

Name " Mazhar-hayat

ID " 7819

Section " "A"

Subject " Hydraulic-engineering

Submitted to " Fawad Ahmad

Semester " 6th

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Q No # 01

Ans Solution:-

The pressure drop ΔP is expected to depend upon gate opening h , the overall depth d , the velocity V , density ρ and viscosity μ .

List the relevant variables.

$\Delta P, h, d, V, \rho, \mu$

write down dimension

$$\Delta P \quad ML^{-1}T^{-2}$$

$$h \quad L$$

$$d \quad L$$

$$V \quad LT^{-1}$$

$$\rho \quad ML^{-3}$$

$$\mu \quad ML^{-1}T^{-1}$$

Number of variable $n = 6$

Number of dimensions: $m = 3$ (M, L and T)

Number of non-dimensional group: $n - m = 3$

Choose $m (=3)$ scaling variables:

geometric (d); Kinematic / time-dependent (V)

dynamic (mass-dependent (ρ)).

(2)

from dimensionless group by non-dimension groups by non-dim the remaining variable: Δp , h and M

$$\bar{\pi}_1 = \Delta p d^a v^b \rho^c$$

$$M^0 L^0 T^0 = (ML^{-1}T^{-2})(L)^a (LT^{-1})^b (ML^{-3})^c \\ = M^{1+c} L^{-1+a+b-3c} T^{-2-b}$$

$$M: 0 = 1+c \quad c = -1$$

$$T: 0 = -2-b \quad b = -2$$

$$L: 0 = -1+a+b-3c \Rightarrow a = 1+3c-b=0$$

$$\Rightarrow \bar{\pi}_1 = \Delta p v^{-2} \rho^{-1} = \frac{\Delta p}{\rho v^2}$$

$$\bar{\pi}_2 = h/d \quad (\text{by inspection, since } h \text{ is length})$$

$$\bar{\pi}_3 = M d^a v^b \rho^c \quad (\text{probably obvious by now, but here goes away})$$

$$M^0 L^0 T^0 = (ML^{-1}T^{-1})^a (LT^{-1})^b (ML^{-3})^c \\ = M^{1+c} L^{-1+a+b-3c} T^{-1-b}$$

$$M: 0 = 1+c \Rightarrow c = -1$$

$$T: 0 = -1-b+0 \Rightarrow b = -1$$

$$L: 0 = -1+a+b-3c \Rightarrow a = -1+3c-b = -1$$

$$\Rightarrow \bar{\pi}_3 = M d^{-1} v^{-1} \rho^{-1} \quad (\text{probably obvious})$$

3

$$M^0 L^0 T^0 = (ML^{-1}T^{-1})(L^a)^9(LT^{-1})^3(ML^{-3})^2 \\ = M^{1+c} L^{-1+9+6-3c} T^{-1-b}$$

$$M; \quad 0 = 1+c \quad c = -1$$

$$T; \quad 0 = -1-b+0 \quad b = -1$$

$$L; \quad 0 = -1+9+6-3c \Rightarrow a = 1+3c-b = -1$$

$$\Rightarrow \pi_3 = M d^{-1} v^{-1} \rho^{-1} = \frac{M}{\rho v d}$$

Recognition of the Reynold number
~~strength~~ suggests that we replace
 π_3 by

$$\pi_3 = (\pi_3)^{-1} = \frac{\rho v d}{M}$$

Hence, dimensional analysis yields

$$\pi_1 = f(\pi_2, \pi_3)$$

i.e.

$$\frac{\Delta P}{\rho v^2} = f\left(\frac{h}{d}, \frac{\rho v d}{M}\right)$$

(a) Dynamic similarity required that all non-dimensional groups be the same in model and prototype

$$\pi_1 = \left[\frac{\Delta P}{\rho v^2} \right]_p = \left[\frac{\Delta P}{\rho v^2} \right]_m$$

(4)

$$\pi_2 = \left[\frac{h}{d} \right]_p = \left[\frac{h}{d} \right]_m \quad (\text{atometric})$$

(atometric if similar shape i.e. "geometric similarity")

$$\pi_3 = \left[\frac{\rho v d}{M} \right]_p = \left[\frac{\rho v d}{M} \right]_m$$

From the last, we have a velocity ratio

$$\frac{V_p}{V_m} = \frac{(\rho/M)_p}{(\rho/M)_m} \frac{d_m}{d_p} = \frac{0.002/8000}{1.0 \times 10^{-6}} = 0.5$$

Hence:

$$V_m = \frac{V_p}{0.5} = \frac{3.0}{0.5} = 6.0 \text{ ms}^{-1}$$

(b) The ratio of the quantities of flow is

$$\frac{Q_p}{Q_m} = \frac{(\text{velocity} \times \text{area})_p}{(\text{velocity} \times \text{area})_m} = \frac{V_p}{V_m} \left(\frac{d_p}{d_m} \right)^2 = 0.5 \times 5^2 = 12.5$$

(c) Finally, for the pressure drop.

$$\pi_1 = \left[\frac{\Delta p}{\rho v^2} \right]_p = \left[\frac{\Delta p}{\rho v^2} \right]_m \Rightarrow \frac{(\Delta p)_p}{(\Delta p)_m} =$$

(5)

$$\frac{\rho_p}{\rho_m} \left[\frac{v_p}{v_m} \right]^2 = \frac{800}{1000} \times 0.5^2 = 0.2$$

Hence :-

$$\Delta p_p = 0.2 \times \Delta p_m = 0.2 \times 60 = 12.0 \text{ kPa}$$

(6)

Q No 11 of 02

Ans

Given data:-

Maximum depth $H_w = 78$
Specific gravity of dam $G = 2.8$
Compression stress $= 781 \text{ T/m}^2$
Height of wave $= 3.8 \text{ m}$
 $C_u = 0$

(1) Limiting:-

σ_{all}

$$\frac{W_w(G - C_u + 1)}{1000(2.8 - 0 + 1)}$$
$$= \frac{781 \times 1000}{1000(2.8 - 0 + 1)} = 205.5778$$

So it is low gravity dam

(2) Top width "a":-

$$\text{Free board} = 1.5 \times 3.8$$
$$= 5.7 \text{ m}$$

$$\text{Height of dam} = H_D = H_w + \text{F.B.}$$
$$= 78 + 5.7$$

$$H_D = 83.7 \text{ m}$$

$$a = 14\% \text{ of } H_D$$

$$a = 0.14 \times 83.7 = 11.718 \text{ m}$$

(7)

(3) Base width "b" (without offset)

For No sliding Criteria

$$b^* = \frac{H \cdot w}{U \& t} = \frac{78}{0.7 \times 2.8}$$

$$= 39.79 \text{ m} \approx \text{2100} \text{ 40 m}$$

Maximum depth $H_w = 78$

ii) For No tension Criteria

$$b' = \frac{H_w}{\sqrt{4}} = \frac{78}{\sqrt{2.8}} = 47$$

(4) Depth of vertical portion on U/s side

$$h' = 2.9 \sqrt{C_2 - C_1}$$

$$= 2 \times 11.7 \sqrt{2.8 - 0}$$

$$h' = 39.15 \text{ m}$$

(5) Up stream offset = $a/16$

$$= \frac{11.7}{16} = 0.73 \text{ m}$$

(6) depth below water level to end of inclined portion in US =

$$US = 3.14 a \sqrt{G}$$

$$= 3.14 \times 11.7 \times \sqrt{2.8}$$

(8)

$$= 61.56 \text{ m}$$

(7) Total width of base of dam

$$b = b' + \frac{a}{16}$$
$$= 47 + \frac{11.7}{16} = 47.7 \text{ m}$$

$$(8) \tan \theta = \frac{b'}{H} = \frac{47}{78} = 31.07$$

$$9) \tan \theta = \frac{a}{d'} = \frac{11.7}{d'} \quad \tan \theta = \frac{11.7}{d}$$

$$\frac{47}{78} d' = 11.7 = d' = \frac{11.7 \times 78}{47}$$

~~$d' = 19.3 \text{ m}$~~ depth of vertical portion
 ~~$d - d' + FB = 19.3$~~

$$d' = 46 \text{ m}$$

depth of vertical portion

$$d - d' + FB = 46 + 6.3$$

$$d = 52.3 \text{ m}$$

9

Q No# 04

Particle diameter :-

The diameter of the particle is directly proportional to the fall velocity because greater the size of particle so it will tend to move faster as compared to the particle of small size thus there will be more gravitational force on particle of greater size so it will fall quickly due to its weight

Particle density :-

density of the particle is directly proportion to the rate of fall velocity since particle ~~down~~ early with high density tends to settle down early compared with particle of density

(10)

Particle concentration:-

concentration of particle size will have considerable effect on its fall velocity as the section having greater concentration will be settled down at the place thus causing the more fall velocity comparing with section of low concentration.

Particle shape:-

Particles having regular shape tend to be affected more than irregular shape. Since regular shaped particles have less surface area which offer very little or no friction while friction is as the particle with smaller surface area are more likely to be affected due to their less resistance.

Viscosity of water:-

\propto Fluid velocity
Through porous media is approximated as inversely proportional to the

(11)

Kinematic viscosity. A decrease in viscosity therefore increase the velocity of a compound through porous media.

Turbulence of water:-

Turbulence of water effect the fall velocity of water in reservoir because the non linearity \Rightarrow zig zag path effect the flow of water \Rightarrow cause the variation in the flow

QNo# 03

Dimensional ANALYSIS

Dimensional analysis is a mathematical technique making use of study of dimension.

its deal with the dimension of physical quantities involved in the phenomenon.

(12)

In dimensional analysis, one first predict the physical parameter that will influence the flow and then by grouping these ~~para~~ ~~the~~ parameter that with in dimensionless combinations a better understanding of the flow phenomenon is made possible.

Type of dimensions

- Fundamental dimension or Fundamental Quantities
- Secondary Dimension or Derived Quantities

Fundamental dimension

These are basic quantities

- Time, T → Time, T
- Distance, L → Distance, L
- Mass, M → Force, F

(13)

$$\text{Force} = \text{Mass} \times \text{Acceleration} = MLT^{-2}$$

Second dimensions :-

They are those quantities which possess more than one fundamental dimensions.

For example:

- Velocity = distance per unit time L/T

Methodology of Dimensional Analysis

The basic principle is dimensional homogeneity which means the dimension of each term in an equation on both side are equal

Dimensional Homogeneous Equation:
Such equations are independent of system of unit for example
lets consider the equation

$$V = (2gH)^{1/2}$$

- Dimension of LHS = $V = L/T = LT^{-1}$

(14)

- Dimensions of LHS = $V = L/T = LT^{-1}$
- Dimension of RHS = $(\rho g h)^{1/2} = L/T$

Similitude Analysis:-

~~It is defined as simi~~
It is a concept used in testing of engineering models.

Usually it is impossible to obtain a pure theoretical solution of hydraulic phenomenon.

The for experimental investigation are often performed on small scale models, called Model analysis.

A few example where model may be used are ship in towing basin, air planes in wind tunnel, etc and to study such phenomenon as the action of wave.

(15)

of wave and tides on
beaches, soil erosion and
transportation of sediment etc