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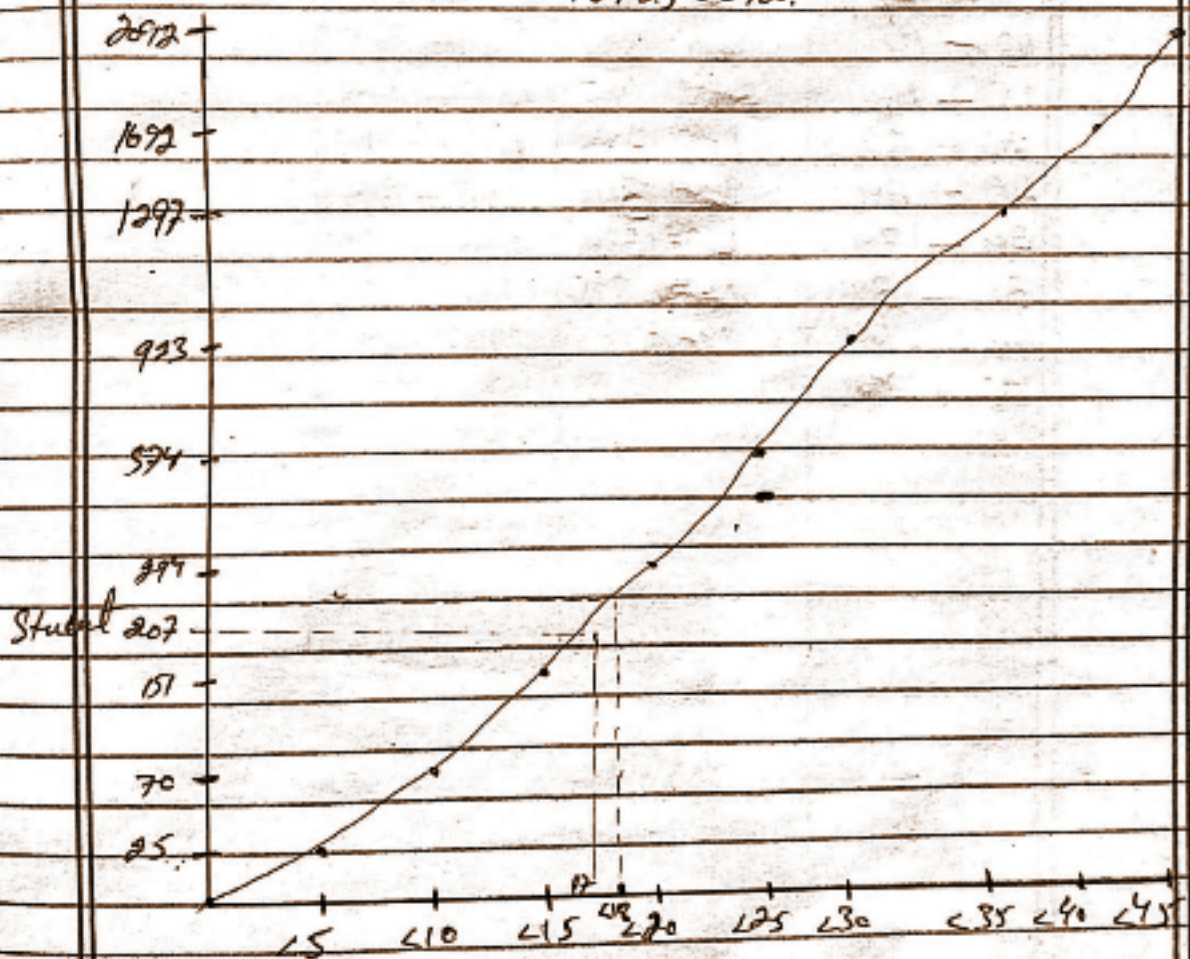
**Assignment:** Probability & Statistics

(21). Part (a)

Time taken  $< 5, < 10, < 15, < 20, < 25, < 30, < 35, < 40$   
interval.  $< 45,$

Frequency:- 25, 45, 81, 143, 280, 349, 374, 395, 400.

Cumulative frequency:- 25, 70, 151, 294, 574, 923, 1297,  
1692, 2092.

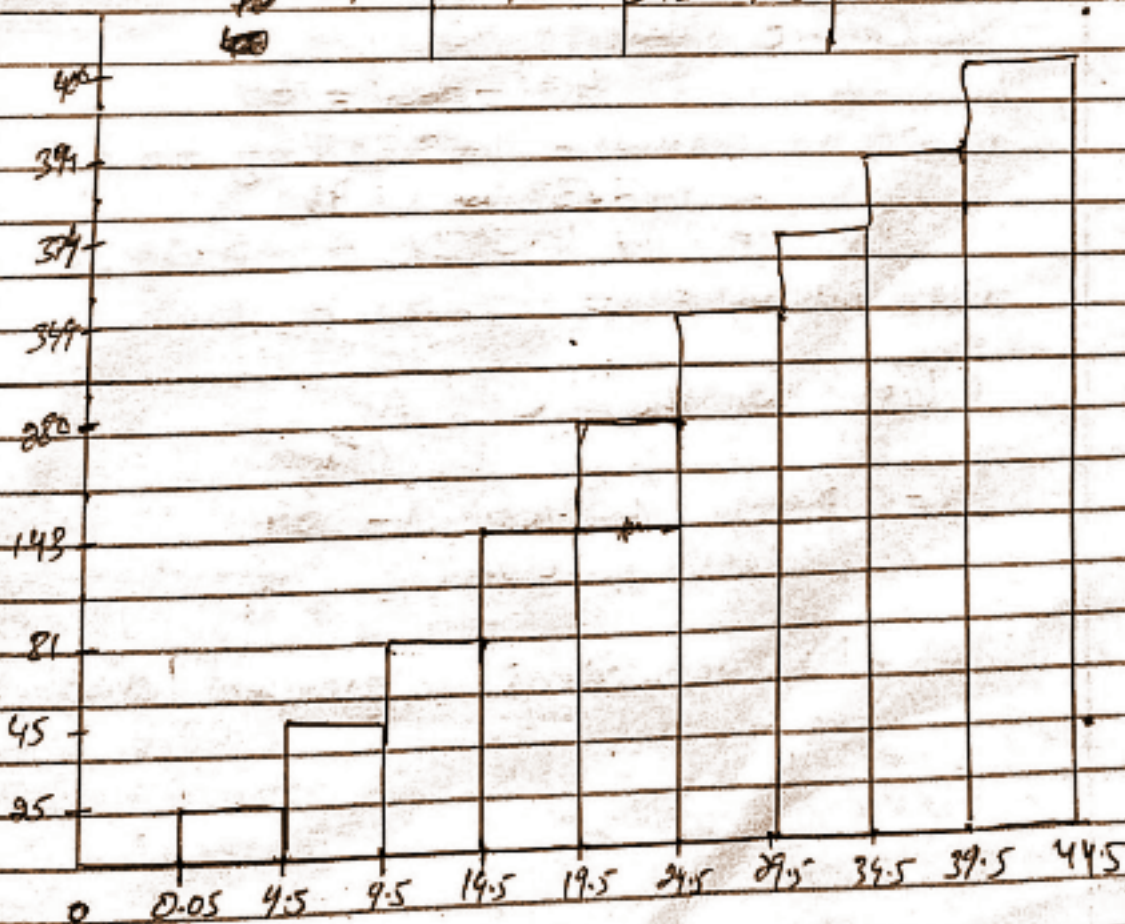


Comment:- The estimate students all 207  
students who take less than 18 minutes  
to walk to the the school at a  
particular morning.

### Question ① Part b

For writing or drawing histogram we need to construct frequency distribution table and then put the class boundary on x-axis ( $x = CB$ ) and put the frequency on y-axis ( $y = \text{frequency}$ ).

|       |     |             |
|-------|-----|-------------|
| 0-4   | 25  | 0.05 - 4.5  |
| 5-9   | 45  | 4.5 - 9.5   |
| 10-14 | 81  | 9.5 - 14.5  |
| 15-19 | 148 | 14.5 - 19.5 |
| 20-24 | 280 | 19.5 - 24.5 |
| 25-29 | 349 | 24.5 - 29.5 |
| 30-34 | 374 | 29.5 - 34.5 |
| 35-39 | 395 | 34.5 - 39.5 |
| 40-44 | 400 | 39.5 - 44.5 |



## Question #2

Construct grouped distribution table for the following data and calculate Mean, Mode, and quartiles.

423, 369, 387, 411, 393, 394, 371  
377, 389, 409, 392, 408, 431  
401, 363, 391, 405, 382, 400, 381  
399, 415, 428, 422, 396, 372, 410,  
419, 386, 390

Total number of data = 30

Smallest data = 362

Largest data = 431

Range =  $431 - 362 = 69$ .

Class interval =  $1 + 3.33 \log 30 =$

$= 1 + 3.33 \log (1.47)$

$= 1 + 4.8951 = 5.8951$

class interval = 6

Class width =  $R/k$

R = Range which is 69

k = class interval

Let's construct grouped distribution table.

| Class     | Frequency | C-Mark | Fx    |
|-----------|-----------|--------|-------|
| 362 - 372 | 4         | 367    | 1468  |
| 373 - 383 | 3         | 378    | 1134  |
| 384 - 394 | 8         | 389    | 3112  |
| 395 - 405 | 5         | 400    | 2000  |
| 406 - 416 | 5         | 411    | 2055  |
| 417 - 427 | 3         | 422    | 1266  |
| 428 - 431 | 2         | 433    | 866   |
|           | 30        |        | 11901 |

Simple or population mean =  $\frac{\text{Sum of all observations}}{\text{Total of observation}}$

$$\text{Simple mean or population mean} = \frac{11914}{30} = 397.13$$

Now to find grouped arithmetic mean

$$\text{Mean} = \frac{\sum fx}{\sum f} = \frac{11901}{30} = 396.7$$

$$\bar{x} = 396.7$$

Now Let's find mode.

|         |   |                       |
|---------|---|-----------------------|
| 362-372 | 4 | 361.5 - 372.5         |
| 373-383 | 3 | 372.5 - 383.5         |
| 384-394 | 8 | 383.5 - 394.5 = Mode. |
| 395-405 | 5 | 394.5 - 405.5         |
| 406-416 | 5 | 405.5 - 416.5         |
| 417-427 | 3 | 416.5 - 427.5         |
| 428-431 | 2 | 427.5 - 431.5         |

$$\text{Mode} = l + \frac{(f_m - f_1) \times h}{(f_m - f_1) + (f_m - f_2)}$$

$$= 383.5 + \frac{(8 - 3) \times 11}{(8 - 3) + (8 - 5)}$$

$$= 383.5 + 6.875$$

### Quartiles

| Class   | Frequency | Cumulative Frequency |
|---------|-----------|----------------------|
| 362-372 | 4         | 4                    |
| 373-383 | 3         | 7                    |
| 384-394 | 8         | 15                   |
| 395-405 | 5         | 20                   |
| 406-416 | 5         | 25                   |
| 417-427 | 3         | 28                   |
| 428-431 | 2         | 30                   |
|         | 30        |                      |

$$\text{Quartile 1} = l + \frac{\frac{n}{4} - c_{f-1}}{f} \times i$$

$$Q_1 = \frac{n}{4} = \frac{1 \times 30}{4} = 7.5$$

$$l = 384, \quad c_{f-1} = 7 \quad f = 8 \quad i = 10$$

$$Q_1 = 384 + \frac{7.5 - 7}{8} \times 10$$

$$Q_1 = 394$$

Q3 = quartile 3<sup>rd</sup>

$$\frac{3n}{4} = \frac{3130}{4} = 22.5$$

$$d = 406, \quad c_f - 1 = 20, \quad b_f = 5, \quad c = 10$$

$$= 406 + \frac{22.5 - 20}{5} \times 10$$

$$Q3 = 411$$

Q4) For the following grouped distribution table calculate the Variance and Standard deviation.

Class = 64-84, 85-104, 105-124, 125-144, 145-164, 165-184, 185-204

Frequency = 15, 18, 27, 10, 6, 5, 13

| Class   | freq | $x$   | $(x - \bar{x})$ | $(x - \bar{x})^2$ | $f(x - \bar{x})^2$ |
|---------|------|-------|-----------------|-------------------|--------------------|
| 64-84   | 15   | 74    | -49.14          | 2414.7            | 36220.5            |
| 85-104  | 18   | 94.5  | -28.69          | 820.2             | 14763.6            |
| 105-124 | 27   | 114.5 | -8.64           | 74.6              | 2052               |
| 125-144 | 10   | 134.5 | 11.36           | 129               | 1290               |
| 145-164 | 6    | 154.5 | 31.36           | 129               | 774                |
| 165-184 | 5    | 174.5 | 51.36           | 983.4             | 4917               |
| 185-204 | 13   | 194.5 | 71.36           | 5092.2            | 66198.6            |

$$\Sigma f = 94$$

$$\Sigma f(x - \bar{x})^2 = 1263178.9$$

$$\bar{x} = \frac{\Sigma fx}{\Sigma f} = \frac{15(74) + 18(94.5) + 27(114.5) + 10(134.5) + 6(154.5) + 5(174.5) + 13(194.5)}{94}$$

$$\bar{x} = 123.14$$

Now finding standard deviation

$$s^2 = \frac{\sum f(x - \bar{x})^2}{\sum f}$$

$$s^2 = \frac{126178.9}{94}$$

$$s^2 = 1342.3$$

$$\sqrt{s^2} = \sqrt{1342.3}$$

$s = 36.64$ . Standard deviation.

Now Let's find variance.

$$V = \frac{\sum f(x - \bar{x})^2}{\sum f - 1}$$

$$V = \frac{126178.9}{94-1} = \frac{126178.9}{93}$$

$$V = 1356.762$$



Q3) By multiplying each of the numbers 3, 6, 2, 17, 5 by 2 and then adding 5, we obtain 11, 17, 9, 7, 19, 15, what is the relation between the standard deviation and the means of the two sets

3, 6, 2, 17, 5

11, 17, 9, 19, 15, 7

First Let's find mean

$$\text{Mean} = \frac{\text{Sum of all obs.}}{\text{Number of obs}}$$

$$\text{Mean} = \frac{24}{6} = 4$$

Let's find Median.

→ Write the set in ascending form

1, 2, 3, 5, 6, 7

$$\text{Median} = \frac{3+5}{2} = 4$$

$$\bar{x} = 4$$

$$\text{Range} = 7 - 1 = 6$$

$$\text{Standard deviation} = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$$

| $x_i$ | $x - \bar{x}$ | $(x - \bar{x})^2$ | Σ                         |
|-------|---------------|-------------------|---------------------------|
| 1     | -3            | 9                 | S = $\frac{25}{6} = 4.16$ |
| 2     | -2            | 4                 |                           |
| 3     | -1            | 1                 |                           |
| 5     | 1             | 1                 |                           |
| 6     | 2             | 4                 |                           |
| 7     | 3             | 6                 |                           |

Standard deviation for the first is 4.16.

After multiplying the first set with 2 and adding 5 we get 11, 17, 9, 19, 15, 7.

11, 17, 9, 19, 15, 7

Write it in ascending order.

7, 9, 11, 15, 17, 19

$$\text{Mean} = \frac{78}{6} = 13$$

$$\text{Median} = \frac{11+15}{2} = 13$$

$$\text{Range} = 12.$$

$$\text{Standard deviation} = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$$

| x  | $x - \bar{x}$ | $(x - \bar{x})^2$ |
|----|---------------|-------------------|
| 7  | -6            | 36                |
| 9  | -4            | 16                |
| 11 | -2            | 4                 |
| 15 | 2             | 4                 |
| 17 | 4             | 16                |
| 19 | 6             | 36                |
|    |               | 112               |

$$s = \frac{112}{6} = 18.66$$

Note:- When we add and multiply a digit to the set. All the statistical values will be change including mean and standard deviation.

The first set is 3, 6, 2, 1, 7, 5 if we just add 5. Let's see what changes.

Write in Ascending form.

1, 2, 3, 5, 6, 7

Add 5 to each digit of the set.

6, 7, 8, 10, 11, 12

$$\text{Mean} = \frac{54}{6} = 9$$

$$\text{Median} = \frac{8+10}{2} = 9$$

$$\text{Standard deviation} = \frac{\sum(x-\bar{x})^2}{n}$$

| $x$ | $x - \bar{x}$ |    |
|-----|---------------|----|
| 6   | -3            | 9  |
| 7   | -2            | 4  |
| 8   | -1            | 1  |
| 10  | 1             | 1  |
| 11  | 2             | 4  |
| 12  | 3             | 9  |
|     |               | 25 |

$$\text{Standard deviation} = \frac{25}{6} = 4.16$$

Remember! - When we add or subtract the value from a set it can affect the mean but it can not affect the standard deviation.

## Comparison of three different sets of data.

|  |  |   |
|--|--|---|
| 1, 2, 3, 5, 6, 7,<br>↓<br>1, 2, 3, 5, 6, 7 | 1, 2, 3, 5, 6, 7 Adding<br>5<br>↓<br>6, 7, 8, 10, 11, 12 | 1, 2, 3, 5, 6, 7 $\times 2$<br>and $+ 5$<br>11, 17, 9, 19, 15, 17 |
| Mean = 4                                   | Mean = 9   | Mean = 13   |
| Median = 4                                 | Median = 9   | Median = 13   |
| Range = 6                                  | Range = 6  | Range = 12  |
| Standard d = <del>4.16</del><br>4.16       | S.d = 4.16   | S.d = 18.66   |

Note:- The relation of mean and standard deviation depends upon the values when we add or subtract there will be no effect on the standard deviation while it will effect the mean.

When we multiply the set by any scalar so all the statistics value can be change and effected.

As we compare all these two cases above in the table of comparison.

Q5) Comment on the following sentences.

(a) The depth of a river at four different points are 2, 7, 5, 6 feet respectively. The average depth is 5 feet. Therefore all the people with height 5 feet can cross it.

↳ As we know four different points 2, 7, 5, 6 while the average = 5. reflects all other points are different from the average value so therefore it show dispersion.

(b) The average marks of one class of students are 30. Therefore every student is hopeless.

↳ This sentence means that all students get the average marks 30 which really affect the performance of the class and reflect the poor image of the whole class.

(c) The average income of a King and his household servants are £20.000 per month. Therefore all the household servants must be fabulously paid.

↳ It reflect the direct correlation among average income of King family and payments to their servant i.e.  
King's family  $\uparrow$  → payment to servant