

Note: Please attempt all Questions in sequence. All questions carry equal marks.

(50)

Q1: Construct a grouped distribution table for the following data and Calculate Mean, Mode Median and Quartiles.

423, 369, 387, 411, 393, 394, 371, 377, 389, 409, 392, 408, 431, 401, 363, 391, 405, 382, 400, 381, 399, 415, 428, 422, 396, 372, 410, 419, 386, 390

Mo Tu We Th Fr Sa Su

DATE: _____

Class	freq	Mid Point	C.F	C.B	$\bar{x} = \frac{\sum fx}{\sum f}$
360-374	4	367	4	359.5 - 374.5	1468
375-389	6	382	10	374.5 - 389.5	2292
390-404	9	397	19	389.5 - 404.5	3573
405-419	7	412	26	404.5 - 419.5	2884
420-434	4	427	30	419.5 - 434.5	1708
					11925

$n=30$

- Mean = $\frac{\sum fx}{\sum f} \Rightarrow \frac{11925}{30}$
mean = 397.5
- median = $L + \left(\frac{\frac{n}{2} - cf}{f} \right) h$
To find median class
= value of $\left(\frac{n}{2} \right)$ observation.
= $\frac{30}{2} \Rightarrow 15$
From the column of cf, we find that the 15th observation lies in class 390-404
 \therefore The median class is 389.5 - 404.5

Put in eq 1

$$m = L + \left(\frac{\frac{n}{2} - cf}{f} \right) \cdot h$$

where $L = 389.5$

$$n = 30$$

$$cf = 10$$

$$f = 9$$

$$h = 15$$

$$m = 389.5 + \left(\frac{15 - 10}{9} \right) \cdot 15$$

$$m = 389.5 + 8.33$$

$$= 397.83$$

• To Find mode

here, max freq = 9

so

The mode class is 389.5-404.5

$$\text{mode} = L + \left(\frac{f_1 - f_0}{2 \cdot f_1 - f_0 - f_2} \right) \cdot C$$

where

$$L = 389.5$$

$$f_1 = 9$$

$$f_0 = 6$$

$$f_2 = 7$$

$$C = 15$$

$$= 389.5 + \left(\frac{9 - 6}{2 \cdot 9 - 6 - 7} \right) \cdot 15$$

$$= 389.5 + 9$$

$$= 398.5$$

• To Find Quantiles

$$Q_3 = \left(\frac{3n}{4} \right) = \left(\frac{3+30}{4} \right) = 22.5$$

which lies under 405-419

Q₃ class: 404.5-419.5

$$\text{so } Q_3 = L + \left(\frac{\frac{3n}{4} - cf}{f} \right) \cdot h$$

where $L = 404.5$

$$cf = 19$$

$$h = 15$$

$$f = 7$$

$$Q_3 = 404.5 + \left(\frac{22.5 - 19}{7} \right) \cdot 15$$

$$= 404.5 + \frac{3 \cdot 15}{7}$$

$$= 404.5 + 7.5$$

$$= 412$$

Mo	Tu	We	Th	Fr	Sa	Su
DATE: / /						
Classes	f_n	c.f	x	$\bar{x} = \sum fx$	x^2	fx^2
64-84	15	15	74	1110	5476	1120
85-104	18	33	94.5	1701	8930.25	160744.5
105-124	27	60	114.5	3091.5	13110.25	353976.75
125-144	10	70	134.5	1345	18690.25	18902.5
145-164	6	76	154.5	927	23870.25	143221.5
165-184	5	81	174.5	872.5	30450.25	152251.25
185-204	13	94	194.5	2528.5	37830.25	491793.25
	94			11575.5	138357.5	1571029.75

$$s^2 = \frac{\sum fx^2}{n} - \left(\frac{\sum fx}{n}\right)^2$$

$$= \frac{1571029.75}{94} - \left(\frac{11575.5}{94}\right)^2$$

$$= 16713.082 - 15164.35$$

$$s^2 = 1548.73$$

Standard Deviation = $\sqrt{1548.73}$
= 39.35

Q4: If two fair dice are thrown, what is the probability of getting

1. A double six
2. A sum of 8 or more dots

Sol:

The sample space S is represented by the following 36 outcomes

$$S = \{(1,1), (1,2), (1,3), (1,4), (1,5), (1,6)$$

$$(2,1), (2,2), (2,3), (2,4), (2,5), (2,6)$$

$$(3,1), (3,2), (3,3), (3,4), (3,5), (3,6)$$

$$(4,1), (4,2), (4,3), (4,4), (4,5), (4,6)$$

$$(5,1), (5,2), (5,3), (5,4), (5,5), (5,6)$$

$$(6,1), (6,2), (6,3), (6,4), (6,5), (6,6)\}$$

1. Let A be the event that double six occurs

$$A = \{(6,6)\} \text{ and thus}$$

$$P(A) = 1/36$$

2. Let B denotes that a sum of 8 or more dots occurs

$$B = \{(2,6), (3,5), (3,6), (4,4), (4,5), (4,6), (5,3), (5,4), (5,5), (5,6), (6,2), (6,3), (6,4), (6,5), (6,6)\}$$

Hence

$$P(B) = 15/36 = 5/12$$

Q5. Let C_1, C_2, \dots, C_M be a partition of the sample space SS , and A and B be two events. Suppose we know that

- A and B are conditionally independent given C_i , for all $i \in \{1, 2, \dots, M\}$
- B is independent of all C_i 's.

Prove that A and B are independent.

The image shows a handwritten solution on a ZTE notebook page. The page has a header with a calendar (Mo, Tu, We, Th, Fr, Sa, Su) and the ZTE logo. The solution is written in blue ink and shows the following steps:

Sol
Since the C_i 's form a partition of the sample space, we can apply the law of total probability for $A \cap B$

$$\begin{aligned} P(A \cap B) &= \sum_{i=1}^m P(A \cap B | C_i) P(C_i) \\ &= \sum_{i=1}^m P(A | C_i) P(B | C_i) P(C_i) \\ &= \sum_{i=1}^m P(A | C_i) P(B) P(C_i) \\ &= P(B) \sum_{i=1}^m P(A | C_i) P(C_i) \\ &= P(B) P(A) \text{ Ans.} \end{aligned}$$

Good Luck