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SECTION B

SUBJECT. PRCD 1 THEORY

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ASSIGNMENT NO. 3

DEPTMNT. BE[CIVIL] 6TH SEMESTER

QUESTION - 01

Explain in detail types of stirrups with figures and Also explain ACI Codes for Shear design.

Ans:-

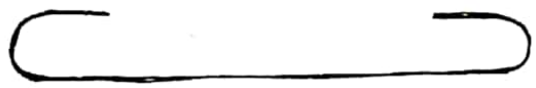
STIRRUP :-

Stirrups are closed-loop bars tied at regular intervals in beam reinforcement to hold the bars in position.

TYPES OF STIRRUPS:-

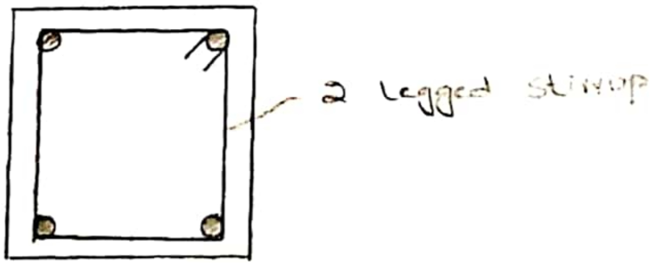
1- Single Legged Stirrup :-

The single-leg stirrups have rarely been used because they are mostly used when binding only two rods.



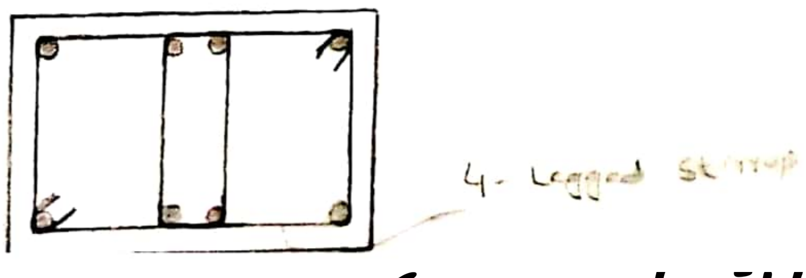
2- Two Legged Stirrup :-

It is most commonly and widely used stirrup. Minimum 4 bars are required for providing this stirrup.

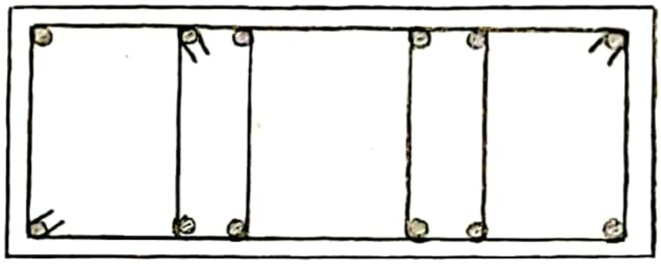


3- Four Legged Stirrup :-

These stirrups are used in case of web reinforcement.



4- Six Legged Stirrup :-



ACI CODES FOR SHEAR DESIGN OF A BEAM

According to ACI-318, following are the formulas used for the shear design of a Beam.

1- Critical Section:- Critical section occurs at 45° and is at distance (d)" from the face of support which is equal to effective depth.

2- Shear Strength Capacity of Concrete is

$$V_c = 2 \times \sqrt{f'_c} \times b_w \times d$$

3- Minimum Web Reinforcement:-

If $V_u \leq \phi V_c$, then theoritically no web reinforcement is required. However ACI Code require provision of atleast a minimum area of web reinforcement equal to,

$\phi = 0.75 \longrightarrow$ For shear design

($\because V_u$ = Total factored shear applied at a given section)

=> For Minimum Reinforcement Area:-

$$A_{v_{min}} = \frac{0.75 \times \sqrt{f'_c} \times b_w \times S}{f_y} \quad \text{or} \quad \frac{50 \times b_w \times S}{f_y} \rightarrow \text{[Higher value is selected]}$$

By interchanging the above formulas, we can obtain the formula for maximum spacing.

$$S_{max} = \frac{A_v \times f_y}{0.75 \times \sqrt{f'_c} \times b_w} \quad \text{or} \quad \frac{A_v \times f_y}{50 \times b_w} \rightarrow \text{[Lesser value is selected]}$$

4- No web-reinforcement is required if

$$V_u < \frac{1}{2}\phi V_c$$

=> Between critical section "V_u" and "ϕV_c", spacing b/w web reinforcement can be find by,

$$S = \frac{\phi \times A_v \times f_y \times d}{V_u - \phi V_c}$$

5- If $V_s \leq 4 \times \sqrt{f'_c} \times b_w \times d$, then max spacing for stirrups will be the smallest of the following.

1- 24"

2- d/2

3- $S_{max} = \dfrac{A_v \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$

4- $S_{max} = \dfrac{A_v \times f_y}{50 \times b_w}$

∵ (V_s = Shear force carried by web reinforcement)

=> If $V_s > 4 \times \sqrt{f'_c} \times b_w \times d$

↓

Max. spacing will be halved

=> If $V_s > 8 \times \sqrt{f'_c} \times b_w \times d$

↓

Then either increase cross-sectional dimensions or increase f'_c.

Question - 02

A simply supported rectangular beam 14" wide having an effective depth of 22" to carry a lateral load of 6.5 k/ft on a 18' simple span. It is reinforced with 7 in^2 of tensile steel area, if f'_c = 4 ksi and f_y = 60 ksi, then design the beam for shear.

Given :-

Breadth of web of beam (b_w) = 14"

Effective depth (d) = 22"

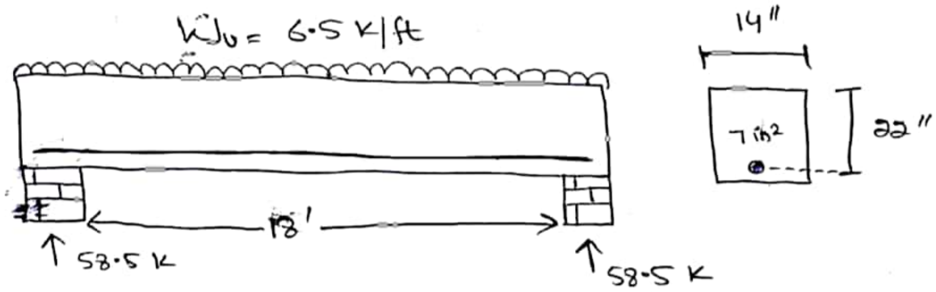
Given Load = 6.5 k/ft

Steel Area = 7 in^2

f'_c = 4 ksi

f_y = 60 ksi

Sol:-



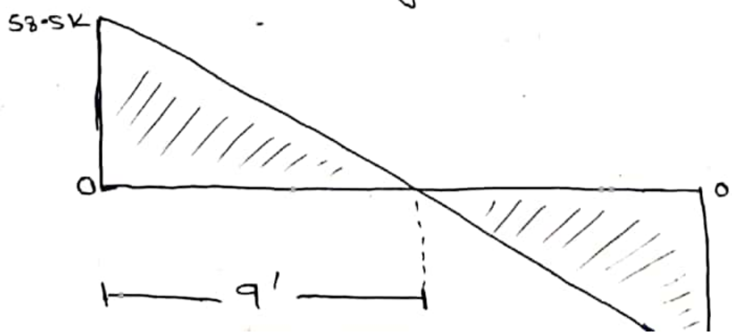
Step #1 :- (Reactions on Supports)

Finding the reactions due to applied load.

Total load = $\frac{6.5 \times 18}{2}$ = 58.5 kips

Step #2 :- (Shear Force Diagram)

The required shear diagram will be.



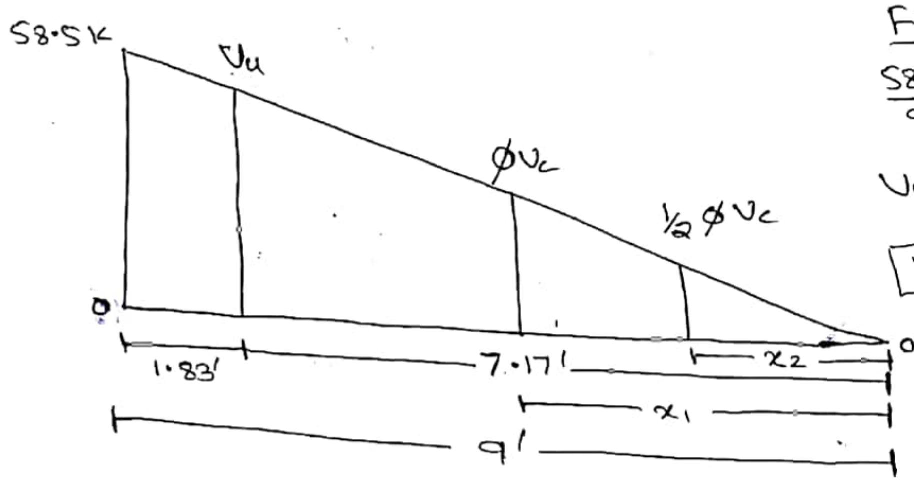
STEP # 3 :-

Finding the value of critical shear "V_u" and its location.

As,

we know that critical shear is located at distance "d" from face of support (d) = 22" = 1.83'

=> we will find the values of critical shear at distance "d" by use of similar triangles.



From Similar Triangles,

$$\frac{58.5}{9} = \frac{V_u}{8.17}$$

$$V_u = \frac{58.5 \times 7.17}{9}$$

$$\boxed{V_u = 46.61 \text{ kips}}$$

STEP # 4 :-

Finding the value of "ϕV_c" and "$\frac{1}{2}\phi V_c$" and also its distances from zero shear to right side.

By formula,

=> $\phi V_c = \phi \times 2 \times \sqrt{f'_c} \times b_w \times d$

$= 0.75 \times 2 \times \sqrt{4000} \times 14 \times 22. \quad = 29219 \text{ lbs}$

$= 29.21 \text{ kips}$

=> Location of ϕV_c by similar triangles,

$$\frac{58.5}{9} = \frac{\phi V_c}{x_1} \quad \Rightarrow \quad \frac{58.5}{9} = \frac{29.21}{x_1}$$

=> $\boxed{x_1 = 4.49'}$

=> Similarly,

$\frac{1}{2}\phi V_c = \phi V_c / 2 \quad \Rightarrow \quad 29.21/2 \quad = 14.60 \text{ kips}$

=> Location of $\frac{1}{2}\phi V_c$ will be,

$\frac{58.5}{9} = \frac{14.60}{x_2} \quad \Rightarrow \quad \boxed{x_2 = 2.24'}$

STEP #5 :-

Finding the value of ϕV_s

By formula, $V_u = \phi V_s + \phi V_c$

$\Rightarrow \phi V_s = V_u - \phi V_c$

$= 46.61 - 29.21$

$\boxed{\phi V_s = 17.4 \text{ kips}}$

STEP #6 :-

Check on Section adequacy,

By formula,

$= \phi \times 8 \times \sqrt{f'_c} \times b_w \times d$

$= 0.75 \times 8 \times \sqrt{4000} \times 14 \times 22 = 116877 \text{ lbs}$

$= 116.87 \text{ kips}$

As $\phi \times 8 \times \sqrt{f'_c} \times b_w \times d > \phi V_s$

So Section is Adequate!

STEP #7 :-

Check on Maximum Spacing for Stirrups,

By formula,

$= \phi \times 4 \times \sqrt{f'_c} \times b_w \times d$

$= 0.75 \times 4 \times \sqrt{4000} \times 14 \times 22 = 58438 \text{ lbs}$

$= 58.43 \text{ kips}$

As $\phi \times 4 \times \sqrt{f'_c} \times b_w \times d > \phi V_s$

So Maximum will be Selected from the following 4 Conditions,

1- $S_{max} = 24''$

2- $d/2 = 22/2 = 11''$

3- $S_{max} = \dfrac{A_v \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$

Here we are using #3 stirrup,

dia $= (3/8)'' = 0.375''$

So

Area $= \frac{\pi}{4}(0.375)^2 = 0.11 \text{ in}^2$

For 2-legged stirrup

$\Rightarrow$ Area $\times 2$

$\Rightarrow 0.11 \times 2 = 0.22 \text{ in}^2$

3- $S_{max} = \dfrac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 14} = 19.87''$

4- $S_{max} = \dfrac{A_v \times f_y}{50 \times b_w} = \dfrac{0.22 \times 60000}{50 \times 14} = 18.85''$

From above 4 conditions, Least value of Spacing for #3, 2 legged stirrup will be Selected as,

$S_{max} = 11''$

STEP # 8 :-

Stirrups spacing from/at critical section will be,
By formula,

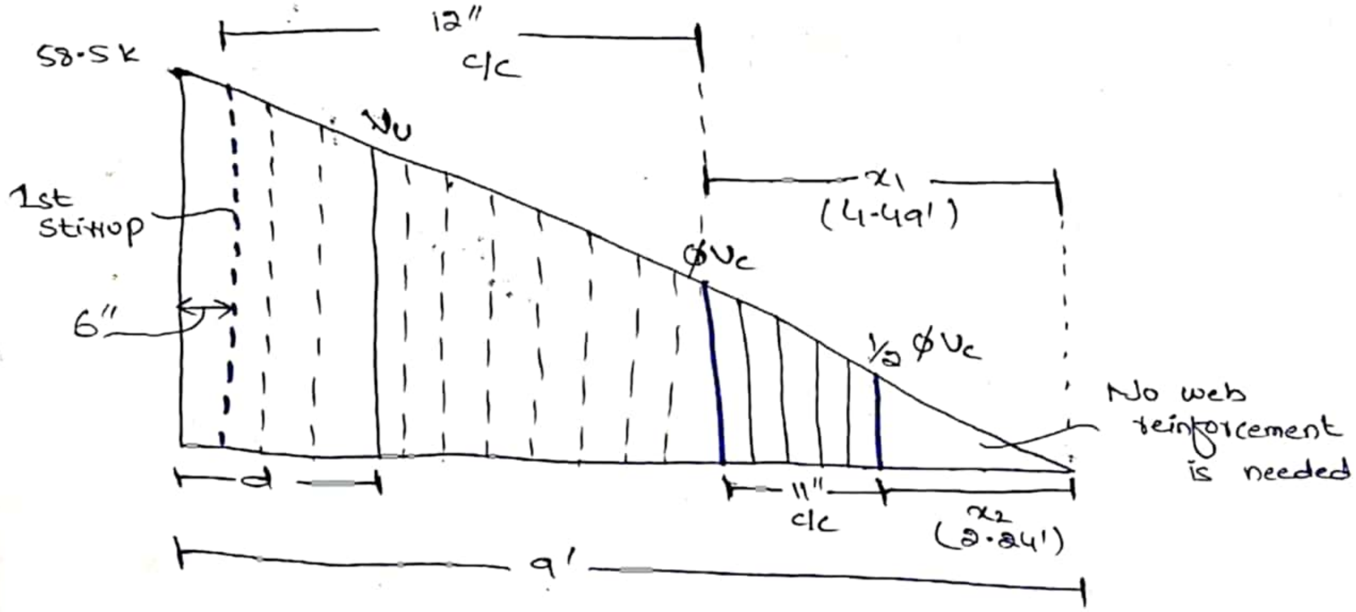
$S = \dfrac{\phi \times A_v \times f_y \times d}{V_u - \phi V_c}$ = 0.75 × 0.22 × 60[redacted] × 22 / (46.61 − 29.21)

$S = 12.5'' \approx 12''$

So 12'' c/c

STEP # 9 :-

Final sketch will be,



As
First stirrup from face of support,

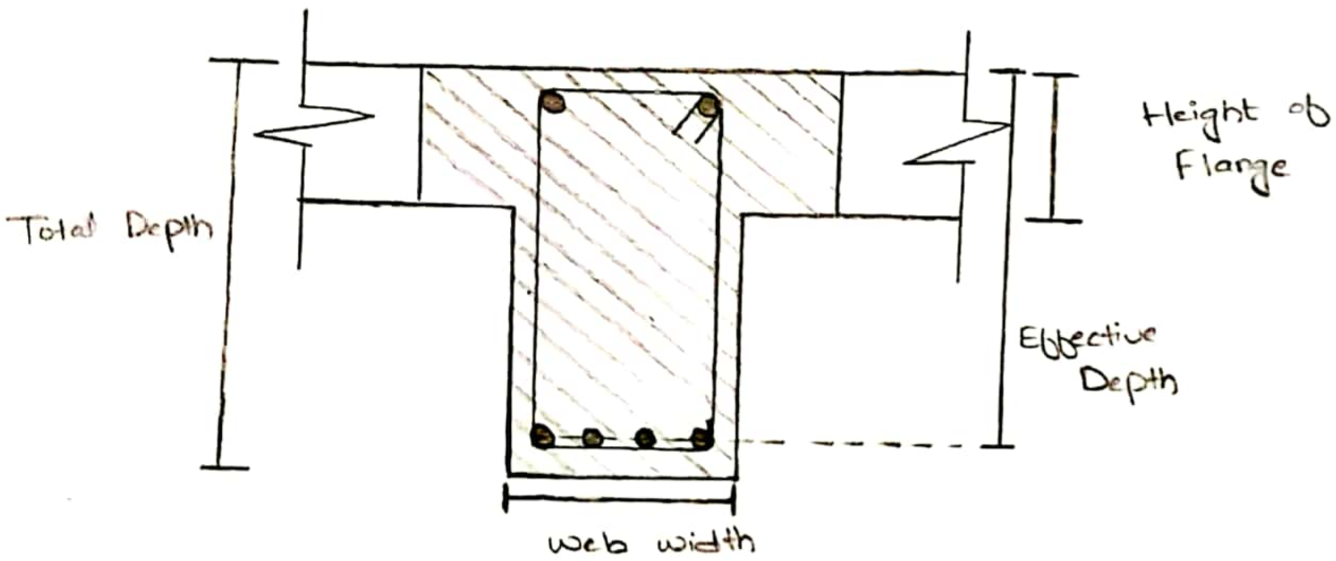
$S/2 = 12/2 = 6''$

QUESTION- 03

Define both the T-Beam and L-Beam with the help of diagram. Also explain flexural analysis of T-Beam.

T- BEAM :-

=> In most of the reinforced concrete structures, Concrete slabs are cast monolithically with the slab So, in this case the beam that act as an intermediate beam are called T- Beams.



=> Because of their T- shape, these beams are Called T- Beams.

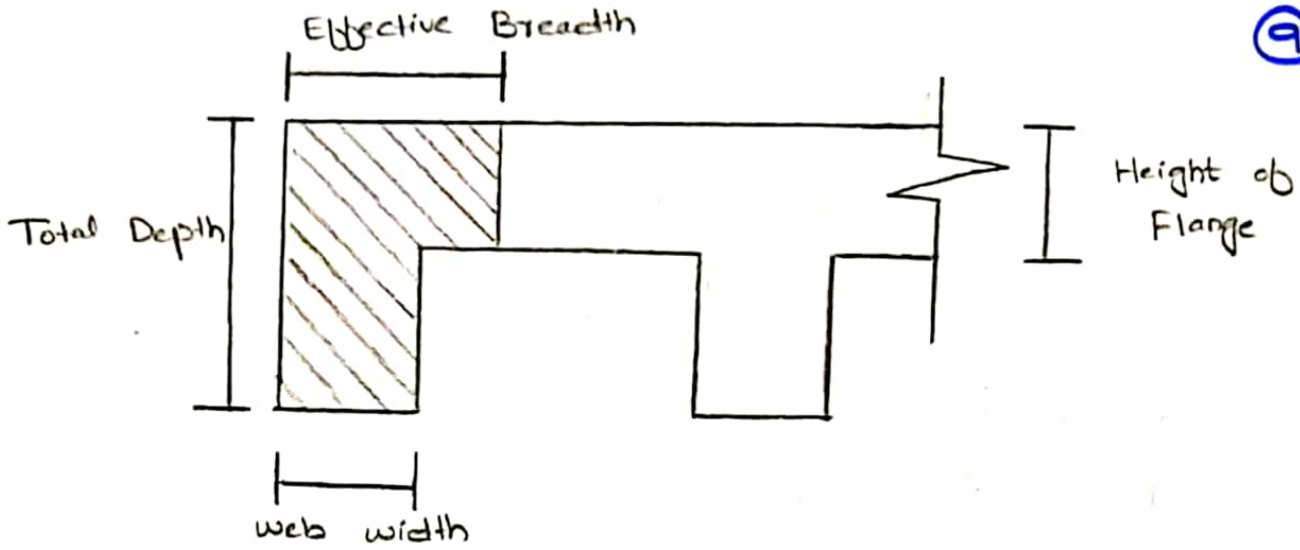
=> It is provided at the Center of the slab to resists the loads.

=> The upper most area of the the beam attached to the slab is called Flange.

=> The bottom rectangular portion of the beam is called web of the beam.

L- BEAM :-

=> L- shaped structure that is in contact with the slab and present at the corner of the floor is called L- Beam.



=> L-Beams are also called Edge Beams.

=> It is always provided at the corners of the slab.

=> L-Beams are typical floor beams because of their reduced overall structural depth, the beams are in Prestressed or reinforced concrete.

FLEXURAL ANALYSIS OF T-BEAM :-

Flexural Analysis of T-Beam consists of the following steps:-

1- For Finding the Ultimate Factored moment, we use the following Formula;

$$M_u = \frac{W_u \times L^2}{8}$$

$\therefore$ (W_u = Total Factored Load, L = Total span of the beam)

2- Effective width (b_e) for T-Beam is Calculated as:-

1- $16(h_f) + b_w$

2- c/c distance

3- span/4

4- $\frac{CTS}{2} + b_w$

$\therefore$ (h_f = height of flange, CTS = Clear transverse span)

- We have to select the least value from above formulas
- If c/c distance is given, then there is no need of "$\frac{CTS}{2} + b_w$"

3 - Checking whether Rectangular or T-Beam Analysis is required

i - If $a > h_f \rightarrow$ Special Analysis is required

ii - If $a < h_f \rightarrow$ Rectangular beam Analysis is required

where

(a = Depth of Compression block
h_f = Height of flange)

4 - For Finding Area of Steel, we have to use

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

where

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b_w}$$

∵ (ϕ = strength Reduction factor
d = Effective depth
a = Compression block depth
b_w = web width of beam)

5 - For checking the range of Reinforcement Ratio,

$$\rho_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left(\frac{\varepsilon_u}{\varepsilon_u + \varepsilon_y}\right)$$

$$\rho_{min} = \frac{200}{f_y}$$

$$\rho = \frac{A_{st}}{b \times d}$$

6 - Formula for Finding No. of bars required is,

$$\text{No. of bars} = \frac{\text{Area of steel}}{\text{Area of single bar}}$$

7 - For checking Minimum width for bars accomodation,

$$b_{min} = 2(\text{clear cover}) + 2(\text{dia of stirrup}) + \text{No. of bars}(\text{dia of bar}) + \text{Spacing b/w bars}(\text{dia of bar})$$

8 - Design Moment is given by,

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2) \rightarrow \text{if } a < h_f$$

$$M_d = \phi \times [A_s \times f_y \times (d - h_f/2) + (A_s - A_{st}) + f_y \times (d - a/2)] \rightarrow \text{if } a > h_f$$

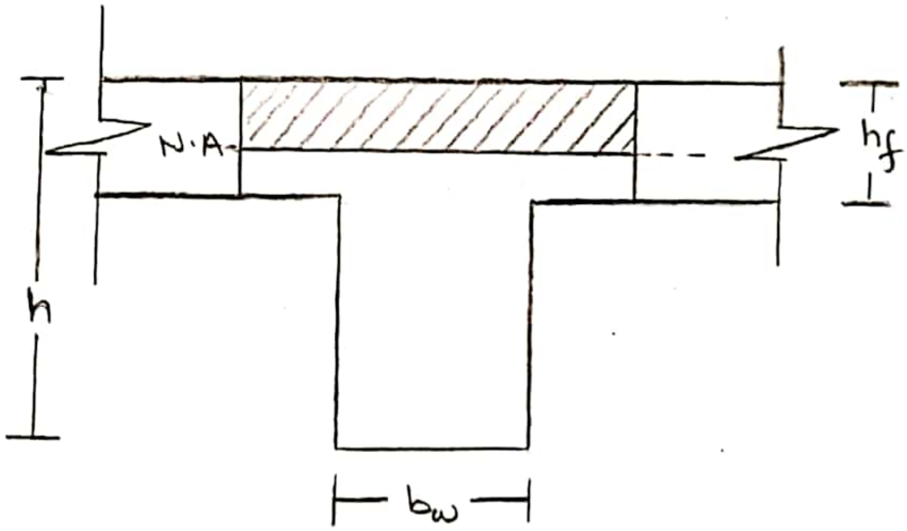
QUESTION - 04

What is the difference b/w. CASE-1 and CASE-2 in the design of T-Beam?

CASE-I :-

From the figure

$a < h_f$



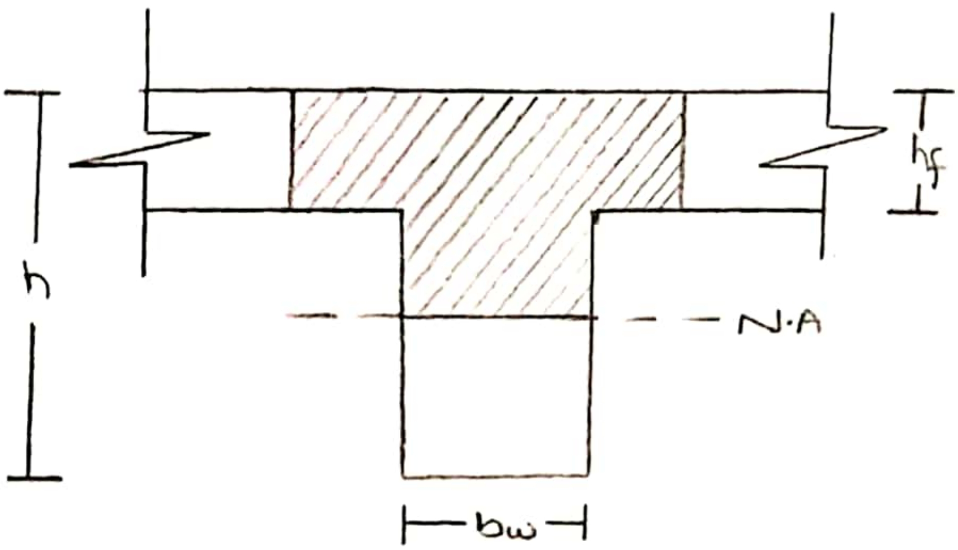
So in this case, Rectangular Beam Analysis is Required.
So,
The Design Moment formula will be

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2)$$

CASE - II :-

From the figure,

$a > h_f$



So in this, Special beam analysis i.e, T-Beam Analysis is required.

So
the required Design Moment will be,

$$M_d = \phi \times \left[A_s \times f_y \times \left(d - \frac{h_f}{2}\right) + (A_s - A_{st}) + f_y \times (d - a/2) \right]$$

QUESTION - 05

A floor system consists of 3.5" concrete slab supported by 16' simple span spaced at 9' c/c, the beam having a web width of 10" and effective depth of 18" and total height is 23". Calculate the necessary flexural reinforcement if the factored applied moment is 5800 kip-inch. Use f'_c = 3 ksi and f_y = 60 ksi

Given :-

Height of flange (h_f) = 3.5"

c/c distance = 9'

Length / span of the beam = 16'

web width (b_w) = 10"

Effective depth (d) = 18"

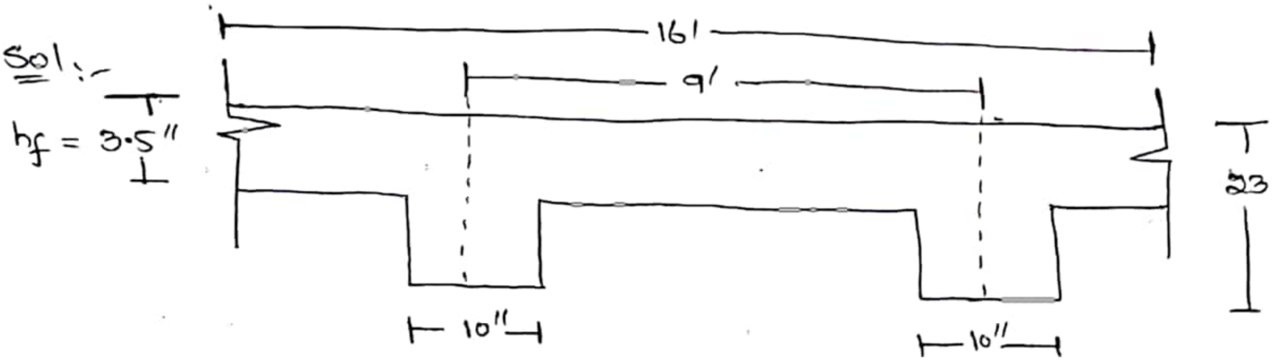
Height (h) = 23"

Total factored moment (M_u) = 5800 kip-inch

f'_c = 3 ksi

f_y = 60 ksi

Sol :-



STEP #1 :-

Calculate the effective width (b_e) for T- beam.

1- $16(h_f) + b_w$ = $16(3.5) + 10$ = 66"

2- c/c distance = 9×12 = 108"

3- Span/4 = $\frac{16}{4} \times 12$ = 48"

Selecting the least value of b_e as,

$$b_e = 48"$$

STEP #2 :-

Check whether Rectangular or T-beam Analysis is required.

Trial # 01 :- Let $a = h_f = 3.5''$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{5800}{0.90 \times 60 \times (18 - 3.5/2)} = 6.61 \text{ in}^2$$

Trial # 02 :-

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b_e}$$

$$a = \frac{6.61 \times 60}{0.85 \times 3 \times 48} = 3.2''$$

$\Rightarrow 3.2'' < 3.5''$

and $\boxed{A_{st} = 6.55 \text{ in}^2}$

So Rectangular Beam Design is Required !

Trial # 03 :- $a = 3.21''$

and $$A_{st} = \frac{5800}{0.90 \times 60 (18 - \frac{3.21}{2})} = \boxed{6.55 \text{ in}^2}$$

So Area of steel is 6.55 in^2.

STEP # 3 :-

Check ρ_{max} and ρ_{min}.

$$\Rightarrow \rho_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \left(\frac{\varepsilon_u}{\varepsilon_u + \varepsilon_t}\right)$$

$$= 0.85 \times 0.85 \times \frac{3}{60} \left(\frac{0.003}{0.003 + 0.005}\right) = 0.013$$

$$\Rightarrow \rho_{min} = \frac{200}{f_y} = \frac{200}{60000} = 0.003$$

$$\Rightarrow \rho = \frac{A_{st}}{b \times d} = \frac{6.55}{10 \times 18} = 0.036$$

$\rho_{min} < \rho < \rho_{max}$

$0.003 < 0.036 < 0.013$

As the value of ρ_{max} is less than ρ, So we have to design it as "Doubly Reinforced Beam."

=> First we have to find the Area of steel against ρ_{max}.

$$\rho_{max} = \frac{Ast}{b \times d} \Rightarrow Ast = \rho_{max} \times (b \times d)$$

$$Ast = 0.013 \times (10 \times 18)$$

$$\therefore \boxed{Ast = 2.34 \text{ in}^2}$$

STEP # 4:-

Finding the value of Mu_2:-

By formula,

$$Mu_2 = \phi \times Ast \times fy \times (d - a/2)$$

First Finding the value of "a"

$$\Rightarrow a = \frac{Ast \times fy}{0.85 \times f'_c \times b} = \frac{2.43 \times 60}{0.85 \times 3 \times 10}$$

$$a = 5.72''$$

$$\Rightarrow Mu_2 = 0.90 \times 2.43 \times 60 \times (18 - 5.72/2)$$

$$\boxed{Mu_2 = 1986.67 \text{ kip-inch}}$$

As $Mu_2 < Mu$

$1986.67 < 5800$

So we have to design the beam in such away that it can resist more bending moment than the applied external moment.

STEP # 5 :-

Finding Difference in moments and Area of steel.

$M_{u1} = M_u - M_{u2}$

$= 5800 - 1986.67$

$M_{u1} = 3813.33$ kip-inch

By formula,

$$A'_{st} = \frac{M_u}{\phi \times f_y \times (d-d')} = \frac{3813.33}{0.90 \times 60 \times (18-2.5)}$$

$A'_{st} = 4.56 \text{ in}^2$

STEP #6 :-

Finding Total Steel Area.

$A_s = A_{st} + A'_{st}$

$= 2.43 + 4.56 \quad = 6.99 \text{ in}^2$

STEP #7 :-

Selection of Bar:-

In Tension Zone :-

Let we use # 8 bar

dia = (8/8) = 1" , Area $= \frac{\pi}{4}(1)^2 = 0.785 \text{ in}^2$

By formula

$$\text{No. of bars} = \frac{\text{Area of Steel}}{\text{Area of single bar}} = \frac{6.99}{0.785} = 8.9 \cong 9$$

So 9 #8 bars

In Compression Zone :-

Let we use # 7 bar

dia = (7/8)" , Area $= \frac{\pi}{4}(7/8)^2 = 0.601 \text{ in}^2$

By formula:

$$\text{No. of bars} = \frac{\text{Area of Steel}}{\text{Area of single bar}} = \frac{4.56}{0.601} = 7.5 \approx 8$$

So 8 #7 bars

STEP # 8 :-

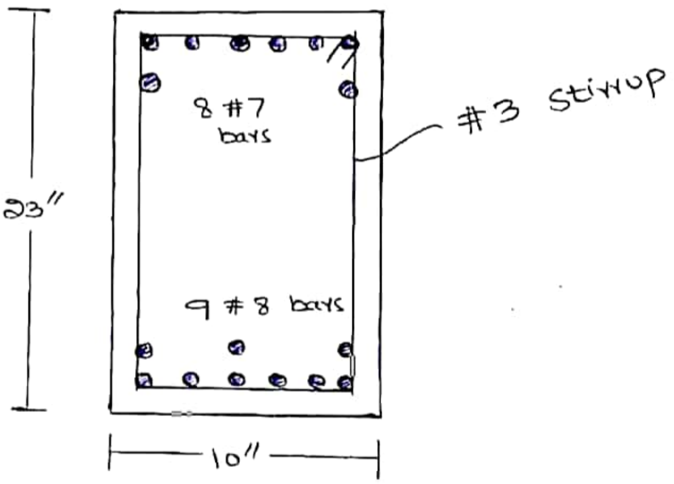
Minimum width for Accomodation of bars.

$$b_{min} = (2 \times 1.5) + (2 \times 3/8) + 9(8/8) + 8(8/8)$$

$$= 20.75''$$

As $20.75'' > 10''$

So, the bars will be placed in multiple Layers.



Effective depth $(d) = 23 - 1.5 + \frac{3}{8} + \frac{8}{8} + \frac{1}{2}(\frac{8}{8}) = 19.6''$

Effective Cover $(d') = 1.5 + \frac{3}{8} + \frac{7}{8} + \frac{1}{2}(\frac{7}{8}) = 3.18''$

STEP # 9 :-

Finding the Design Moment.

$$M_d = \phi\left[A's \times f_y \times (d - d') + (A_{st} - A'_{st}) \times f_y \times (d - a/2)\right]$$

First $a = \frac{(A_s - A'_{st}) \times f_y}{0.85 \times f'_c \times b} = \frac{(9 \times 0.785 - 8 \times 0.601) \times 60}{0.85 \times 3 \times 10} = 5.31''$

$$\Rightarrow M_d = 0.90\left[(8 \times 0.601) \times 60 \times (19.6 - 3.18) + (9 \times 0.785 - 8 \times 0.601) \times 60 \times \left(19.6 - \frac{5.31}{2}\right)\right]$$

$$\boxed{M_d = 6328.38}$$

As $6328.38 > 5800 \rightarrow$ So design is OK!

QUESTION - 06

A beam is revised to developed and ultimate moment of 6000 kip-inches limited to 14 x 26 inch size, use $f'_c = 4$ ksi and $f_y = 60$ ksi. Determine flexural reinforcement assume two rows of tensile reinforcement and effective depth of beam is 22 inches.

Sol:-

Given :-

Breadth (b) = 14"

Height (h) = 26"

Concrete Compression strength (f'_c) = 4 ksi

Steel Tensile strength (f_y) = 60 ksi

Ultimate Factored Moment (M_u) = 6000 kip-inches

Effective depth of beam (d) = 22"

Assume Effective Cover (d') = 2.5"

STEP #1 (Reinforcement Ratio)

By formula,

$$\rho_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left(\frac{\varepsilon_u}{\varepsilon_u + \varepsilon_y}\right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \times \left(\frac{0.003}{0.003 + 0.005}\right)$$

$$\boxed{\rho_{max} = 0.0180}$$

STEP #2 :- (Area of Steel)

As we know that,

$$\rho_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = \rho_{max} \times (b \times d)$$

$$\Rightarrow A_{st} = 0.0180 \times (14 \times 22) = \boxed{5.54 \text{ in}^2}$$

Step # 3 :- (Design Moment) :-

By Using formula

$$M_{u_2} = \phi \times A_{st} \times f_y \times (d - a/2)$$

$$\Rightarrow a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{5.54 \times 60}{0.85 \times 4 \times 14} = \boxed{6.98''}$$

So,

$$M_{u_2} = 0.90 \times 5.54 \times 60 \times \left(22 - \frac{6.98}{2}\right)$$

$$= 5537.4 \text{ kip-inch}$$

As,

$$5537.4 < 6000$$

So we have to design a Section as doubly reinforced.

Step # 4 :- (Difference In Moments)

$$M_{u_1} = M_u - M_{u_2}$$

$$= 6000 - 5537.4$$

$$\boxed{M_{u_1} = 462.6 \text{ kip-inches}}$$

Step # 5 :- (Area of Steel)

$$M_{u_1} = \phi \times A'_{st} \times f_y \times (d - d')$$

So Area of steel in Compression Zone will be,

$$\Rightarrow A'_{st} = \frac{M_{u_1}}{\phi \times f_y \times (d - d')} = \frac{462.6}{0.90 \times 60 \times (22 - 2.5)}$$

$$\Rightarrow \boxed{A'_{st} = 0.44 \text{ in}^2}$$

STEP # 6 :- (TOTAL Steel Area)

$A_s = A_{st} + A'_{st}$

$= 5.54 + 0.44 = 5.98\ in^2$

STEP # 7 :- (Selection & No. of bars Used)

1 - Steel in Tension Zone :-

we use # 7 bar,

dia = $(7/8)'' = 0.875''$, Area = $\frac{\pi}{4}(0.875)^2$

$= 0.601\ in^2$

So,

No. of bars $= \dfrac{A_{st}}{\text{Area of single bar}}$

$= \dfrac{5.98}{0.601} = 9.9 \simeq 10$ bars

So 10 #7 bars.

2 - Steel in Compression Zone :-

we use # 5 bar,

dia = $(5/8)'' = 0.625''$, Area = $\frac{\pi}{4}(0.625)^2$

$= 0.306\ in^2$

So,

No. of bars = $\dfrac{A'_{st}}{\text{Area of single bar}}$

$= \dfrac{0.44}{0.306} = 1.43 \simeq 2$ bars

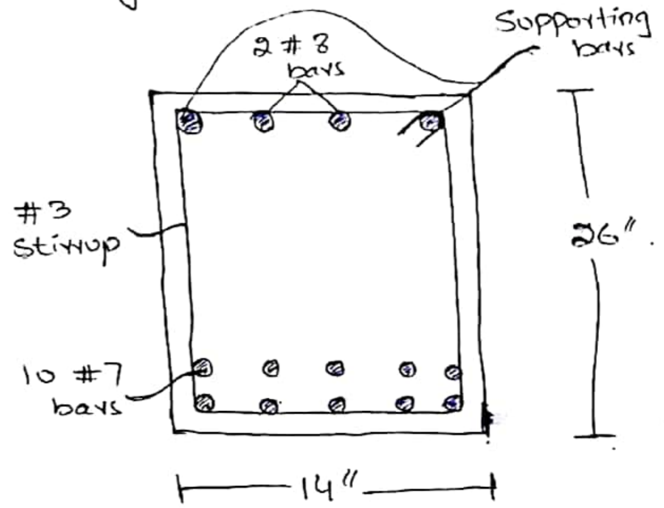
So 2 # 5 bars

STEP # 8 :- (Minimum Width of Beam)

$b_{min} = 2(1.5) + 2(3/8) + 10(7/8) + 9(7/8)$

$b_{min} = 20.37 > 14''$

So not good in one Layer.



Now,

=> Effective depth $(d) = 26 - 1.5 - 3/8 - 7/8 - 1/2(7/8)$

$= 22.82''$

=> Effective Cover $(d') = 1.5 + 3/8 + 1/2(5/8)$

$= 2.18''$

STEP # 9 :- (Design Moment)

$$M_d = \phi \times [A'_{st} \times f_y \times (d - d') + (A_{st} - A'_{st}) \times f_y \times (d - a/2)]$$

$$a = \frac{(A_{st} - A_{st}') \times f_y}{0.85 \times f'_c \times b}$$

$$= \frac{(10 \times 0.601 - 2 \times 0.306) \times 60}{0.85 \times 4 \times 14} = 6.80''.$$

$$M_d = 0.90[(2 \times 0.306) \times 60 \times (22.82 - 2.18) + (10 \times 0.601 - 2 \times 0.306) \times 60 \times (22.82 - 6.80/2)]$$

$M_d = 7047.6$ kip - inches

As $7047.6 > 6000$

Design is OK!