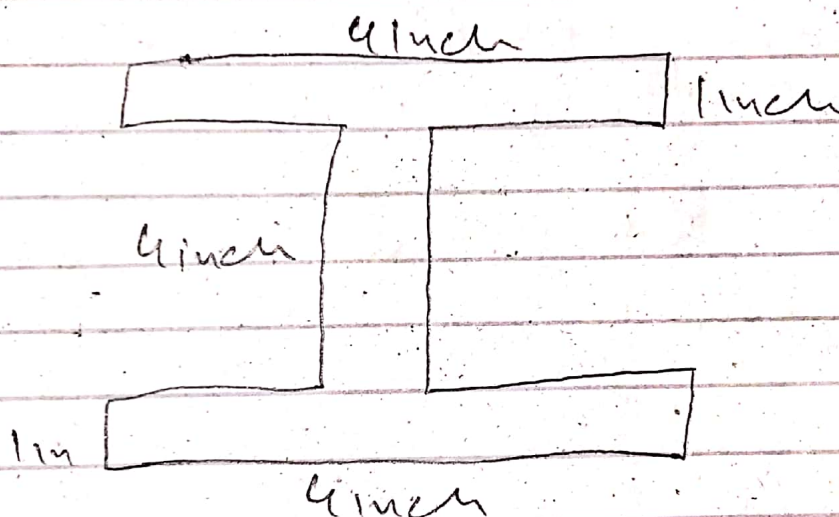
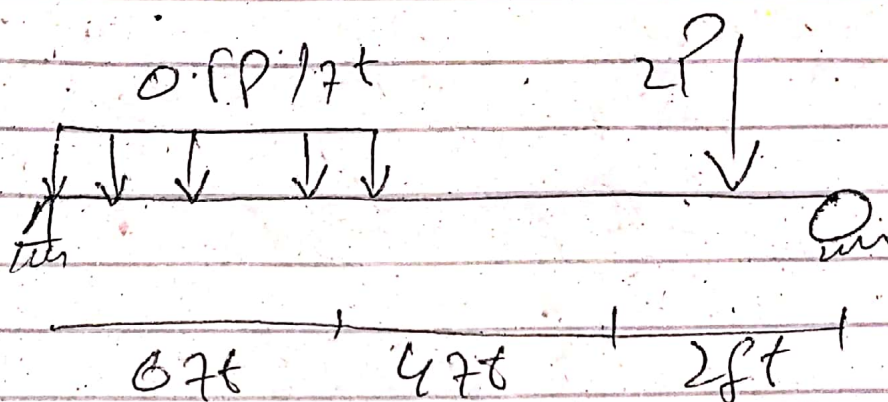


Q

# MOS II



$$\sum F_y = 0 \uparrow + \text{upward is } +$$

$$R_A + R_B - 32 \times 6 - 12.8 = 320$$

$$\sum M_A = 0 \curvearrowright 12.8(10) - 32(6) \times 3 = 0$$

$$R_B \cdot 12 = 1876$$

$$R_B = \frac{1876}{12}$$



(2)

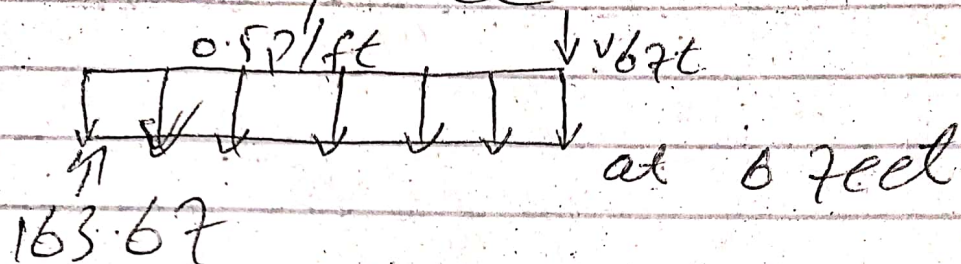
$$R_B = 156.33 \text{ lb}$$

Now

$$R_A = 320 - 156.33$$

$$R_A = 163.67$$

Shear Force



$$\sum F_y = 0 \uparrow \text{ at } 6 \text{ ft from left support}$$

$$-V_{6ft} + 163.67 - 32 \times 6$$

$$V_{6ft} = -28.33$$

$$\sum F_y = 0 \text{ at } 10 \text{ ft from left support}$$



(3)

$$163.67 - 32 \times 6 - 128 - V_{10.7t} = 0$$

$$-116.33 - V_{10.7t} = 0$$

$$-V_{10.7t} = 116.33$$

$$V_{10.7t} = -116.33$$

Bending Moment

$$\sum M_{6.7t} = 0$$

$$\sum M_{6.7t} = -163.67(6) + 32(6)(4.5)$$

$$\sum M_{6.7t} = 598.02$$

at 3.7t

$$\sum M_{3.7t} = 0$$

$$\begin{aligned} \sum M_{3.7t} &= -16 + 163.67(3) + 32(6)(3) \\ &= 84.88 \text{ lb ft} \end{aligned}$$



(4)

Now we find moment  
at change point

$$\frac{163.67}{x} = \frac{28.33}{(6-x)}$$

$$163.67(6-x) = 28.33(x)$$

$$x = 5.11 \text{ ft}$$

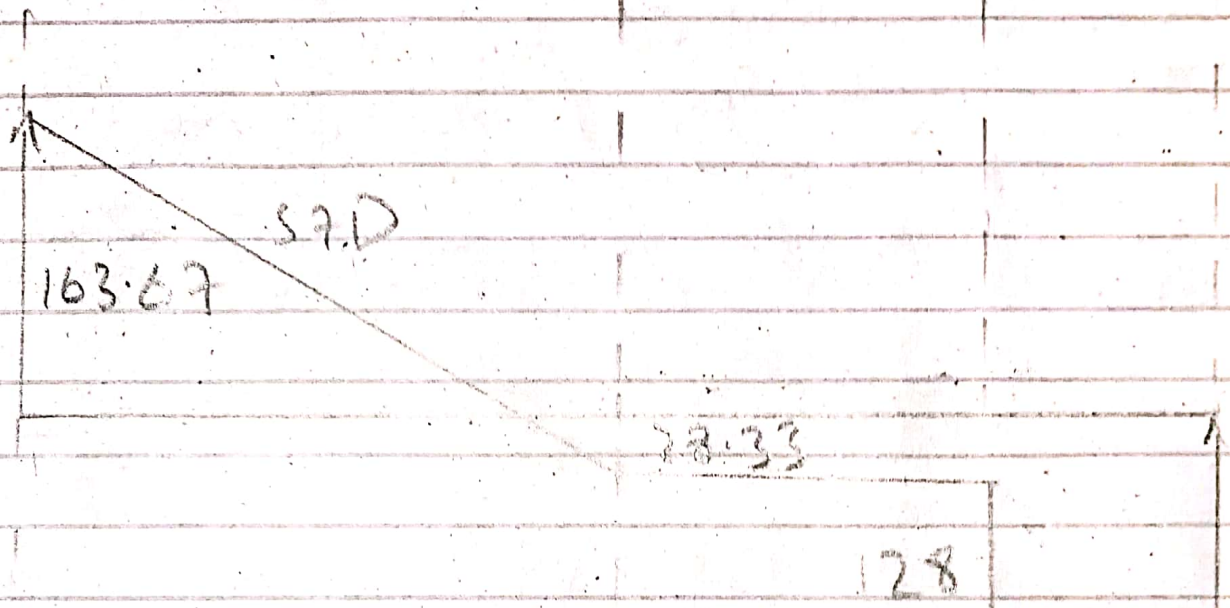
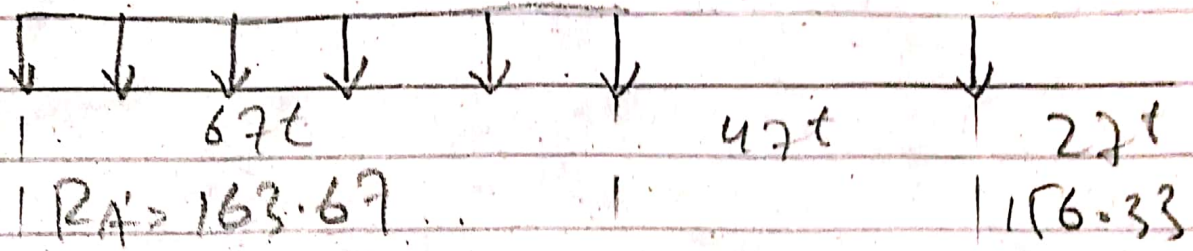
$$\sum M_{5.11} = 0 \text{ +}$$

$$\sum M_{5.11} = -163.67(5.11) + 32(6)$$
$$\left(\frac{5.11}{3}\right)$$

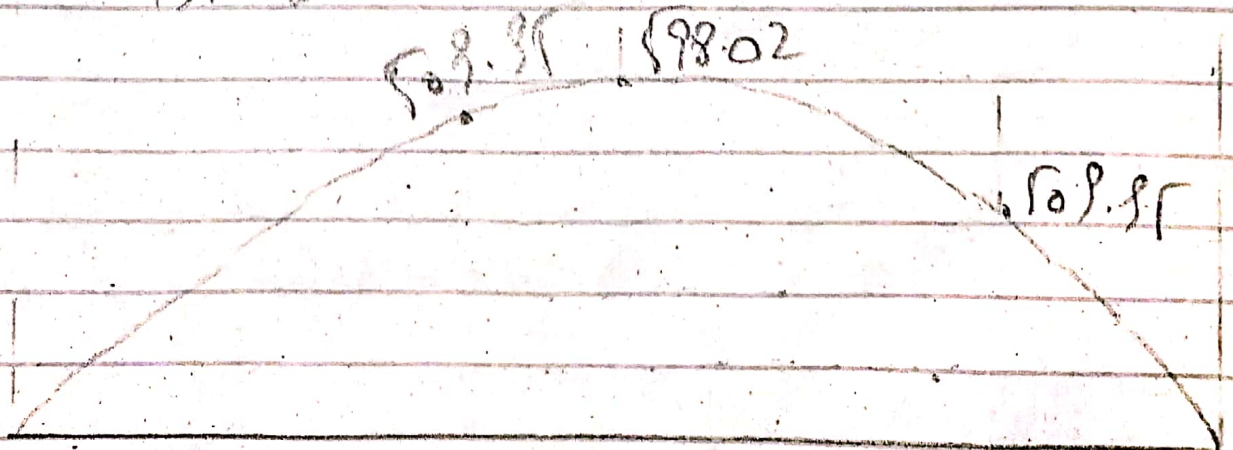
$$\sum M_{5.11} = 509.89$$

(5)

# Shear Force Bending Moment Diagram



## BMD





(6)

Moment of inertia

$$y_1 = 5.7, y_2 = 3, y_3 = 0.7$$

$$A_1 = 4 \text{ in}^2, A_2 = 4 \text{ in}^2$$
$$A_3 = 4 \text{ in}^2$$

$$y = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3}$$

$$y = 3''$$

$$I_1 = \frac{bh^3}{12}$$

$$I_3 = \frac{b \times h^3}{12}$$

$$I_1 = \frac{4 \times 1^3}{12}$$

$$I_3 = \frac{4 \times 1^3}{12}$$

$$I_1 = 0.33 \text{ in}^4$$

$$I_3 = 0.33 \text{ in}^4$$

$$I_2 = \frac{h^3 \times b}{12}$$

$$I_2 = 0.33 \text{ in}^4$$

$d$

$$\begin{aligned}d_1 &= \bar{y} - y_1 \\d_1 &= 3 - 5 \\d_1 &= -2\end{aligned}$$

$$\begin{aligned}d_2 &= \bar{y} - y_2 \\&= 3 - 3 \\d_2 &= 0\end{aligned}$$

$$\begin{aligned}d_3 &= \bar{y} - y_3 \\&= 3 - 0 \\d_3 &= 3\end{aligned}$$

$A d^2$

$$\begin{aligned}① A_1 d_1^2 &= 4 \times (-2)^2 \\&= 2 \text{ inch}^4\end{aligned}$$

$$\begin{aligned}② A_2 d_2^2 &= 4 \times 0 \\&= 0\end{aligned}$$

$$\begin{aligned}③ A_3 d_3^2 &= 4 \times (3)^2 \\&= 2 \text{ inch}^4\end{aligned}$$

$$\begin{aligned}I_{x1} &= I_1 + A_1 d_1^2 \\&= 0.33 + 2 \\&= 2.33 \text{ inch}^4\end{aligned}$$

$$\begin{aligned}I_{x2} &= I_2 + A_2 d_2^2 \\&= 5.33 \text{ inch}^4\end{aligned}$$

$$\begin{aligned}I_{x3} &= I_3 + A_3 d_3^2 \\&= 2.33 \text{ inch}^4\end{aligned}$$

$$\bar{I}_{xx} = I_{x_1} + I_{x_2} + I_{x_3}$$

$$= 2(1.33) + 1.33 + 2(1.33)$$

$$\bar{I}_{xx} = 5.6 \text{ cm}^4$$



(8)

Shear Stress

for  $v = 116.33$

Case 1<sup>a</sup>-

$$\tau_{\text{Top fiber}} = \frac{VQ}{Ib}$$

$$= \frac{116.33 \times 0}{6}$$

$$= 0 \text{ psi}$$

Case 2<sup>A</sup>-

for 2 inches below

$$\tau_{1A} = \frac{116.33 \times 10}{6(4)}$$

$$= 6.97 \text{ psi}$$

Case 3<sup>B</sup>-

$$\tau_{3B} = \frac{116.33 \times 10}{6}$$

$$\tau_{1B} = 27.91 \text{ psi}$$

(9)

Case 3: stress at  
centroidal Axis

$$\tau_{max} = \frac{VQ}{Ib}$$

$$Q = Q_1 + Q_2$$

$$Q = 10 + 1(2)$$

$$Q = 12$$

$$\tau_{max} = \frac{156.33 \times 12}{86}$$

$$\tau_{max} = 3348 \text{ psc}$$

Case 4A: 2 mm Above bottom

$$\tau_{2A} = \frac{VQ}{Ib}$$
$$= \frac{156.33 \times 10}{86 \times 4}$$

$$= 6.97 \text{ psc}$$

Case 4B =

$$\tau_{20} = \frac{VQ}{Ib}$$

$$= \frac{156.33 \times 10}{86} = 27.91 \text{ psc}$$



(10)

Case 5 At bottom fiber

$$\begin{aligned}\tau_{\text{Bottom}} &= \frac{VQ}{It} \\ &= \frac{156.33 \times 0}{56} \\ &= 0 \text{ psi}\end{aligned}$$

Case 6

$$\begin{aligned}VQ &= -28.33 \\ Q &= 12\end{aligned}$$

$$\begin{aligned}\tau_{\text{max}} &= \frac{28.33 \times 12}{56(1)} \\ &= 6.07 \text{ psi}\end{aligned}$$

Case 7 at 1 inch below

$$\begin{aligned}\tau_A &= \frac{28.33 \times 10}{56(4)} \quad b=4 \\ &= 1.26 \text{ psi}\end{aligned}$$

$$\begin{aligned}\tau_B &= \frac{28.33 \times 60}{56} \quad b=7 \\ &= 5.05 \text{ psi}\end{aligned}$$

⑪

## Flexural Stress

$$\sigma = \frac{My}{I}$$

$$\text{Moment } M = 598.02$$

$$I = 56$$

Case 1 - at top of fiber

$$\sigma_{\text{top}} = \frac{My}{I}$$

$$= \frac{598.02 \times 3}{56}$$

$$= 32.03 \text{ psi}$$

Case 2 - 1 inch below top

$$\sigma_1 = \frac{My}{I}$$

$$= \frac{598.02 \times 2}{56}$$

$$= 21.35 \text{ psi}$$



(12)

Case 3<sup>rd</sup> at Geometrical  
Centroid

$$\sigma = \frac{My}{I} \quad \text{at } y=0$$

$$= 0 \text{ psi}$$

Case 4<sup>th</sup> (7 in above)

$$\sigma = \frac{My}{I}$$

$$= \frac{598.02 \times 2}{I}$$

$$= 21.35 \text{ psi}$$

Case 5<sup>th</sup> - at bottom

$$\sigma = \frac{My}{I}$$

$$= \frac{598.02 \times 3}{I}$$

$$= 32.03 \text{ psi}$$

(13)

Shear Force & Bending  
Stress Diagram

\* Stress state of a point  
& element =

Flexural stress at point E'

$\sigma_x = 21.35 \text{ psi}$  from Case 2  
1 inch below  
top fiber

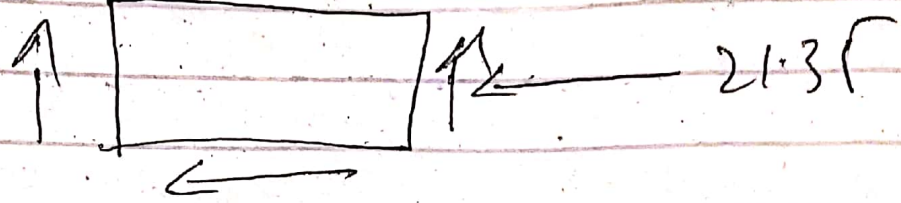
Now shear stress at point C

$\tau_{xy} = 1.26 \text{ psi}$  from  
Case 7

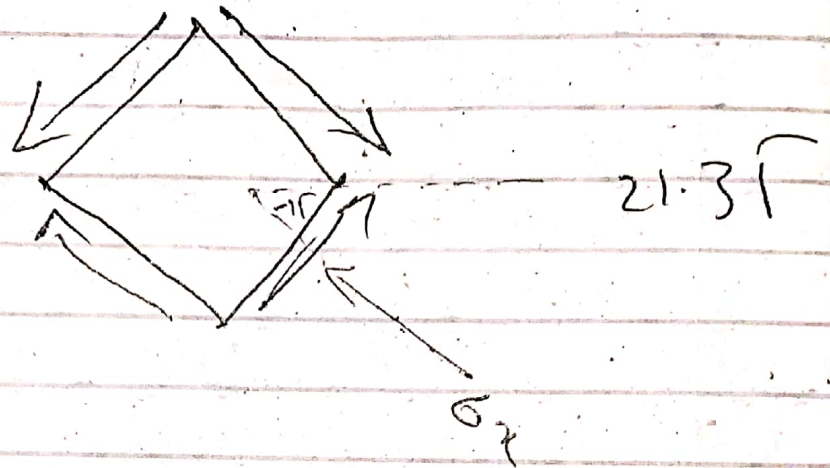
$\sigma_x = -21.35 \text{ (compressive)}$



# Stress Transformation (14)



Let assume  $\theta = -15^\circ$



Now

$$\sigma_x = \frac{\sigma_x + \sigma_y}{2} + \frac{\sigma_x - \sigma_y}{2} \cos 2\theta + \tau_{xy} \sin 2\theta$$

$$\begin{aligned} \sigma_x &= \frac{-21.3 \text{ psi} + 0}{2} + \frac{(-21.3 \text{ psi})}{2} \cos 2(15^\circ) \\ &\quad + 1.26 \{ \sin 2(-15^\circ) \} \\ &= -10.67 - 10.67(0.866) + 1.26(-0.5) \end{aligned}$$

$$\sigma_x' = -20.54 \text{ psi}$$

(17)

$$\sigma_y' = \frac{\sigma_x + \sigma_y}{2} - \frac{\sigma_x - \sigma_y}{2} \cos 2\theta - \tau_{xy} \sin 2\theta$$

$$= -10.67 + 10.67(0.866) - 1.26(-0.5)$$

$$= +0.7 \text{ psi}$$

$$\tau_{xy}' = -\left(\frac{\sigma_x - \sigma_y}{2}\right) \sin 2\theta + \tau_{xy} \cos 2\theta$$

$$= -\left(\frac{-21.3(-0)}{2}\right) \sin 2(-15) + 1.26 \left\{ \cos 2(-15) \right\}$$

$$= 10.67(0.0) + 1.26(0.866)$$

$$\tau_{xy}' = -4.24 \text{ psi}$$

Principal Stress:

$$\tan 2\theta_p = \frac{\tau_{xy}}{(\sigma_x - \sigma_y)/2}$$

$$\sigma_x = -21.3 \quad \sigma_y = 0$$

$$\tau_{xy} = 1.26$$



(16)

$$\tan 2\theta = \frac{1.26}{(-21.35)/2}$$

$$= \frac{1.26}{-10.67}$$

$$= -0.11$$

$$\tan \theta = \frac{-0.11}{2}$$

$$= -0.05$$

$$\theta = \tan^{-1}(0.05)$$

$$\theta = -2.86$$

$$\text{Now } \sigma_x' = \frac{\sigma_x + \sigma_y}{2} + \frac{\sigma_x - \sigma_y}{2} \cos 2\theta + \tau_{xy} \sin 2\theta$$

$$\sigma_x' = \left( \frac{-21.35 + 0}{2} \right) + \left( \frac{21.35 - 0}{2} \right) \cos 2(-2.86) + 1.26 \left\{ \sin 2(-2.86) \right\}$$

$$= -10.67 - 10.67(0.88) + 1.26(-0.09)$$
$$= -11.74 \text{ psi}$$

(17)

$$\sigma_{xy} = \frac{\sigma_x + \sigma_y}{2} - \frac{\sigma_x - \sigma_y}{2} \cos 2\theta -$$

$$\tau_{xy} \sin 2\theta$$

$$= \left( \frac{-21.35 + 0}{2} \right) - \left( \frac{21.35 - 0}{2} \right) \cos 2(-2.86) -$$
$$(1.26) \sin(-2.86)$$

$$= -10.67 + 10.67(0.88) - 1.26(-0.05)$$

$$= -8.58 \text{ psi}$$

Shear Stress:

$$\tan 2\theta_s = \frac{(\sigma_x - \sigma_y)/2}{\tau_{xy}}$$

$$\tan 2\theta_s = \frac{((21.35 - 0)/2)}{\tau_{xy}}$$

$$= \frac{(-21.35 - 0)}{1.26} / 2$$

$$\tan 2\theta_s = 8.47$$



$$\tan \theta = \frac{8.47}{2} = 4.23$$

$$\theta_s = \tan^{-1}(4.23)$$

$$\theta_s = 76.69^\circ$$

$$\text{Now } \bar{x}'_y' = \frac{-b_x - b_y \sin 2\theta}{2} +$$

$$\bar{x}_y \cos 2\theta$$

$$= -\frac{(-21.35 - 0) \sin 2(76.69)}{2}$$

$$+ 1.26 \{ \cos 2(76.69) \}$$

$$= 10.67 (0.448) + 1.26 (-0.89)$$

$$\bar{x}'_y' = \boxed{3.68}$$

(18)

Mohr's Circle

Mohr's Circle Center Coordinates

$$(h, k) = \left[ \frac{\sigma_x + \sigma_y}{2}, 0 \right]$$

$$= \left[ \frac{-21.3}{2}, 0 \right]$$

$$= [-10.67, 0]$$

$$\text{Radius} = r = \sqrt{\left( \frac{\sigma_x - \sigma_y}{2} \right)^2 + (\tau_{xy})^2}$$

$$= \left( \frac{-21.3 - 0}{2} \right)^2 + (1.26)^2$$

$$= \sqrt{(-10.67)^2 + (1.26)^2}$$

$$\text{Radius} = 10.67$$