

~~3~~ 3

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \frac{1}{57,500} \begin{bmatrix} 350,000 & -125,000 \\ -400,000 & +225,000 \end{bmatrix}$$

$$= \begin{bmatrix} 225,000 \\ -175,000 \end{bmatrix}$$

$$= x_1 = 225,000, \quad x_2 = 175,000$$

$$\text{Total Cost} = x_1 + x_2 = 400,000$$

3 4

Q 3 Answer:

Answer:

A vector space is a collection of objects called vectors, which may be added together and multiplied by numbers. Scalars are often taken to be real numbers, but there are also vector spaces with scalar multiplications by complex numbers, rational numbers or generally any field.

$$a) \text{ Sol}^n: k \begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} ka & kb \\ kc & kd \end{pmatrix}$$

For $k \in \mathbb{R}$.

According to the definition of vector space if any scalar multiplied by vector space then it will become vector space.

So in this case

$k \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ is not vector space





Q NO 48

ANSWERS

a) Let $m = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ 2×2 .

inverse
 $m^{-1} = \frac{1}{\det m} = \begin{bmatrix} d & -b \\ -c & a \end{bmatrix} = \frac{1}{da - bc}$

entries a and d for matrix m
 interchanged

Put $-$ ive in front of b and c

b) $\begin{pmatrix} 3 & 4 \\ 2 & 3 \end{pmatrix} = 9 - 8 = 1$

c) $\begin{pmatrix} 2 & 2 \\ 3 & 3 \end{pmatrix} = 6 - 6 = 0$

d) $A = \begin{vmatrix} 1 & 1 & 1 \\ 5 & 9 & 5 \\ 7 & 1 & 5 \end{vmatrix}$

$1 \cdot 9 \cdot 5 + 1 \cdot 5 \cdot 7 + 1 \cdot 9 \cdot 7 - 1 \cdot 9 \cdot 7 - 1 \cdot 5 \cdot 1$

$= 45 + 35 + 5 - 63 - 5$

$= 45 + 35 + 5 - 63 - 5 = 90 - 88 =$

2 Answer

$$\begin{pmatrix} ka & b \\ kc & d \end{pmatrix} = 6 \begin{pmatrix} ka & kb \\ kc & kd \end{pmatrix}$$

b) solⁿ:

Let $P(x) = a_3x^3 + a_2x^2 + a_1x + c$ which is defined and correct according to def. of vector space.



1

DATE: _____

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Q No 1 :

ANSWER :

$$\text{For } \mathbb{R}^3, v_1 \times v_2 \times v_3 = \begin{pmatrix} 1 \\ 5 \\ 9 \end{pmatrix} \cdot \begin{pmatrix} 5 \\ 9 \\ 7 \end{pmatrix} \cdot \begin{pmatrix} 9 \\ 7 \\ 5 \end{pmatrix}$$

$$= 1D_1 (5, 9, 7) + 1D_2 (5, 9, 7) + 1D_3 (5, 5, 7)$$

= The desired candidates for \mathbb{R}_2 is

$(1, 5, 5, 9, 5)$

Similarly $(1, 9, 5, 9, 9)$

and $(1, 7, 5, 7, 9, 7)$

$$\text{So } A = \begin{bmatrix} 1.5 & 1.9 & 1.7 \\ 5.5 & 5.9 & 5.7 \\ 9.5 & 9.9 & 9.7 \end{bmatrix}$$



So you can see each column of above \mathbb{R}_2 vectors are linear dependent.

2

~~90-88~~~~* 2 Answer~~

Q NO 2 :

ANSWER :

In matrix form we can write it as :

$$450 \times 1 + 25 \times 2 = 1000.$$

$$400 \times 1 + 350 \times 2 = 500$$

$$\begin{bmatrix} 450 & 250 \\ 400 & 350 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 1000 \\ 500 \end{bmatrix}$$

$$A \quad X \quad B$$

$$X = A^{-1} B$$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 450 & 250 \\ 400 & 350 \end{bmatrix}^{-1} \begin{bmatrix} 1000 \\ 500 \end{bmatrix}$$

$$\text{adj}(A) = \begin{bmatrix} 300 & -250 \\ -400 & 450 \end{bmatrix} \quad |A| = \begin{bmatrix} 450 & 250 \\ 400 & 350 \end{bmatrix}$$

$$|A| = (450)(350) - (250)(400) \\ = 157,500 - 100,000 = 57,500$$

$$= \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \frac{1}{57,500} \begin{bmatrix} 350 & -250 \\ -400 & 450 \end{bmatrix} \begin{bmatrix} 1000 \\ 500 \end{bmatrix}$$



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ANSWERS

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