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SECTION : A

DEPARTMENT : BS (SE)

SUBMET TO : SAIFULLAH JAN

SUBJECT : OPERATIONS RESEARCH

EXAM : MID TERM

SEMISTER : 4<sup>th</sup>

DATE : 14, APRIL, 2020

# ANSWER NO : 1

Mechanics

	1	2	3	4	5	Row minimum
Jobs 1	6	12	3	11	15	3
2	4	2	7	1	10	1
3	8	11	10	7	11	7
4	16	19	12	23	21	16
5	9	5	7	6	10	5

Mechanics

Row Reduction

	1	2	3	4	5
Jobs 1	3	9	0	8	12
2	3	1	6	0	9
3	1	4	3	0	4
4	0	3	10	7	5
5	4	0	2	1	5

Column Min:

0 0 0 0 4

Mechanic = 3

Column Ratio

	1	2	3	4	5
1	3	4	0	8	8
2	3	1	6	0	5
3	1	4	3	0	0
4	0	3	10	7	1
5	4	0	7	1	1

$\bar{5} = 5$  Optimal Solution

Jobs	mechanics	Time
1	3	3
2	4	1
3	5	11
4	1	16
5	2	5
		<hr/> 36

Total Processing Time = 36 hours

# ANSWER NO: 2.

## SOLUTION:-

Step 1: Introduce artificial variable in each row.

Which is,

$$s_1, s_2, s_3$$

$$\left(\frac{1}{2}\right)x_1 + \left(\frac{1}{4}\right)x_2 + s_1 = 4$$

$$x_1 + 3x_2 - s_2 + A_1 = 20$$

$$x_1 + x_2 - s_3 + A_2 = 10$$

Step 2: Put the artificial variable into the objective function: for max - problem max.

$$Z = 2x_1 + 3x_2 + MA_1 + MA_2$$

$$Z - 2x_1 - 3x_2 - MA_1 - MA_2 = 0$$

Step 3:- "Clean UP" the objective function.

Now to make a table

$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$A_1$	$A_2$	$Z$	
$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	0	0	4
1	3	0	-1	0	1	0	0	20
1	1	0	0	-1	0	1	0	10
2	-3	0	0	0	-M	-M	1	0

Dividing  $R_1$  by  $-M$

MOST PIVOT ROW: ←

$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$A_1$	$A_2$	$Z$	
$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	0	0	4
1	3	0	-1	0	1	0	0	20
1	1	0	0	-1	0	1	0	10
$-\frac{2}{M}$	$\frac{3}{M}$	0	0	0	1	1	$-\frac{1}{M}$	0

→ MOST PIVOT COLUMN:

$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$A_1$	$A_2$	$Z$	
$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	0	0	4
1	3	0	-1	0	1	0	0	20
1	1	0	0	-1	0	1	0	10
$-\frac{2}{M}$	$\frac{3}{M}$	0	0	0	1	1	$-\frac{1}{M}$	0

→ MOST PIVOT NUMBER:

$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$A_1$	$A_2$	$Z$	
$\frac{1}{2}$	$\frac{1}{4}$	1	0	0	0	0	0	4
1	3	0	-1	0	1	0	0	20
1	1	0	0	-1	0	1	0	10
$-\frac{2}{M}$	$\frac{3}{M}$	0	0	0	1	1	$-\frac{1}{M}$	0

$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$A_1$	$A_2$	$Z$	
1	$\frac{1}{2}$	2	0	0	0	0	0	8
-1	3	0	-1	0	1	0	0	20
1	1	0	0	<del>0</del>	0	1	0	10
$-\frac{2}{M}$	$\frac{3}{M}$	0	0	0	1	1	$-\frac{1}{M}$	0

by  $(R_1)_2$

	$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$A_1$	$A_2$	$Z$	
$x_1$	1	$\frac{1}{2}$	2	0	0	0	0	0	8
$A_1$	0	$\frac{5}{2}$	-2	-1	0	1	0	0	12
$A_2$	0	$\frac{1}{2}$	-2	0	-1	0	1	0	2
$Z$	0	$\frac{4}{M}$	$\frac{4}{M}$	0	0	1	1	$-\frac{1}{M}$	$\frac{16}{M}$

$$R_2 \rightarrow R_2 - R_1$$

$$R_3 \rightarrow R_3 - R_1$$

$$R_4 \rightarrow \left(\frac{2}{M}\right)R_1 + R_4$$

# ANSWER NO: 3

Minimum cost of transportation =  $40 \times 22 + 80 \times 4 + 10 \times 24 + 30 \times 9 + 30 \times 7 + 50 \times 32 = 3520$

Origin	Destination				Supply	Row Difference					
	1	2	3	4							
1	<del>22</del>	<del>22</del>	17	4	<del>80</del>	13	13	-	-	-	-
2	<del>24</del>	37	9	7	<del>70</del>	2	2	2	17	24	24
3	<del>32</del>	37	20	15	<del>30</del>	5	5	5	17	32	-
Demand	<del>60</del>	<del>40</del>	<del>30</del>	<del>10</del>	240						
Column Difference	4	15	8	3							
	4	-	8	3							
	8	-	11	8							
	8	-	-	8							
	8	-	-	-							
	24	-	-	-							