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~~Assignment~~ Assignment # 03

Subject :- MOS II

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pb #01

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Given data:

$$L = 6ft$$

$$L_c = 0.7L$$

$$E = 10.3 \times 10^6 \text{ psi}$$

$$\text{Factor of safety} = 2$$

$$b = 3/4 \text{ in } h = 2 \text{ in}$$

Req:

safe central load = P

Sol:

$$P_{cr} = \frac{\pi^2 EI}{L_c^2}$$

$$= P_{cr} = \frac{\pi^2 E A r^2}{L_c^2} \quad \text{--- (1)}$$

Now $r = \sqrt{I/A}$

$$r = \sqrt{\frac{1.6^{3/2}}{12}}{\frac{12}{b^4}}$$

$$= r = \sqrt{h^2/12}$$

$$r = \frac{b}{2\sqrt{3}}$$

$$= r = \frac{3/4}{2\sqrt{3}}$$

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$$\alpha = \frac{0.75}{7.46}$$

$$\alpha = 0.216 \text{ in}$$

Now

$$P_{cr} = \frac{\tilde{\lambda}^2 E A}{(L/\alpha)^2}$$

$$P_{cr} = \frac{(2.14)^2 (10.3 \times 10^6) (1.5 \text{ in}^2)}{\left(\frac{0.7 \times 1}{\alpha}\right)^2}$$

$$= P_{cr} = \frac{9.8596 \times 15.45 \times 10^6}{\left(\frac{0.7 \times 72}{0.216}\right)^2}$$

$$= P_{cr} = \frac{152.33}{5444.4}$$

$$P_{cr} = 2.7979 \times 10^3 \text{ psi}$$

$$P_{cr} = 2.7979 \text{ ksi}$$

for a safety

$$P_{safe} = \frac{P_{cr}}{\text{factor of safety}}$$

$$P_{safe} = \frac{2.7979}{2}$$

$$P_{safe} = 1.3989 \text{ ksi}$$

ps #02

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Given data:

$$\text{load} = 20 \text{ kips} = 2.4 \times 10^5 \text{ psi}$$

$$\text{length } L = 10 \text{ ft}$$

$$E = 29 \times 10^6 \text{ psi}$$

req:

length of each side = ?

sol:

As we know that

$$\frac{le}{r} = \frac{\sqrt{\pi^2 E}}{6p} \Rightarrow le/r = \frac{\sqrt{(3.14) \times (29 \times 10^6)}}{2.4 \times 10^5}$$

$$\frac{le}{r} = \sqrt{1.19 \times 10^3}$$

$$le/r = 34.5$$

$$r = le/34.5$$

$$r = \frac{10 \times 12}{34.5}$$

$$r = 120/34.5$$

$$r = 3.47 \text{ inch}$$

(11)

1st method:

$$r = \frac{\sqrt{b^2}}{12}$$

$$r^2 = \frac{1}{12} = \frac{b^2}{144}$$

$$b^2 = 144 \times (9.4)^2 \times 12$$

$$b^2 = 138.72$$

$$\sqrt{b^2} = \sqrt{138.72}$$

$$b = 11.77$$

2nd method

$$E/A = 12r^2$$

$$A = E/12r^2$$

$$h^2 = \frac{b^2}{12} \times 12r^2$$

$$h = \frac{b^2}{12r^2}$$

$$h = 12r^2$$

$$h = 11.77$$

Q 39.

(5)

Prison data

$$\text{load} = 20 \text{ kips} = 2.4 \times 10^5 \text{ psi}$$

$$\text{length} = l = 10 \text{ ft}$$

$$E = 1.6 \times 10^6 \text{ psi}$$

Ans:

length of each side. ?

Sol

As we know that

$$l_e / \alpha = \frac{\sqrt{\pi^2 E}}{6P}$$

$$l_e / \alpha = \frac{(\sqrt{3.14})^2 (1.6 \times 10^6)}{2.4 \times 10^5}$$

$$l_e / \alpha = \frac{\sqrt{9.8596 \times 1.6 \times 10^5}}{2.4}$$

$$l_e / \alpha = \sqrt{85.780}$$

$$l_e / \alpha = 8.107$$

$$\alpha = l_e / 8.107$$

$$\alpha = 10 \times 12 / 8.107$$

(6)

$$r = 14.802 \text{ m/s}$$

1st method

$$r = \sqrt{b^2/12}$$

$$r^2 \times 12 = b^2$$

$$b^2 = (14.802)^2 \times 12$$

$$b^2 = 2629.190$$

$$\sqrt{b^2} = \sqrt{2629.190}$$

$$b = 51.275$$

2nd method

$$I = Ar^2$$

$$A = I/r^2$$

$$A^2 = \frac{I^2}{r^2}$$

$$I = A^2/r^2$$

$$A^2 = I r^2$$

$$A^2 = 2629.190$$

$$\sqrt{A^2} = \sqrt{2629.190}$$

$$A = 51.275$$

$$\phi = 0.4$$

(7)

Given data:

$$\text{Column} = 36 \text{ mm} \times 45 \text{ mm}$$

$$E = 200 \times 10^3 \text{ Pa}$$

$$C_p = 240 \times 10^6 \text{ Pa}$$

$$L = 12 \text{ m}$$

$$\text{Factor of safety} = 2.5$$

Q1 a) $q = \text{min} = ?$

(b) $p_{\text{safe}} = ?$

Sol:

As we know that

$$C_p = \frac{E \lambda^2}{(l/r)^2}$$

$$l/r = \sqrt{\frac{E \lambda^2}{C_p}}$$

$$l/r = \sqrt{\frac{(3.14)^2 \times (200 \times 10^3)}{240 \times 10^6}}$$

$$l/r = 90.69$$

Now $r = \sqrt{b^2/12}$

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$$r = \frac{\sqrt{145}}{12}$$

$$r = 12.98 \text{ mm}$$

Now

$$l_e = 90.64 \times 12.98$$

$$l_e = 1177.44 \text{ mm}$$

Now factor for pin hinge

$$L = l_e$$

$$L_{\text{mm}} = 1177.44 \text{ mm}$$

(per (B))

$$P_{cr} = \frac{\pi^2 EA r^2}{L^2}$$

$$P_{cr} = \frac{(3.14)^2 (200 \times 10^5) (12.98)^2}{(12 \times 1000)^2}$$

$$P_{cr} = 32.2243 \text{ kN}$$

Now

For $P_{\text{safe}} = ?$

$$P_{\text{safe}} = \frac{P_{cr}}{\text{factor of safety}}$$

(9)

$$P_{safe} = \frac{32.2343}{2.5} \text{ GM}$$

$$P_{safe} = 12.8937 \text{ GM.}$$