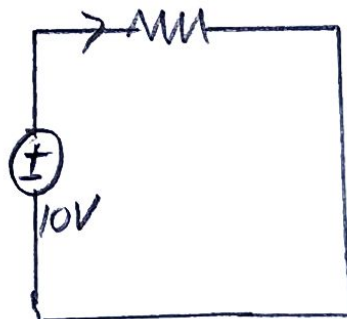
$$\therefore \frac{1}{R_{eq}} = \frac{1}{15} + \frac{1}{5}$$

$$= \frac{2+3}{15}$$

$$R_{eq} = \frac{15}{4} \text{ OR } R_{eq} = \frac{4}{15}$$



$$35/4 \Omega \rightarrow \frac{15}{4} + 5 = \frac{15+20}{4}$$

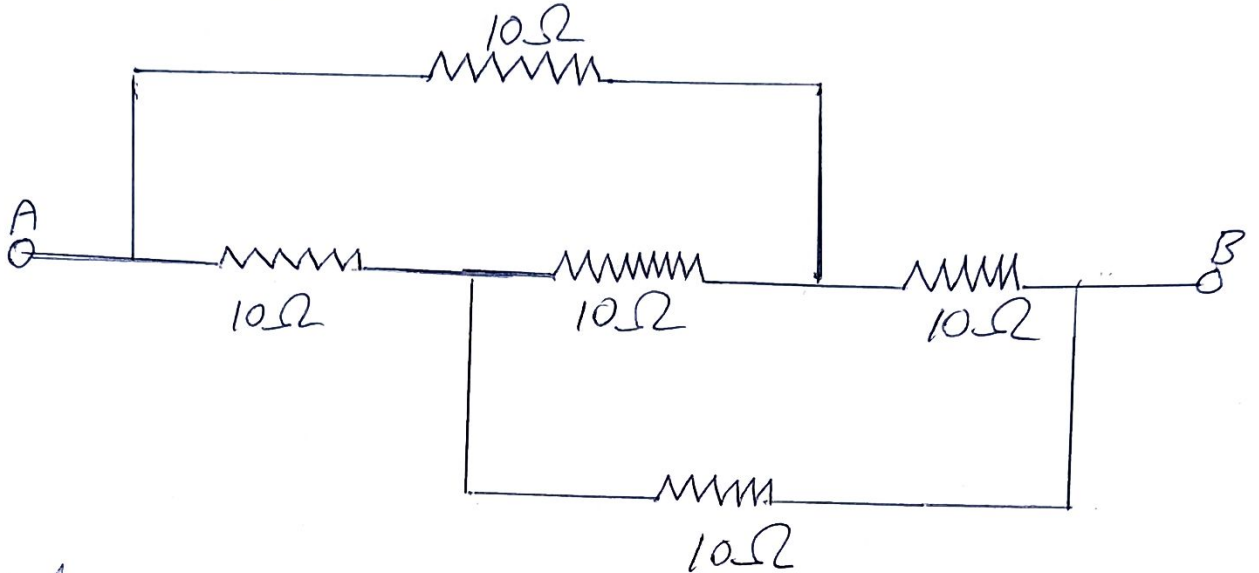


$$i = \frac{10}{35/4} = \frac{10 \times 4}{35} = \frac{8}{7} A$$

6

Q#4

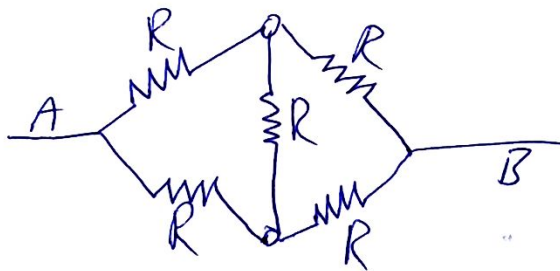
a) Calculate the resistance between terminal A & B for the circuit shown below:



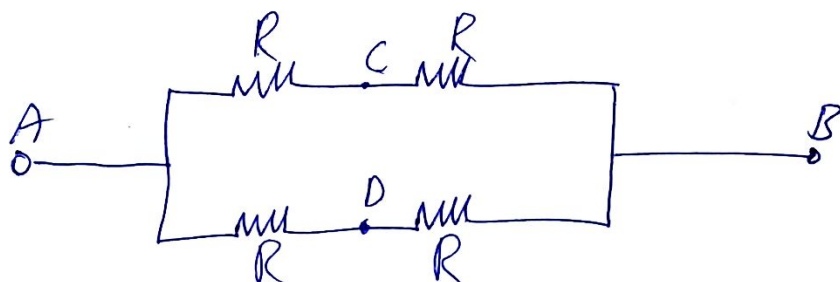
Soln-

$$A = VA$$

$$B = VB$$



all resistance has some value



(10)

$$R_{eq} = \frac{2R \times 2R}{2R + 2R}$$

$$= \frac{2(10) \times (10)2}{2(10) + 2(10)}$$

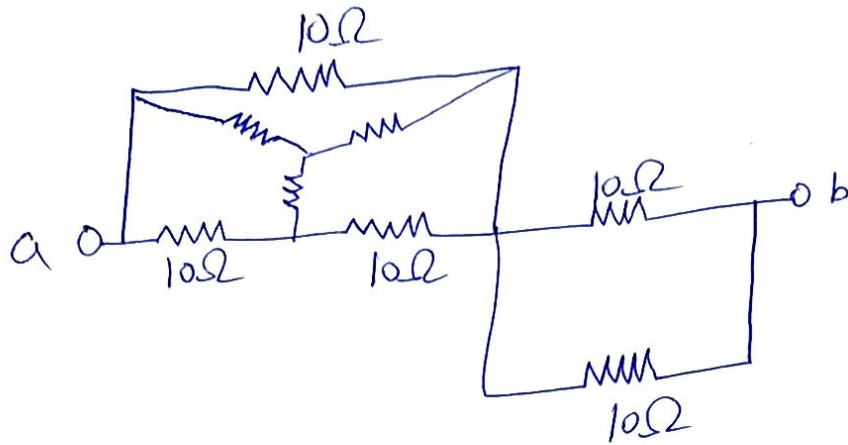
$$= \frac{20 \times 20}{20 + 20}$$

$$= \frac{400}{40}$$

$$R_{eq} = 10 \Omega$$

$$R_{eq} = R$$

2nd Method (11)



$R_{ab} = ?$ $\Delta \rightarrow Y$

$$R_1 = \frac{10 \times 10}{10 + 10 + 10}$$

$$R_1 = \frac{100}{30}$$

$$R_1 = 3.333 \Omega$$

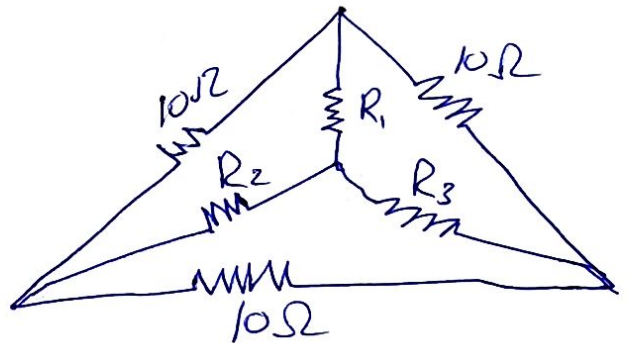
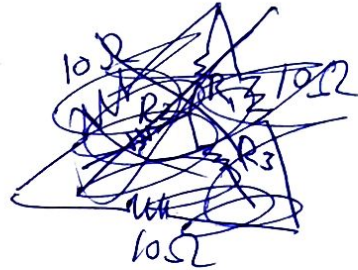
$$R_2 = \frac{10 \times 10}{10 + 10 + 10}$$

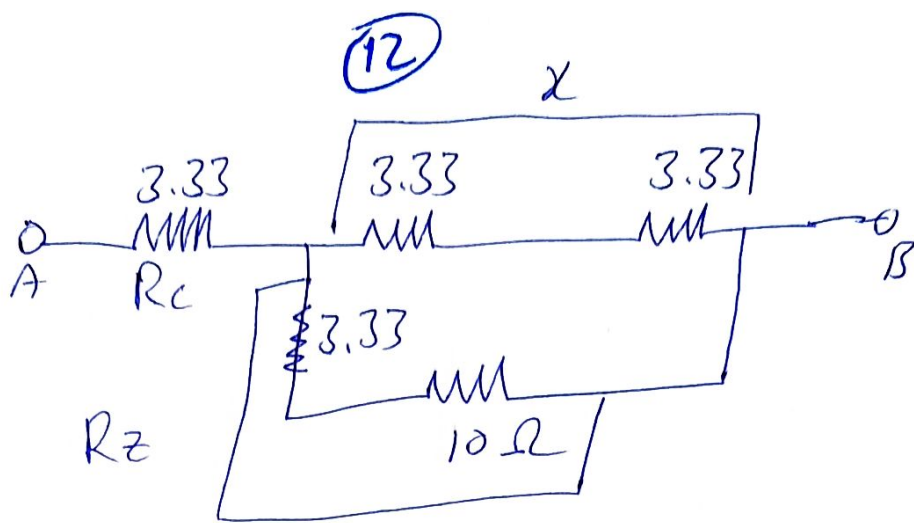
$$R_2 = \frac{100}{30}$$

$$R_2 = 3.33 \Omega$$

Similarly

$$R_3 = 3.33 \Omega$$



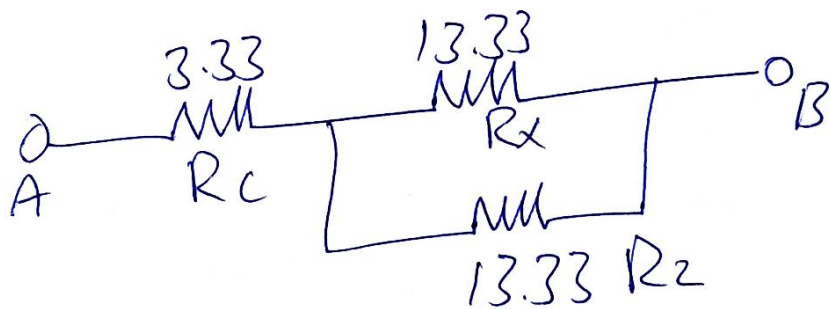


$$R_x = 10 + 3.33$$

$$R_x = 13.33 \Omega$$

$$R_z = 10 + 3.33$$

$$R_z = 13.33$$



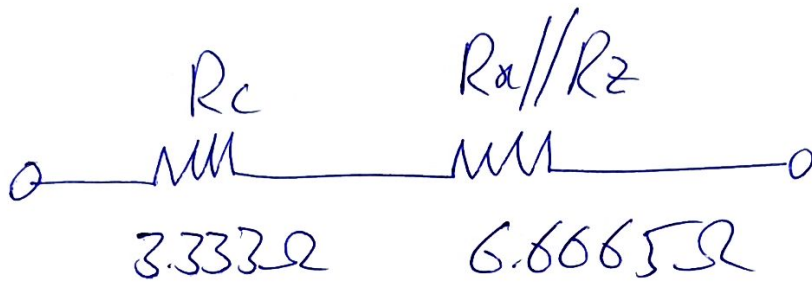
$$R_x // R_z = \frac{R_x \times R_z}{R_x + R_z}$$

$$= \frac{13.33 \times 13.33}{13.33 + 13.33}$$

(13)

$$R_x // R_z = \frac{177.768}{26.66}$$

$$R_x // R_z = 6.665 \Omega$$



$$R_{ab} = R_c + R_x // R_z$$

$$R_{ab} = 3.33 + 6.6665$$

$$R_{ab} = 9.99$$

$$R_{ab} \approx R$$

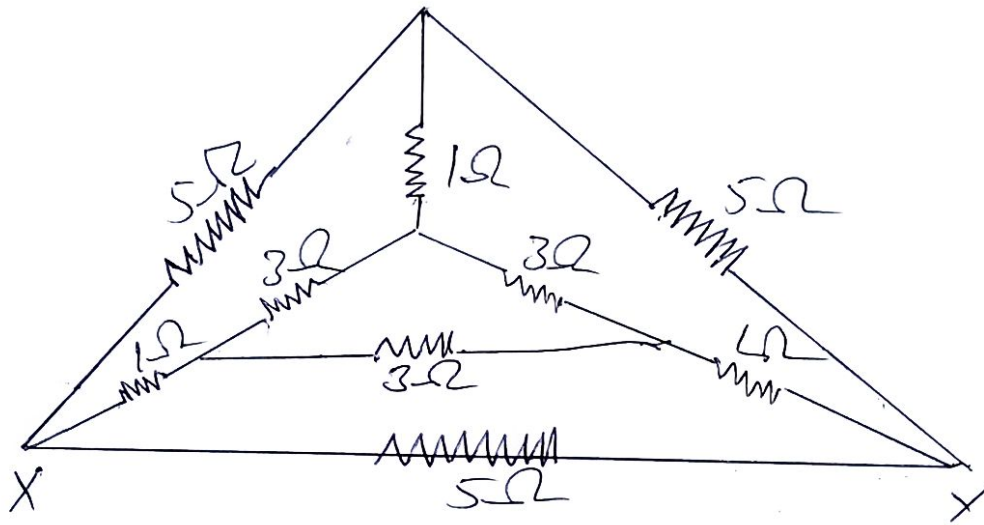
$$R_{eq} = R$$

$$\therefore 9.99 \approx 10$$

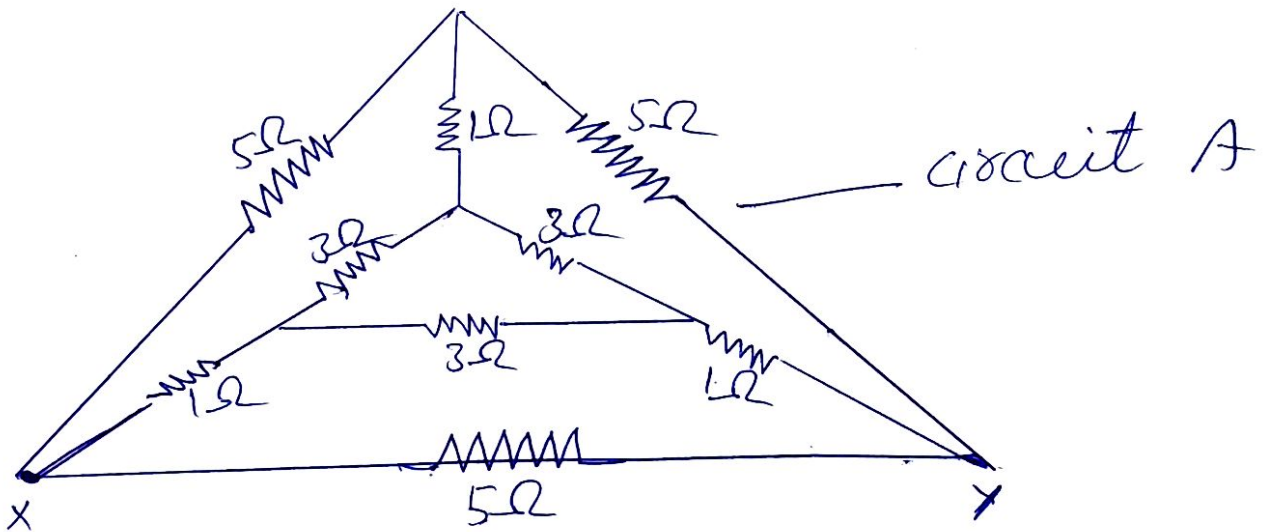
Q# 4(b)

(14)

Determine the resistance between terminal X & Y for the circuit shown in figure



Sol:-



(15)

$$R_1 = \frac{3 \times 3}{3+3+3} = \frac{9}{9} = 1$$

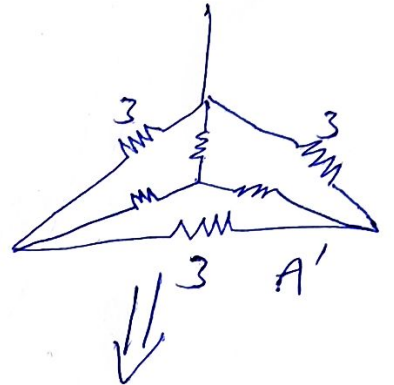
$$R_1 = 1 \Omega$$

$$R_2 = \frac{3 \times 3}{3+3+3} = \frac{9}{9} = 1$$

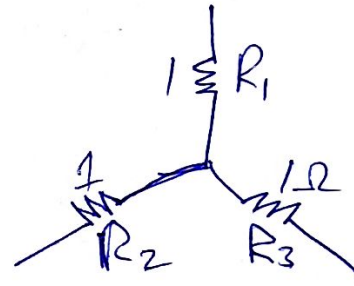
$$R_2 = 1 \Omega$$

$$R_3 = \frac{3 \times 3}{3+3+3} = \frac{9}{9} = 1$$

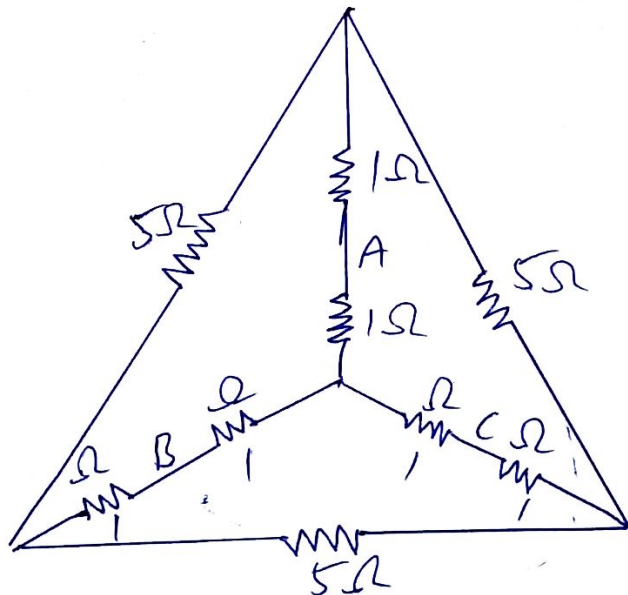
$$R_3 = 1 \Omega$$



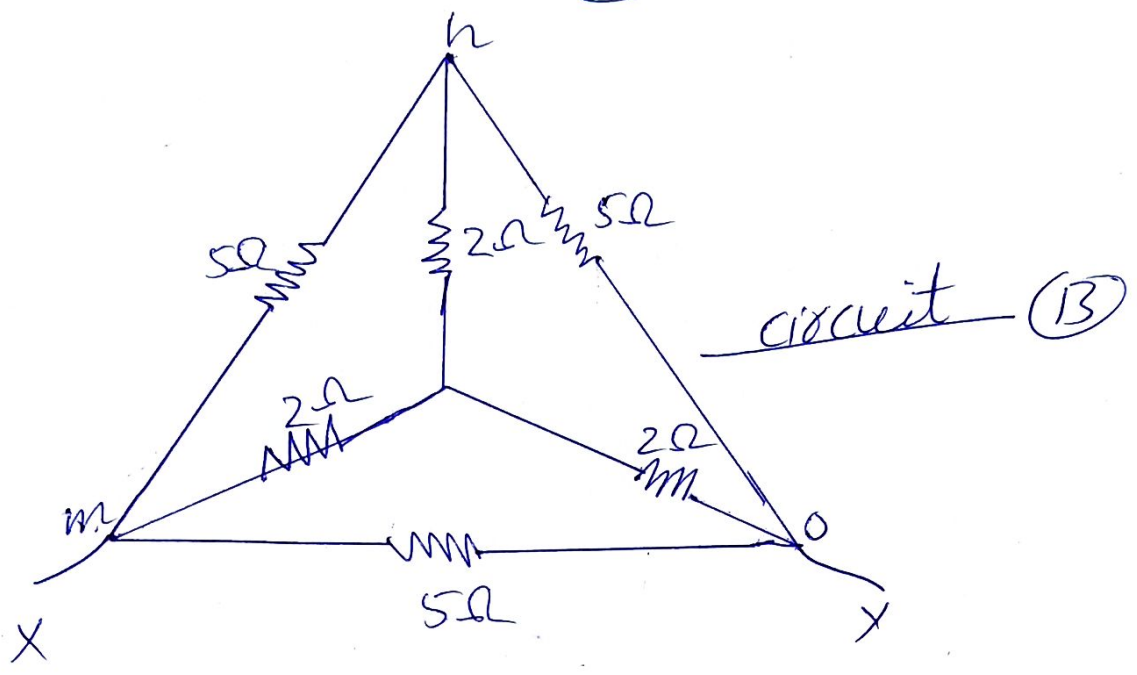
Δ to Y



*Put in circuit
A



(16)



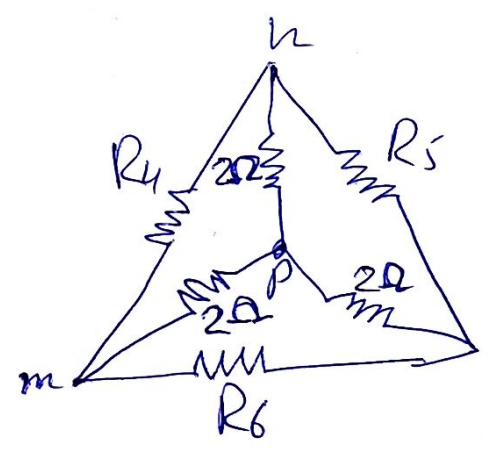
$$R_4 = 2 + 2 + \frac{2 \times 2}{2}$$

$$R_4 = 6\Omega$$

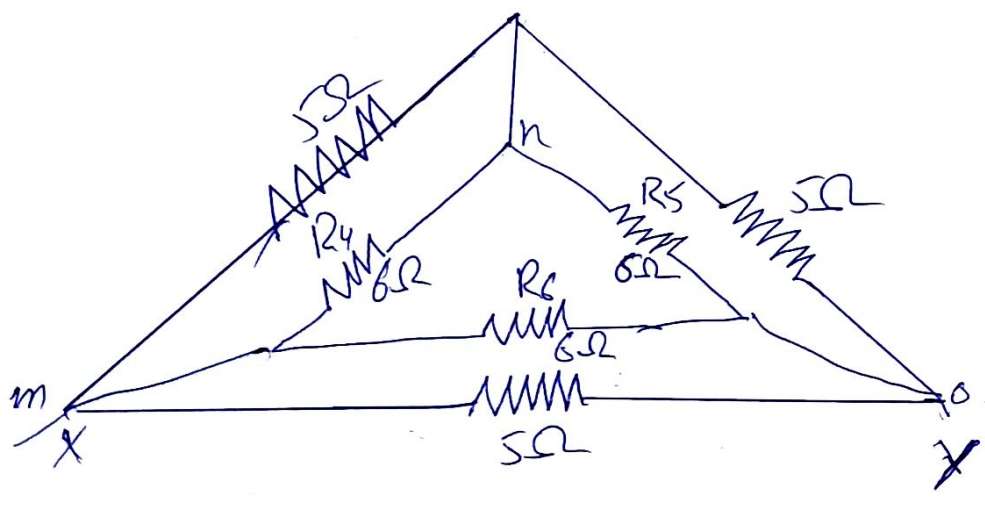
$$R_5 = 4 + 2$$

$$R_5 = 6\Omega$$

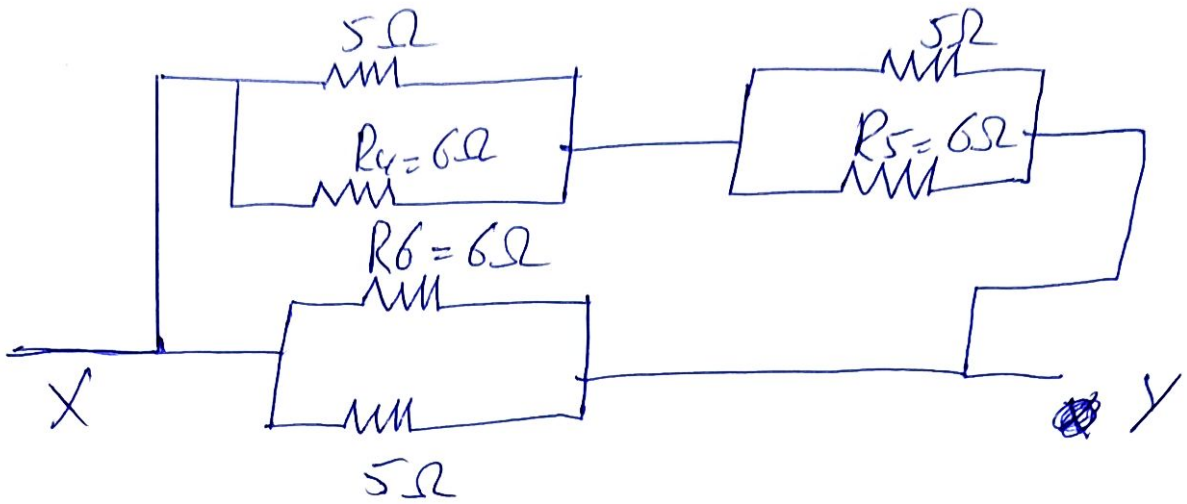
$$R_6 = 6\Omega$$



Put it circuit B



(17)

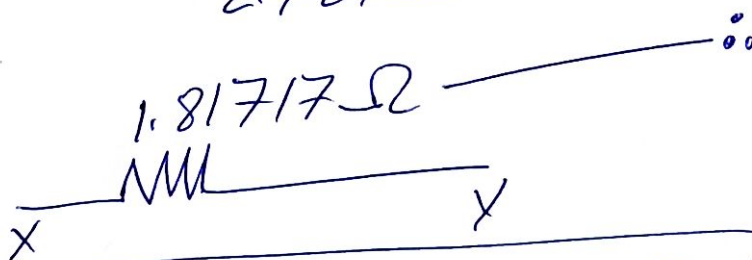
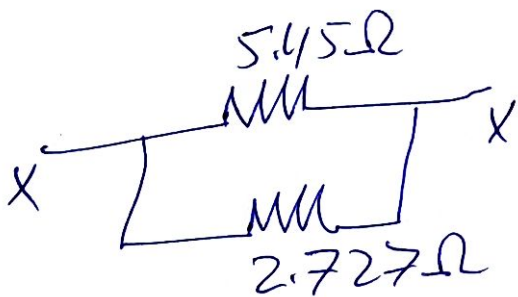
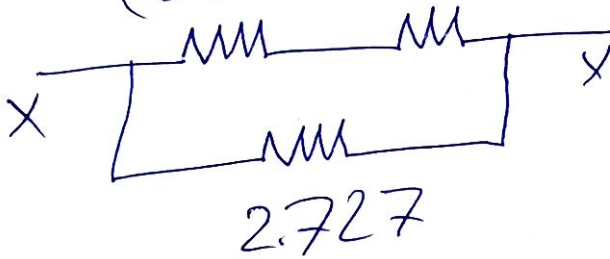


So

$$R_{eq} = 5 \parallel R_6 = 5 \parallel 6 = \frac{5 \times 6}{5 + 6} = \frac{30}{11}$$

$$R_{eq} = 2.727 \Omega$$

$$(2.727 + 2.727) \Omega$$



$$\frac{5.45 \times 2.725}{5.52 + 2.725} = 1.81717$$

$$Z_{eq} = Z_{xy} = 1.81717 \Omega$$