

7875

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Qs #01

VENTURE FLUME:

A venture flume is a critical flow open flume with a constricted flow which causes a drop in the hydraulic grade line, creating a critical depth:

Explanation:

It is used in flow measurement of very large flow rates, usually given in millions of cubic units. A venturi meter would normally measure in millimeters whereas a venturi flume measures in meters.

Problem:-

Given Data:-

$$b = 3 \text{ m}$$

$$Q = 12 \text{ m}^3 \cdot \text{s}^{-1}$$

(a) Discharge Per unit width

$$q_v = \frac{Q}{b} = \frac{12}{3} = 4 \text{ m}^2 \cdot \text{s}^{-1}$$

Then For a Rectangular channel

$$E_c = \frac{3}{2} h_c = \left(\frac{q_v^2}{g} \right)^{\frac{1}{3}} = \left(\frac{4^2}{9.81} \right)^{\frac{1}{3}} = 1.177 \text{ m}$$

Ans: critical depth is 1.18m

(b) For a Rectangular channel

$$E_c = \frac{3}{2} h_c = \frac{3}{2} \times 1.177 = 1.766 \text{ m}$$

Ans: Minimum Specific Energy = 1.77m

(c) As $E > E_c$, there are two possible depths for a given Specific Energy

$$E = h + \frac{v^2}{2g} \quad \text{where } v = \frac{Q}{A} = \frac{q_v}{h} \quad (\text{for rectangular channel})$$

$$\Rightarrow E = h + \frac{cv^2}{2gh^2}$$

Substituting values in meter-second units

$$4 = h + \frac{0.8155}{h^2}$$

For the subcritical (slow, deep) solution, the first term, associated with potential energy, dominates, so rearrange as,

$$h = 4 - \frac{0.8155}{h^2}$$

Iteration (from e.g. $h=4$) gives $h=3.948$ m.

For the supercritical (fast, shallow) solution, the second term, associated with kinetic energy, dominates, so rearrange as

Iteration (from, e.g., $h=0$) gives $h=0.4814$ m

Alternate depths are 3.95 m and 0.4814 m.

Q1 Problem

Solution:

check Froude Number

$$Fr = \frac{V}{\sqrt{gy}} = \frac{6 \text{ m/s}}{9.81 \times 0.1} = 6.06 > 1$$

So the flow is supercritical

$$E = y + \frac{v^2}{2g} = 0.1 \text{ m} + \frac{6}{2 \times 9.81} = 1.935 \text{ m}$$

Solving for the alternate depth for an $E = 1.935 \text{ m}$ yields $y_{alt} = 1.93 \text{ m}$

Q₃ Problem

Solution:-

$$E_1 = y_1 + \frac{V_1^2}{2g} = 3.0 + \frac{2}{2 \times 9.81} = 3.20 \text{ m}$$

$$E_2 = E_1 - \Delta z = 3.20 - 0.60 = 2.60 \text{ m}$$

Also

$$E_2 = y_2 + \frac{v^2}{2gy_2^3} = y_2 + \frac{6}{2 \times 9.81 \cdot y_2^3} = 2.60 \text{ m}$$

So $y_2 = 2.24 \text{ m}$. $\Delta y = y_2 - y_1 = 0.76 \text{ m}$ so water surface drops 0.16 m .

For a downward step of 15 cm we have giving $y_2 = 3.17 \text{ m}$ and $\Delta y = y_2 - y_1 = 0.17 \text{ m}$ so water surface rises 0.09 m .

The maximum upstep possible affecting upstream water surface level is for $y_2 = y_c$

$$y_c = 3 \sqrt{\frac{q^2}{g}} = 3 \sqrt{\frac{6^2}{9.81}} = 1.54 \text{ m}$$

problem 07:

A water passing from the vice gate in Dam:

Given data:

$$y_1 = 3 \text{ m} \quad y_2 = 0.9 \text{ m}$$

$$b = 3 \text{ m}$$

Sol:

as we know that

$$F_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \rightarrow \text{①}$$

Also

$$Q = A_1 v_1 = A_2 v_2$$

$$b_1 y_1 v_1 = b_2 y_2 v_2$$

($b_1 = b_2 = b$)

$$y_1 v_1 = y_2 v_2$$

$$y_1 v_1 = y_2 v_2$$

$$v_2 = \frac{y_1}{y_2} \times v_1$$

$$v_2 = \frac{3}{0.9} \times v_1 = 4v_1 \rightarrow \text{②}$$

putting eq (1)

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$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} = 2.6 + \frac{v_1^2}{2g} = 2.9 + \frac{v_2^2}{2g}$$

$$v_1 = 1.879 \text{ m/sec. put in eq (1) to get}$$

$$v_2 = 1.141$$

$$Q_1 = A_1 v_1 = b y_1 v_1$$

$$= 3.9 \times 3.6 \times 1.879$$

$$Q_1 = 26.38 \text{ m}^3/\text{sec}$$

$$\Rightarrow Q_2 = A_2 v_2 = b y_2 v_2 = 3.9 \times 3.116 \times 1.141$$

$$Q_2 = 26.38 \text{ m}^3/\text{sec}$$

$$Q = Q_1 = Q_2 = 26.38 \text{ m}^3/\text{sec}$$

(1) Froude number \rightarrow At upstream side

$$Fr_1 = \frac{v_1}{\sqrt{g y_1}} = \frac{1.879}{\sqrt{9.81 \times 3.6}} = 0.31$$

Subcritical flow

(2) Froude number \rightarrow At down stream side

$$Fr_2 = \frac{v_2}{\sqrt{g y_2}} = \frac{1.141}{\sqrt{9.81 \times 2.9}} = 2.58$$

Super critical flow