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Subject	"	"	PRC D-1
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①

Q No 2

a) Briefly describe Bond stress and Development length?

Bond stress

Bond stress is the shear stress developed along the contact surface between the reinforcing steel and surrounding concrete which prevent the bar from slipping out of concrete. The permissible bond stress depend upon the grade of concrete and type of steel.

Development length:

It is minimum length of bar which must be embedded in concrete beyond any section to develop its full strength. This is also called anchorage length in case of axial tension or axial compression and development length in case of flexural tension or flexural compression.

$$\text{Development length in tension} = \frac{\phi \sigma_{st}}{4\tau_{bd}}$$

$$\text{Development length in compression} = \frac{\phi \sigma_{sc}}{5\tau_{bd}}$$

Q) In which condition doubly reinforced beam can be used?

Ans Doubly reinforced beam can be used in following situations.

→ when singly reinforced beam is not provided in term of moment-resisting capacity.

→ where the cross sectional of the beam are restricted by architectural or other consideration.

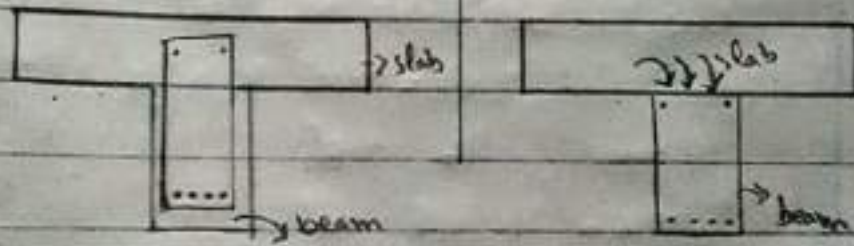
→ when the size of the beam is confined.

→ when the section of the beam is subjected to torsion stress.

→ when the beam is not stop more than a few balking.

(C) differentiate b/w T-beam analysis and rectangular beam analysis:

T-Beam	Rectangular-beam
In T-Beam both the slab and beam are connected each other and we called this joint is called monolithic joint	It should look like rectangular cross section and there should no joints b/w slab and beam but it should act separately from one another.



(4)

d) write a short note on the effect of strength reduction factor on Flexural strength.

Effect of strength Reduction factors:-

- (i) Due to strength reduction factor, it is possible to cope with the variation in dimension i.e. structure remain safe.
- (ii) Strength reduction factors help to absorb the effects due to change in material strength.
- (iii) Possible inaccuracies in the strength equation.
- (iv) Ensure good level of safety of reinforced concrete structure.

(5)

(e) Design method:-

Design method are procedure, techniques and aid for designing. They offer a number of different kind of choices that a designer might use with an overall design process.

Following are design method are given as

Simple design:-

This is the most commonly used design method. It is used where end connections of the member in a structure do not develop restraint moment that would affect the structure.

Semi rigid Design method:-

It permits a reduction in maximum bending moment in beam suitably connected to fixed support as compared to simple design.

In case where this method of design is employed, experimental evidence shall be made to show that stress in any part of structure are not in excess.

(6)

Step # 01

A rectangular beam has to carry a service live load of 2.47 kips/ft and a calculated dead load of 1.05 kips/ft (without self-weight) on an 18-ft simple span limited to 10 inches width and 20 inches total depth for architectural reasons. If $f_y = 60,000$ psi and $f_c = 4,000$ psi. What steel area must be provided? Draw sketch of your final design.

Given data:-

$$\text{Live load (L)} = 2.47 \text{ kips/ft}$$

$$\text{Dead load (D.L)} = 1.05 \text{ kips/ft}$$

$$\text{Span} = 18'$$

$$\text{width (b)} = 10''$$

$$\text{depth (h)} = 20''$$

$$f_y = 60,000 \text{ Psi} = 60 \text{ Ksi}$$

$$f_c = 4,000 \text{ Psi} = 4 \text{ Ksi}$$

Solution:-

Step # 01

$$\text{Effective depth (d)} = h - 3 \Rightarrow 20 - 3 = 17''$$

$$\text{Effective cover (d')} = 2.5''$$

Reinforcement Ratio is

(7)

$$I_{max} = 0.85 \times \beta \times \frac{f'c \cdot I_g}{f_y} \left(\frac{\epsilon U_{max}}{\epsilon_u + \epsilon_y} \right)$$

$$I_{max} = 0.85 \times 0.85 \times \frac{4}{60} \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$I_{max} = 0.0180$$

Step #2

As we know that

$$I_{max} = \frac{I_t}{b \times d} \Rightarrow I_t = I_{max} (b \times d)$$

$$I_t = 0.0180 \times (10 \times 17)$$

$$I_t = 3.06 \text{ m}^2$$

Step #3

$$M_{us} = \phi \times A_{st} \times f_y \times (d - \frac{a}{2})$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f'c \times b} = \frac{3.06 \times 60}{0.85 \times 4 \times 10} = 5.4$$

$$M_u = 0.90 \times 3.06 \times 60 \times (17 - 5.4/2)$$

$$= 2362.97 \text{ kip-in}$$

Moment due to given load:-

$$\text{Beam self weight} = \frac{10}{12} \times \frac{20}{12} \times 150$$

$$= 208.33 \text{ Lb/ft}$$

(8)

$$\begin{aligned}\text{Total factored load} &= 1.2(1050 + 218.33) + 1.6(240) \\ &= 5461.99 \text{ lb/ft} \\ &= 5.46 \text{ kip/ft}\end{aligned}$$

$$\begin{aligned}\text{Ultimate Factored moment} &= \frac{wL^2}{8} \\ &= \frac{5.46 \times (18)^2 \times 12}{8}\end{aligned}$$

$$M_u = 2653.56$$

So

$$M_u < M_o$$

$$2362.97 < 2653.56$$

Doubly Reinforcement Required

Step # 4

$$M_{u1} = 2653.56 - 2362.97$$

$$= 290.64 \text{ kip-inch}$$

step # 5

$$M_{u1} = \phi \times A_{st} \times f_y \times (d - d')$$

$$A_{st}' = \frac{M_{u1}}{\phi f_y (d - d')}$$

$$= \frac{290.64}{0.9 \times 60 \times (17 - 2.5)} = 0.37 \text{ in}^2$$

$$0.9 \times 60 \times (17 - 2.5)$$

step # 6 Total steel area

$$A_s = A_{st} + A_{st}'$$

(7)

$$A_t = 3.06 + 0.37 = 3.43 \text{ in}^2$$

⇒ Step No #7

Use use #8 bar (dia = $\frac{9}{8} = 1.125$)

$$A_{bar} = 0.785 \text{ in}^2$$

$$\begin{aligned} \text{No. of bars} &= \frac{A_t}{\text{Area of 1 bar}} \\ &= \frac{3.43}{0.785} = 4.36 \approx 5 \text{ bars} \end{aligned}$$

So 5 #8 bars for Tension zone

→ Compression steel :-

Use #6 bars

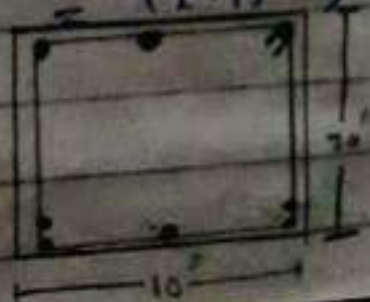
$$\text{dia } (\frac{6}{8}) = 0.75, \text{ Area} = 0.44 \text{ in}^2$$

$$\begin{aligned} \text{No. of bars} &= \frac{A_{st}'}{\text{Area of 1 bar}} = \frac{0.37}{0.44} = 0.84 \\ &0.84 \approx 1 \text{ bar} \end{aligned}$$

So 1 #6 bars in compression zone

Step #8

$$\begin{aligned} b_{min} &= 2(1.5) + 2\left(\frac{3}{8}\right) + 5\left(\frac{9}{8}\right) + 4\left(\frac{6}{8}\right) \\ &= 12.75 > 10'' \text{ multiple layers} \end{aligned}$$



(10)

$$\text{Effective depth } (d) = 20 - 1.5 - \frac{3}{8} - \frac{7}{8} - \frac{1}{2} \left(\frac{3}{8} \right)$$
$$d = 16.62''$$

$$\text{Effective cover } (d') = 1.5 + \frac{3}{8} + \frac{1}{2} \left(\frac{3}{8} \right)$$
$$d' = 2.25''$$

Step # 09 :-

$$M_d = \phi \times \left[A_{st}' \times f_y \times (d - d') \right] + (A_{st} - A_{sc}') \times f_y \times (d - a/2)$$

$$a = \frac{(A_{st} - A_{sc}') \times f_y}{0.85 \times f_c' \times b}$$

$$= \frac{(5 \times 0.785 - 1 \times 0.44) \times 60}{0.85 \times 4 \times 10} = 6.15''$$

$$M_d = 0.90 \left[(1 \times 0.44) \times 60 \times (16.62 - 2.25) + (5 \times 0.785 - 1 \times 0.44) \times 60 \times \left(16.62 - \frac{6.15}{2} \right) \right]$$

$$M_d = 2890.46$$

$$\text{As } M_d = 2890.46 > 2653.56$$

Design is OK.

(11)

No 3

Given data:

$$c/c \text{ distance} = 10'$$

$$\text{Total depth} = 28''$$

$$\text{Effective depth} = 28'' - 3'' = 25''$$

$$D.L = 50 \text{ lb/ft}^2$$

$$S.S = 225 \text{ lb/ft}^2$$

$$f_y = 60,000 \text{ PSI}$$

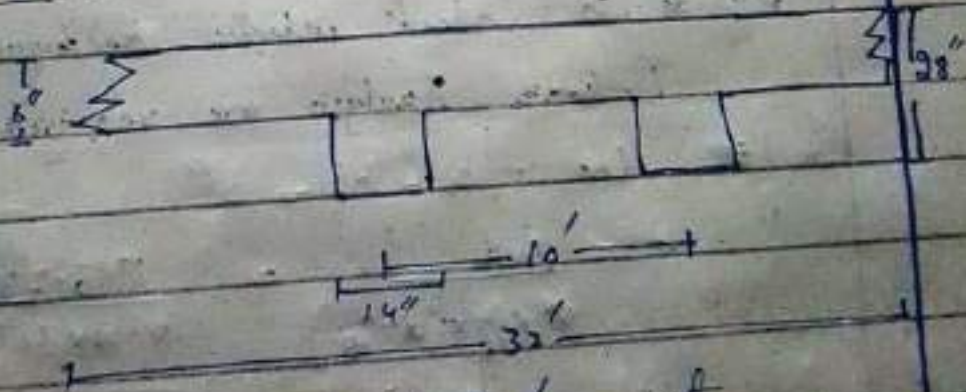
$$f'_c = 4,000 \text{ PSI}$$

$$\text{Span} = 32'$$

$$\text{slab thickness} = 6''$$

$$\text{web width} = 14''$$

Solution:



Step No 1 :- Estimate factored moment

$$M_u = \frac{w_u \times L^2}{8}$$

Beam self weight per foot

(2)

$$w_k = b \times t \times \gamma_c$$

$$w_k = \frac{14 \times 28 \times 150}{12 \times 12} = 408.33 \text{ lb/ft}$$

Total Factored Load :-

$$= 1.2(50 + 408.33) + 1.6(225)$$

$$= 709.99 \text{ lb/ft} = 0.905 \text{ Kip/ft}$$

Moment :-

$$w_k l^2 = 0.905 \times (39)^2 \times 12 = 1396.23 \text{ Kip-inch}$$

Step #02 calculate

Effective width :- width 'bc'

a) $16(h_f) + w = 16(6) + 14 = 110''$

b) c/c distance = $10(12) = 120''$

c) span/4 = $32 \times 12 = 96''$

So $bc = 96''$

Step #03 check whether Rectangular or T-Beam Analysis are required :-

Trail #1 $l_{cl} \cdot a = h_f = 6''$

$$a_k = \frac{M_o}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{1396.23}{0.9 \times 60 \times (25 - \frac{6}{2})}$$

$$A_{st} = 1.17 \text{ in}^2$$

Trail #2

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{1.17 \times 60}{0.85 \times 4 \times 76} = 0.22 < 6''$$

So Rib beam design

(13)

$$A_s = \frac{1396.23}{0.9 \times 60 (25 - \frac{0.7}{8})} = 1.051 \text{ in}^2$$

$f_{max} = 0.03$

$$a = \frac{1.03 \times 60}{0.85 \times 4 \times 96} = 0.18 \text{ in}$$

$$A_s = \frac{1396.23}{0.9 \times 60 (25 - \frac{0.18}{2})} = 1.031 \text{ in}^2$$

step # 4

check f_{max} and f_{min}

$$f_{max} = 0.85 \times 0.85 \times \frac{4}{60} \left(\frac{0.03}{0.005 + 0.005} \right)$$

$$f_{max} = 0.018$$

$$f_{min} = \frac{200}{f_y} = \frac{200}{60,000} = 0.003$$

$$f = \frac{A_s b}{b \times d} = \frac{1.03}{14 \times 25} = 0.0029$$

$$f_{min} < f < f_{max}$$

$$0.003 < 0.0029 < 0.018$$

So

f is less than f_{min}

So,

$$S_{min} = A_s \rightarrow A_s = S_{min} \times b \times d$$

$$A_s = 0.003 \times 14 \times 25 = 1.05 \text{ in}^2$$

Step # 05 :-

selection of No of bars

Let bar # 8 than

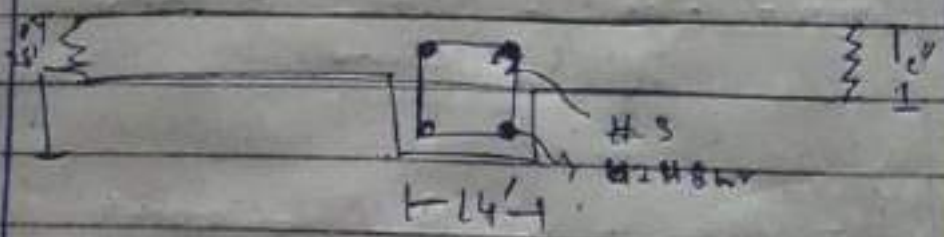
$$d_{in} = \frac{8}{8} = 1 \text{ Area} = 0.785 \text{ in}^2$$

$$\text{No of bars} = \frac{1.05}{0.785} = 1.3 \approx 2$$

step # 06

check minimum width

$$b_{min} = 2(1.5) + 2(\frac{3}{8}) + 2(\frac{8}{8}) + 1(\frac{8}{8}) = 6.75 \text{ in} < 14 \text{ in}$$



step # 7 Design moment:

$$M_d = \phi \times f_y \times A_s \times (d - a/2)$$

$$\text{Area of steel} = \frac{\text{Area of 1 bar} \times \text{No of bars}}{0.785 \times 2} = \frac{1.57 \text{ in}^2}{1.57 \text{ in}^2}$$

$$a = \frac{1.57 \times 60}{0.85 \times 4 \times 96} = 0.2 \text{ in}$$

(15)

$$Md = 0.90 \times 60 \times 1.57 \times (25 - 0.02/2)$$

$$= 2111.02 \text{ kip-in}$$

$$As = 2111.02 > 1396.23$$

okay