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Section = "A"

Subject =

Intro To Structural Dynamic

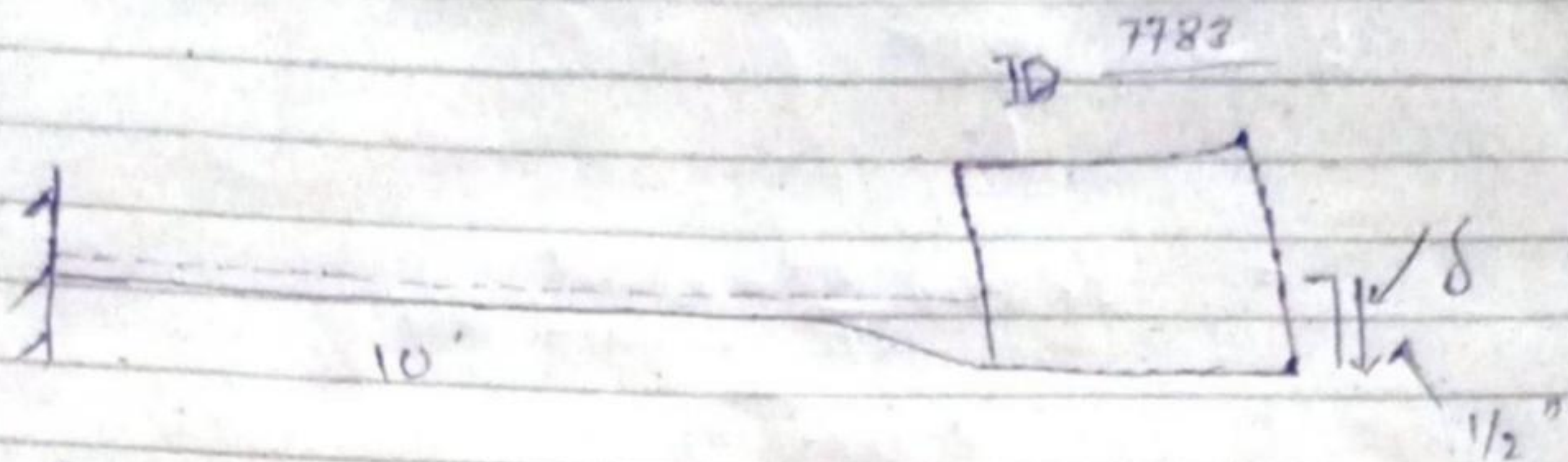
&

EARTHQUAKE

ENGG.



①
Q No 1: Problem.



Given data: $E = 29,000 \text{ ksi}$
 $I = 150 \text{ in}^4$

δ_{st} = Deflection due to 7783 lb static load.

Beam is pulled $1/2$ " downwards.

R.D: Natural time periods of system develop and solve the equation of motion.

Draw graph to show the variation of displacement with time & the vibration of equivalent static force with time.

Solution:

General EOM for SDOF system is;

$$Ku + \dot{u} + m\ddot{u} = P(t)$$

Since system is undamped $(C=0)$.
undergoing free vibration $P(t)=0$

Hence general EOM becomes

$$Ku + m\ddot{u} = 0 \rightarrow \text{①}$$

②

$$K = \frac{3EI}{l^3}$$
$$= \frac{3 \times 2900 \frac{\text{K}}{\text{in}^2} \times 15 \text{ in}^4}{(10 \times 12 \text{ in})^3}$$

$$K = 7.55208 \text{ K/in}$$

⇒ In order to eliminate chances of mistake during calculation, it is more appropriate to use fundamental unit like lb, ft, sec or kg, m, sec.

$$K = 7.55208 \text{ K/in} \Rightarrow 90625 \text{ lb/ft.}$$

$$m = \frac{w/g}{g} = \frac{7783}{32.2} \Rightarrow$$

$$m = 241.708 \text{ slug.}$$

$$\omega_n = \sqrt{\frac{K}{m}} \Rightarrow \sqrt{\frac{90625}{241.708}}$$

$$\omega_n = 19.36 \text{ rad/sec.}$$

$$T_n = \frac{2\pi}{\omega_n} = \frac{2\pi}{19.36} = 0.3243 \text{ sec}$$

put m & K in eqn (1).

$$90625u + 241.708 \ddot{u} = 0$$

where K is in lb/ft is lbsec/ft².

(3)

General solution to EOM for undamped free vibration is

$$u(t) = u(0) \cos(\omega_n t) + \frac{\dot{u}(0)}{\omega_n} \sin(\omega_n t)$$

$$u(0) = \frac{1}{2}'' = \frac{1}{24} \delta'' \quad \dot{u}(0) = 0$$

$$u(t) = \left(\frac{1}{24}\right) \times \cos(19.36) + 0 = \left(\frac{1}{24}\right) \times \cos(19.36)$$

Equivalent static force at any time 't' is

$$F_s(t) = k \cdot u(t) = \frac{90625 \times \cos(19.36)}{24}$$

$$\boxed{(85.5054 \text{ t})}$$

Amplitude of dynamic displacement, u_0 for undamped free vibration is

$$u_0 = \sqrt{\left(u(0)\right)^2 + \left(\frac{\dot{u}(0)}{\omega_n}\right)^2}$$

$$\sqrt{\left(\frac{1}{24}\right)^2 + 0}$$

$$= \boxed{\frac{1}{24} \delta''}$$

(4)

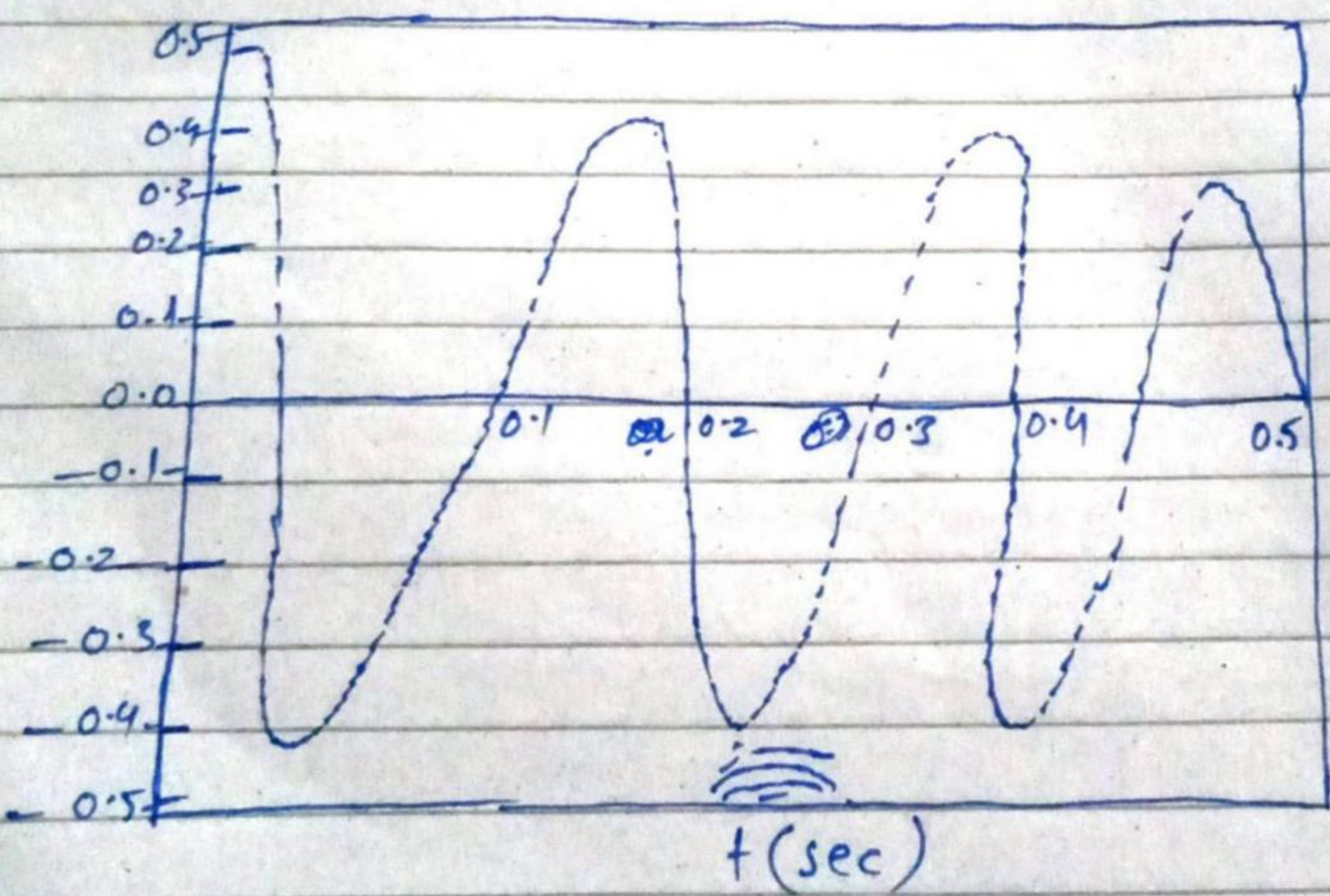
Amplitude of equivalent static
force, f_{so}

$$K_{40} = 90625 \times \frac{1}{24}$$

$$K_{40} = 3776$$

(4)

(5)



Variation of displacement.

QNO2: ①

Given data:

ζ (Damping ratio) of Reinforced
Concrete with considered Cracking = 3-5%
= 3%

Required Data:-

Develop and solve the equation
showing variation in equivalent
static force with time.

→ Draw graph to show the variation of
displacement with time & the variation of
equivalent static force with time.

Solution:-

EOM for damped force vibration is
 $Ku + c\dot{u} + m\ddot{u} = 0$ — (1)
from data.

$$K = 90625 \text{ lb/ft}$$

$$\omega_n = 19.36$$

$$m = 241.708$$

We know that

$$C = \zeta \times 2m\omega_n \\ = (0.03) \times 2(241.708)(19.36)$$

$$C = \boxed{280.76} \text{ lb-sec/ft}$$

(2)

Put the value of eq (1).

$$90625u + 280.76\dot{u} + 241.708u = 0$$

Solution to The EOM form damped free vibration is

$$u(t) = e^{-\zeta\omega_n t} \left[u(0)\cos(\omega_n t) + \frac{1}{\omega_n} \left[\dot{u}(0) + u(0)\zeta\omega_n \right] \sin \omega_n t \right]$$

$$\omega_n = 19.36 \text{ rad/sec}$$

$$u(t) = e^{-0.03(19.36)t} \left[\frac{1}{24} \cos(19.36t) + \frac{1}{19.36} \left[0 + \frac{1}{24} \times 0.03 \times 19.36 \times \sin(19.36t) \right] \right]$$

$$u(t) = e^{-0.5808t} \left[0.041 \cos(19.36t) + 0.0516 \sin(19.36t) \right]$$

$$f_s(t) = K \cdot u(t) \Rightarrow 90625 \times u(t)$$

$$f_s(t) = e^{-0.5808t} \left[90625 \times 0.041 \cos(19.36t) + 90625 \times 0.0516 \sin(19.36t) \right]$$

$$f_s(t) = e^{-0.5808t} \left[3715.62 \cos(19.36t) + 90625 \cdot 0.0516 \sin(19.36t) \right]$$

①

CON03

Problem

Given data:

- Force = 60 kips
- $U_1 = \frac{7783}{1000} = 7.783$
- After $j = 7$ (cycle).
- Completed = 3.57 sec.
- $U_{j+1} = 2.286 \text{ cm} = 0.9 \text{ in.}$
- Ignore the vertical vibration.

Req:

- Damping ratio.
- Natural periods of undamped vibration.
- Stiffness of structural.
- Weight of tank.
- Damping coefficient.
- Number of cycles to reduce the displacement amplitude to 0.5".

(a) Damping Ratio: $\zeta = ?$

$$As = j = \frac{1}{2\pi\zeta} \ln \left[\frac{U_1}{U_{j+1}} \right]$$

Putting value.

$$= 7 = \frac{1}{2(3.14)\zeta} \ln \left[\frac{7.783}{0.9} \right]$$

$$\zeta = (7 \times 2 \times 3.14) \zeta = (2.157)$$

(2)

$$g(43.96) = (2.157)$$

$$g = \frac{2.157}{43.96}$$

$$|g| = 0.049$$

$$|g| = 4.9\%$$

(b) $T_D = ?$

As "Seven" cycles are completed in "3.57" sec.

Thus Time required to complete one cycle = $\frac{7}{3.57} = 1.96 \text{ sec}$

$$T_D = 1.96 \text{ sec}$$

Now $\omega_D = \omega_n \sqrt{1 - g^2}$

$$= \frac{2\pi}{T_D} = \frac{2\pi}{T_n} \left(\sqrt{1 - g^2} \right)$$

As $T_D = \frac{T_n}{\sqrt{1 - g^2}}$

$$T_n = T_D \left(\sqrt{1 - g^2} \right)$$

(3)

$$= 1.96 \sqrt{1 - (0.049)^2}$$

$$\boxed{T_n = 1.9576 \text{ sec.}}$$

Natural period of undamped vibration.

(c) Stiffness of structure $K = ?$

$$\text{As } K = \frac{F \cdot \cos \alpha}{2}$$

$$= K = \frac{60, \cos(60^\circ)}{2}$$

$$\left. \begin{array}{l} F = 60 \text{ kips} \\ \alpha = 60^\circ \end{array} \right\}$$

$$K = 15 \text{ K/in}$$

$$\boxed{K = 18000 \text{ lb/ft}}$$

(4)

(d) Weight of Tank, $w = ?$

As

$$\omega_n = \sqrt{k/m} = \sqrt{\frac{k}{(w/g)}} = \sqrt{\frac{k \cdot g}{w}}$$

$$= \omega_n^2 = \frac{k \cdot g}{w} \Rightarrow \left(W = \frac{k \cdot g}{\omega_n^2} \right)$$

By putting value of $\omega_n = \frac{2\pi}{T_n}$.

$$W = \frac{k \cdot g}{\left(\frac{4\pi^2}{T_n^2} \right)} = k \cdot g \left(\frac{T_n^2}{4\pi^2} \right)$$

$$W = \frac{18000 \text{ lb}}{\text{ft}} \cdot \frac{32.2}{\text{sec}} \left(\frac{(1.9576)^2}{(4(3.14)^2)} \right)$$

$$W = 56319.268 \text{ lb}$$

(5)

"e"

Damping Co-efficient = $C = ?$

gt ix know That $G = \frac{C}{2m\omega n}$

$$\Rightarrow C = G (2m\omega n) = G (2m \left(\frac{2\pi}{T_n} \right))$$

By putting value -

$$C = 0.049 \left(2 \left(\frac{56319.26}{32.2} \right) (2 \cdot (3.14)) \right)$$

1.9576

$$C = 594.87 \text{ lb}\cdot\text{sec}/\text{ft}$$

(F) No of cycle to reduce displacement altitude from 7.783 to 0.5 in?

$j = ?$

$$j = \frac{1}{2\pi G} \ln \left(\frac{u_1}{u_{j+1}} \right)$$

$$= \frac{1}{2(3.14)(0.049)} \ln \left(\frac{7.783}{0.5} \right)$$

$$= \underline{7.01} \text{ "OR"}$$

$$j = 7 \text{ cycle}$$