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MODULE

6th

TECHNOLOGY

CIVIL ENGG

SUBJECT

HYDRAULIC ENGG

SECTION

B

Q No 1

(A) Given DATA:-

$$\text{Channel width} = b = 8\text{m}$$

$$\text{Discharge} = Q = 7835 \text{ lit/sec} = 7.835 \text{ m}^3/\text{sec}$$

$$\begin{aligned} \text{Mean velocity} = v = R - 200 &= 7835 - 200 \\ &= 7635 \\ &= 2388.71 \text{ m/sec} \end{aligned}$$

As we know

$$Q = q b$$

$$\begin{aligned} q = Q/b &= \frac{7.835}{8} = \text{~~0.979375~~ } \\ &= 0.9793 \text{ m}^2/\text{sec} \end{aligned}$$

$$\Rightarrow y_c = \left(\frac{q^2}{g} \right)^{1/3}$$

$$= \left(\frac{0.9793^2}{9.81} \right)^{1/3} = 0.460 \text{ m}$$

$$y_c = 0.460 \text{ m}$$

As it is rectangular section

$$Q = q b \quad \text{--- (1)}$$

$$Q = Av \quad \text{--- (2)}$$

Equating (1) and (2)

$$qb = Av$$

$$qb = ybv$$

$$q = yv$$

$$vc = q/y_c = \frac{0.9793}{0.460}$$

$$= 2.12 \text{ m/sec}$$

$\therefore v > v_c$ (supercritical flow)

Height of hydraulic jump on the upstream
Side

As

$$Q = Av$$

$$Q = byv$$

$$y_1 = \frac{Q}{v_1 b}$$

$$y_1 = \frac{7.835}{2388.71 \times 8} = 0.00041 \text{ m}$$

$$y_2 = -\frac{y_1}{2} + \sqrt{\frac{y_1^2}{4} + \frac{2y_1 v_1}{g}}$$

$$y_2 = \frac{0.00041}{2} + \sqrt{\left(\frac{0.00041}{2}\right)^2 + \frac{2(0.00041)(2388.71)}{9.81}}$$

$$y_2 = \frac{0.00041}{2} + \sqrt{\left(\frac{0.00041}{2}\right)^2 + \frac{2(0.00041)(2388.71)}{9.81}}$$

$$y_2 = 21.838 \text{ m}$$

$$\Delta y = y_2 - y_1$$

$$= 21.838 - 0.00041$$

$$\Delta y = 21.837$$

$$\therefore \Delta E = E_1 - E_2$$

As we know that

$$Q_1 = Q_2$$

$$A_1 v_1 = A_2 v_2$$

$$b_1 y_1 v_1 = b_2 y_2 v_2$$

$$v_2 = \frac{y_1 v_1}{y_2}$$

$$v_2 = \frac{0.00041 \times (2388.71)}{21.838} = 0.044 \text{ m/sec}$$

$$\Delta E = E_1 - E_2 = \left(y_1 + \frac{v_1^2}{2g} \right) - \left(y_2 + \frac{v_2^2}{2g} \right)$$

$$= \left(0.00041 + \frac{2388.71^2}{2(9.81)} \right) - \left(21.838 + \frac{0.044^2}{2(9.81)} \right)$$

$$E_1 - E_2 = \cancel{2900} \ 290800.5611$$

⇒ Power Absorbed:

$$\Delta P = \rho g Q (E_1 - E_2)$$

$$\Delta P = 1000 \times 9.81 \times 7.835 (290800.56)$$

$$\Delta P = 22352323.62 \text{ W}$$

Q No 1 part b

Given DATA :-

$$B = 4 \text{ m}$$

$$Q = 7835 \text{ ft}^3/\text{sec} = \frac{7835}{(3.28)^3} = 222.03 \text{ m}^3/\text{sec}$$

$$y_1 = 2.9 \text{ m}$$

$$y_2 = 1.1 \text{ m}$$

Let specific Energy at upstream and downstream side

$$E_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \quad \text{--- (1)}$$

We know that $Q = A_1 v_1 = A_2 v_2$

$$b y_1 v_1 = b y_2 v_2$$

$$\therefore b_2 = b_1 = b$$

$$v_2 = \frac{y_1 v_1}{y_2}$$

$$v_2 = \frac{2.9 v_1}{1.1}$$

$$v_2 = 2.634 v_1 \quad - \textcircled{2}$$

Put the value of (eq) (2) in eq (1)

$$2.9 + \frac{v_1^2}{2 \times 9.81} = 1.1 + \left(\frac{2.634 v_1}{2 \times 9.81} \right)^2$$

$$2.9 - 1.1 = \frac{6.938 v_1^2}{19.62} - \frac{v_1^2}{19.62}$$

$$1.8 = \frac{6.938 v_1^2 - v_1^2}{19.62}$$

$$1.8 \times 19.62 = 5.938 v_1^2$$

$$v_1^2 = \sqrt{\frac{1.8 \times 19.62}{5.938}}$$

$$v_1 = 2.44 \text{ m/sec}$$

Now put the value of "v₁" in eq (1)

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$2.9 + \frac{2.44^2}{2 \times 9.81} = 1.1 + \frac{v_2^2}{2 \times 9.81}$$

$$2.9 - 1.1 = \frac{v_2^2}{2 \times 9.81} - \frac{5.95}{2 \times 9.81}$$

$$1.8 = \frac{v_2^2 - 5.95}{2 \times 9.81}$$

$$1.8 \times 2 \times 9.81 = v_2^2 - 5.95$$

$$\sqrt{v_2^2} = \sqrt{41.266}$$

$$v_2 = 6.42 \text{ m/sec}$$

Using Froude No to Determine type of flow

upstream side :-

$$Fr_1 = \frac{v_1}{\sqrt{g y_1}} = \frac{2.44}{\sqrt{9.81 \times 2.9}} = 0.457 < 1$$

(subcritical flow)

Downstream side :-

$$Fr_2 = \frac{v_2}{\sqrt{g y_2}} = \frac{6.42}{\sqrt{9.81 \times 1.1}} = 1.95 > 1$$

(supercritical flow)

Q No 2

(A) Given Data :-

$$y = 1.8 \text{ m}$$

$$b = 66' = \frac{66}{3.28} = 20.12 \text{ m}$$

$$Q = \frac{7835}{3.28^3} = 222.03 \text{ m}^3/\text{sec}$$

Required DATA :-

Minimum Height (P) of weir

$$Q = AV$$

$$V = \frac{Q}{A} = \frac{Q}{by} = \frac{222.03}{20.12 \times 1.8} = 6.13 \text{ m/sec}$$

As we know

$$y_c = \left(\frac{q^2}{g} \right)^{1/3} = \left(\frac{11.04^2}{9.81} \right)^{1/3} \quad ; \quad q = \frac{Q}{b} = \frac{222.03}{20.12}$$

$$y_c = 2.32 \text{ m}$$

$$= 11.04 \text{ m}^2/\text{sec}$$

(8)

Also

$$v = \sqrt{2gH}$$

$$v_c = \sqrt{2gyc} = \sqrt{9.81 \times 2.32}$$

$$= 4.77 \text{ m/sec}$$

Now; According to specific energy

$$E_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = \frac{v_c^2}{2g} + y_c + P$$

$$1.8 + \frac{6.13^2}{2 \times 9.81} = \frac{4.77^2}{2 \times 9.81} + 2.32 + P$$

$$3.72 = 3.48 + P$$

$$P = 3.72 - 3.48$$

$$P = 0.24 \text{ m}$$

Qno 2

(B)

Given DATA

$$b = 2.8 \text{ m}$$

$$d = 1.5 \text{ m}$$

$$H_1 = 5 \text{ m}$$

$$H_2 = 5 + 1.5 = 6.5 \text{ m}$$

$$H = 5 + 0.6 = 5.6 \text{ m}$$

$$C_d = 0.7835$$

Required Data $Q = ?$

Discharge through submerged portion

$$Q_1 = C_d \times b \times (H_2 - H) \times \sqrt{2gH}$$

$$= 0.7835 \times 2.8 \times (6.5 - 5.6) \times \sqrt{2 \times 9.81 \times 5.6}$$

$$Q_1 = 20.69 \text{ m}^3/\text{sec}$$

Discharge of free portion

$$Q_2 = \frac{2}{3} C_d \times b \sqrt{2g} \left[H^{3/2} - H_1^{3/2} \right]$$

$$Q_2 = \frac{2}{3} (0.7835) \times 2.8 \sqrt{2 \times 9.81} \left[5.6^{3/2} - 5^{3/2} \right]$$

$$Q_2 = 13.422 \text{ m}^3/\text{sec}$$

Total Discharge

$$Q = Q_1 + Q_2$$

$$Q = 20.69 + 13.422$$

$$Q = 34.11 \text{ m}^3/\text{sec}$$

Q No 3

(A) Given data

$$P_1 = R + 800 = 7835 + 800 = 8635 \text{ N/m}^2$$

$$d_1 = R - 200 = 7835 - 200 = 7635 \text{ mm}$$

$$= 7.635 \text{ m}$$

$$A_1 = \frac{\pi d_1^2}{4} = \frac{\pi (7.635)^2}{4} = 45.79 \text{ m}^2$$

$$d_2 = R + 3000 = ~~7835~~ 7835 + 3000 = 10835 \text{ mm}$$

$$= 10.835 \text{ m}$$

$$A_2 = \frac{\pi d_2^2}{4} = \frac{\pi (10.835)^2}{4} = 92.22 \text{ m}^2$$

$$Q = 0.95 \text{ m}^3/\text{sec}$$

$$\therefore Q = Av$$

$$v = Q/A$$

$$v_1 = \frac{Q_1}{A_1} = \frac{0.95}{45.79} = 0.021 \text{ m/sec}$$

$$v_2 = \frac{Q_2}{A_2} = \frac{0.95}{92.22} = 0.01 \text{ m/sec}$$

(1) Head loss due to sudden Enlargement

$$h_e = \left(1 - \frac{A_1}{A_2}\right)^2 \left(\frac{v_1 - v_2}{2g}\right)^2$$

$$= \left(1 - \frac{45.79}{90.22} \right)^2 \times \left(\frac{0.021 - 0.01}{2 \times 9.81} \right)^2$$

$$h_e = 1.56 \times 10^{-6} \text{ m}$$

$$h_e = 0.0000015 \text{ m}$$

② Power lost due to sudden enlargement

$$P = \rho g Q h_e$$

$$P = 1000 \times 9.81 \times 0.95 \times 1.5 \times 10^{-6}$$

$$P = 0.014 \text{ W}$$

③ Pressure into smallest pipe
Apply Bernoulli's eq

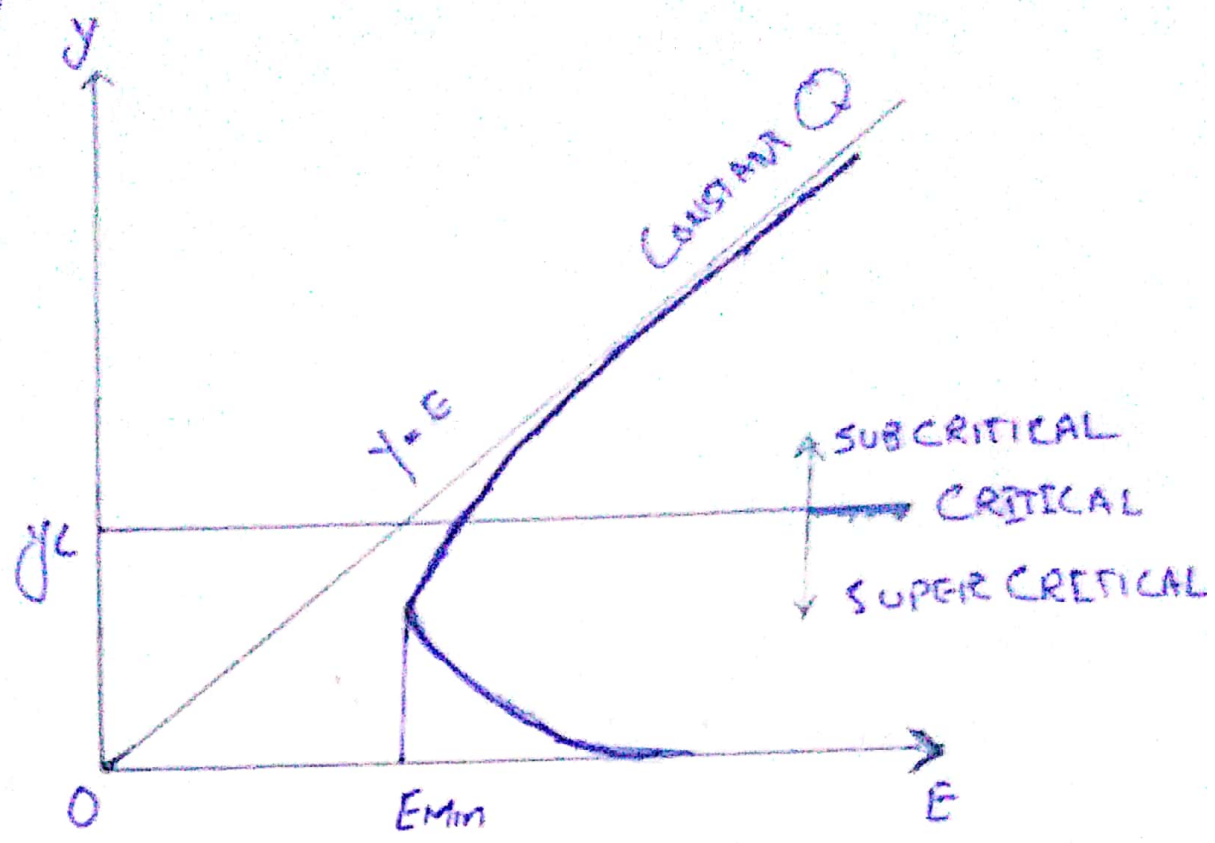
$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + h_e$$

$$\frac{8635}{1000 \times 9.81} + \frac{0.071^2}{2 \times 9.81} = \frac{P_2}{1000 \times 9.81} + \frac{0.21^2}{2g} + 1.56 \times 10^{-6}$$

$$P_2 = 0.879 \times 9810$$

$$P_2 = 8632.73 \text{ N/m}^2$$

Q No 3
B



What does this blue curve indicate? How is it obtained? Explain the above figure from each and every point of view?

Ans. The above graph is a plot between depth flow (y) and specific energy (E). It is made from a three-degree polynomial equation which shows us the different specific energy for the depth flow which may be either

- i) Subcritical
- ii) Critical
- iii) Super critical

Specific energy is used to clarify the meaning of the above terms in an open channel.

How is it achieved :-

Total Energy = Potential Energy + Kinetic Energy

$$T.E = mgh + \frac{1}{2} mv^2$$

$$\begin{aligned} \therefore w &= mg \\ m &= w/g \end{aligned}$$

$$= wh + \frac{1}{2} \frac{w}{g} v^2$$

Ignoring "w" weight of water

$$TE = h + \frac{v^2}{2g}$$

$$TE = y + \frac{v^2}{2g} \quad \text{--- (1)}$$

As we know that

$$Q = VA$$

$$V = \frac{Q}{A}$$

\therefore squaring b.s

$$V^2 = \frac{Q^2}{A^2}$$

put V^2 in eq (1)

$$E = y + \frac{Q^2}{A^2 \cdot 2g} \quad \text{--- (2)}$$

let's suppose the channel is Rectangular

$$A = y \times b \quad \text{--- (3)}$$

$$Q = qb = (y) \quad \text{--- (4)}$$

putting value of (3) and (4) in (2)

$$E = y + \frac{Q^2}{y^3 b^2 \cdot 2g} \quad \text{(putting 3)}$$

$$E = y + \frac{q^2}{y^3 \cdot 2g} \quad \text{--- putting (4)}$$

$$E - y = \frac{q^2}{y^3 \cdot 2g}$$

$$(E-y)y^2 = \frac{q^2}{2g}$$

$$(E-y)y^2 = \text{constant}$$

As " q " and " g " are constants

critical depth is the flow depth corresponding to minimum specific Energy

$y > y_c \Rightarrow$ subcritical flow

$y = y_c \Rightarrow$ critical flow

$y < y_c \Rightarrow$ supercritical flow