

Final paper

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Section: B

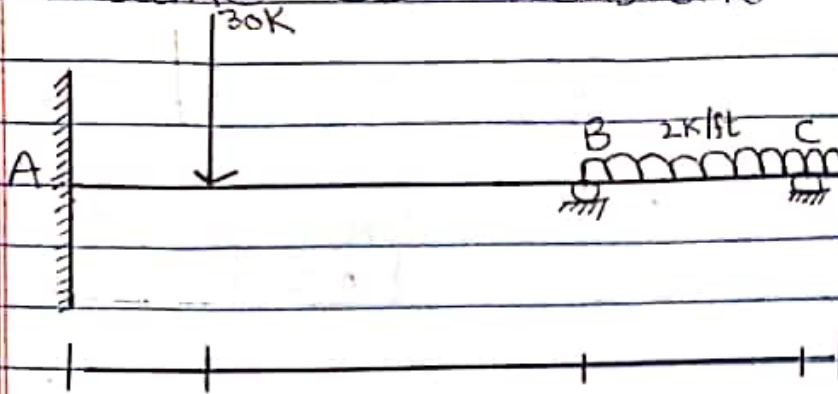
Subject: Structural Analysis II

Submitted to: Eng Adeed

Date: 25/9/2020

Q1

Q1 Analyze the beam shown in fig-1 by stiffness method. Assume EI constant.

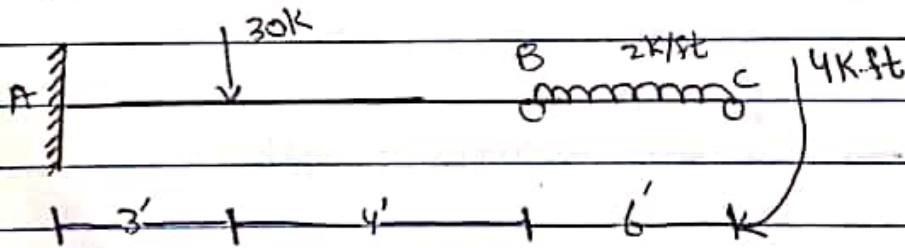


Solution:

* Step # 1

Determining Kinematic Interminancy,
 $K \cdot I = 4^{\circ}$

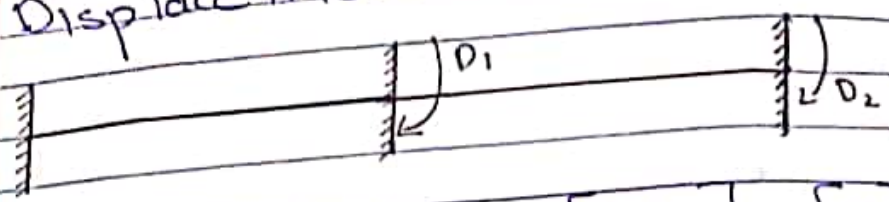
So we have to reduce the extend portion



Now $K \cdot I = 2^{\circ}$

* Step # 02

Determine unknown Joint Displacement

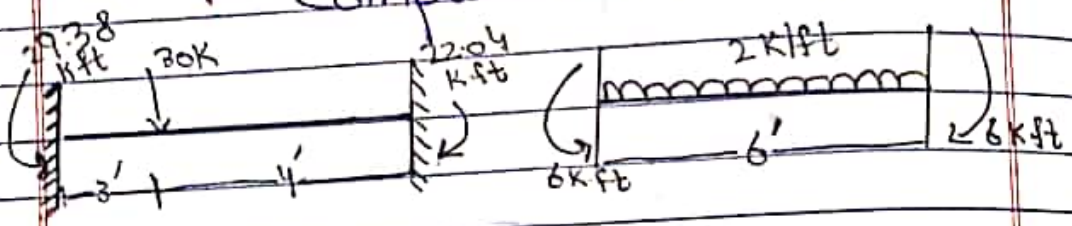


$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$\begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

★ Step # 3

compute [ADL] matrix



→ for point load (not at mid)

→ for left end:

$$\frac{Pab^2}{L^2} = \frac{(30)(3)(4)^2}{(7)^2} = \boxed{29.38 \text{ K.ft}}$$

→ for right end:

$$\frac{Pa^3}{L^2} = \frac{(30)(3)^2(4)^2}{(7)^2} = \boxed{22.04 \text{ K.ft}}$$

(4)

Day: M T W T F S

Date: ___/___/___

→ for uniformly distributed load:

$$\frac{wL^2}{12} \Rightarrow \frac{2(6)^2}{12} = 6 \text{ k-ft}$$

$$ADL_1 = +22.04 - 6 = 16.04 \text{ k-ft}$$

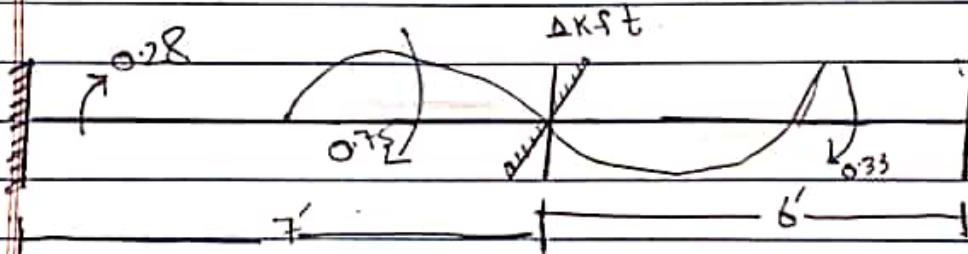
$$ADL_2 = 6 \text{ k-ft}$$

* Step # 04:

Now compute [S] matrix

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

a) $D_1 = K$, $D_2 = 0$



$$\frac{4EI}{7} = 0.57$$

$$\frac{2EI}{6} = 0.33$$

$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{7} = 0.28$$

$$S_{11} = 0.57 + 0.67$$

$$S_{11} = 1.24 EA$$

$$S_{21} = 0.33 EA$$

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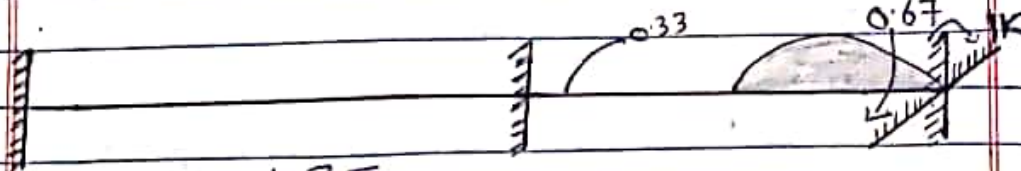
5

Day: MTWTFSS

Date: ___/___/___

b) $D_1 = 0$

$D_2 = 1K$



$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$S_{12} = 0.33$

;

$S_{22} = 0.67$

$S =$	$\begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$
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Step# 05

Now compute [D] matrix

$$\begin{bmatrix} P_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$= \frac{1}{\begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}} \times \text{Adj} \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$|S| = (124 \times 0.67) - (0.33 \times 0.33)$$

$$= 83.308 - 0.1089$$

$$|S| = 83.219$$

$$\text{Adj } A = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 124 \end{bmatrix}$$

Now

$$\begin{bmatrix} AD_1 - ADL_1 \\ AD_2 - ADL_2 \end{bmatrix} = \begin{bmatrix} 0 & -16.04 \\ 4 & 6 \end{bmatrix} = \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} \text{ \textcircled{E}}$$

~~$$A \times \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 124 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$~~

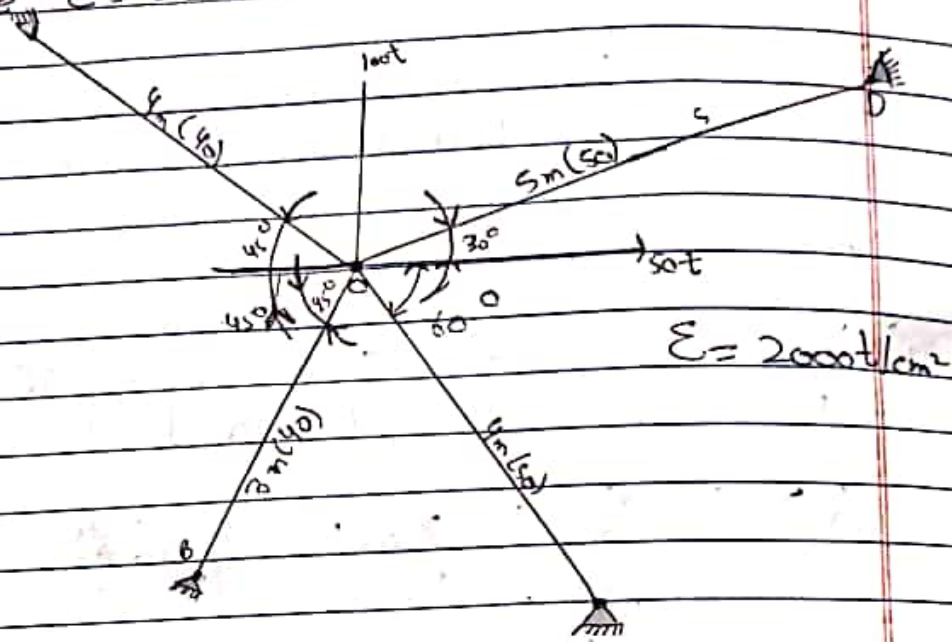
$$\rightarrow \begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \frac{1}{|S|} \times \text{Adj } A \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

$$= \frac{\begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 124 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}}{83.219}$$

$$= \begin{bmatrix} 0.919 & -0.452 \\ -0.452 & 1.70 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.83 \\ 3.85 \end{bmatrix}$$

Q No 12) Analyze the pin-jointed frame show by stiffness method - length of member in m and cross section area in cm² are show in fig 3
 Take $E = 2000 \text{ t/cm}^2$



Solution:



For A

$$\sin 45^\circ = \frac{P}{H} = \frac{P}{4}$$

$$\rightarrow P = 2.828m$$

$$\cos 45^\circ = \frac{b}{H} = \frac{b}{4}$$

$$\rightarrow -2.828m$$



For B

$$\sin 45 = \frac{P}{H} = \frac{P}{3}$$

$$\rightarrow P = 2.12m$$

$$\cos 45 = \frac{b}{H} = \frac{b}{3}$$

$$\rightarrow b = 2.12m$$

\Rightarrow For C

$$\sin 60 = \frac{P}{H} = \frac{P}{4}$$

$$(\sin 60)(4) = P$$

$$\rightarrow P = 3.46$$

$$\cos 60 = \frac{b}{H} = \frac{b}{4}$$

$$\cos 60 \times 4 = b$$

$$\rightarrow b = 2$$

For D

$$\sin 30 = \frac{P}{5}$$

$$\rightarrow P = 2.5m$$

$$\cos 30 = \frac{b}{5}$$

$$b = 4.33m$$

9

Date: ___/___/___

Day: M T W T F S

Now

$$EA_{(A)} = 2000 \times 40 = 80,000t$$

$$EA_{(B)} = 2000 \times 40 = 80,000t$$

$$EA_{(C)} = 2000 \times 50 = 100,000t$$

$$EA_{(D)} = 2000 \times 50 = 100,000t$$

Step # 1 K.I

$$KI = 2j - 8$$

$$= 2(5) - 8$$

$$KI = 2^0$$

★ Step # 2

Select unknown joint displacement

A(-2.82, 2.82)

D(4.33, 2.5)

D₂

D₁

B(-2.12, 2.12)

C(2, -3.46)

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} S_0 \\ -100 \end{bmatrix}$$

* Step#03

$$\begin{bmatrix} AMD \end{bmatrix}_{4 \times 2} \quad \begin{bmatrix} S \end{bmatrix}_{2 \times 2}$$

1) $D_1 = 1K$, $D_2 = 0$

$$AMD = \frac{EA}{L^2} (x_k - x_i)$$

$$AM_{D_{11}} = \frac{80000}{(400)^2} \times (0 - 282) = 141$$

$$AM_{D_{21}} = \frac{80000}{(300)^2} \times (0 - 212) = 188.44$$

$$AM_{D_{31}} = \frac{100,000}{(500)^2} \times (0 - 433) = -173.2$$

$$AM_{D_{41}} = \frac{100,000}{(400)^2} \times (0 - 200) = -125$$

Now,

$$S_{11} = \sum_{i=1}^m \frac{EA}{L^3} (x_k - x_i)^2$$

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$$= \frac{80,000 (282)^2}{(400)^3} + \frac{80,000 \times (212)^2}{(300)^2}$$

$$\frac{100,000 \times (-433)^2}{(500)^3} + \frac{100,000 \times (-200)^2}{(400)^3}$$

$$S_{11} = 99.405 + 133.107 + 149.991 + 62.5$$

$$\boxed{S_{11} = 445.063}$$

$$\Rightarrow S_{12} = S_{21} - \sum_{k=1}^m \frac{\epsilon A}{L^3} \times (x_k - x_j)(y_k - y_j)$$

$$= \frac{80,000 (282)(-282)}{(400)^3} + \frac{80,000 (-22)(212)}{(300)^3}$$

$$+ \frac{100,000 (-433)(0-250)}{(500)^3} + \frac{100,000 (-200)(0+16)}{(400)^3}$$

$$\boxed{S_{12} = S_{21} - 12.237}$$

$$(2) D_1 = 0, \quad D_2 = \Delta K'$$

$$AMD = \frac{\epsilon A}{L^2} (y_k - y_j)$$

$$AMD_{12} = \frac{80,000 (-282)}{(400)^2} = -1141$$

$$AMD_{22} = \frac{80,000 (212)}{(300)^2} = 188.44$$

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$$AMD_{32} = \frac{100,000 \cdot (-250)}{(500)^2} = -100$$

$$AMD_{42} = \frac{100,000 \cdot (346)}{(400)^2} = 216.25$$

$$\text{Now, } S_{22} = \sum_{i=1}^m \frac{\epsilon A_i}{L^3} (y_k - y_j)^2$$

$$= \frac{80,000 \cdot (-282)^2}{(400)^3} + \frac{80,000 \cdot (212)^2}{300^3}$$

$$+ \frac{100,000 \cdot (-250)^2}{500^3} + \frac{100,000 \cdot (346)^2}{400^3}$$

$$S_{22} = 469.628$$

= Step #4

$$[D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.003 & 12.237 \\ 12.237 & 469.628 \end{bmatrix}^{-1} \times \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

Step #5

$$[AM]$$

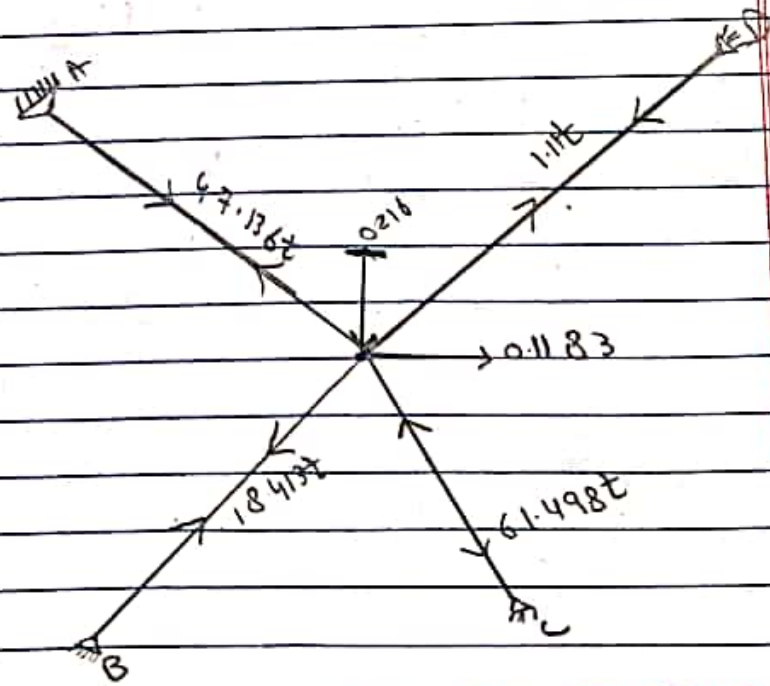
Day: MTWTFSS

AM ₁	=	141	-141	x	0.1183
AM ₂		184.44	188.44		-0.216
AM ₃		-173.2	-100		
AM ₄		-125	216.25		

$$= 141 \times 0.1183 + (-141) \times (-0.216) + 188.44 \times 0.1183 + (188.44) \times (-0.216) - 173.2 \times 0.1183 + (-100) \times (-0.216) - 125 \times 0.1183 + 216.25 \times (-0.216)$$

AM ₁	=	16.68 + 30.46
AM ₂		22.29 - 40.76
AM ₃		-20.49 + 21.6
AM ₄		-14.79 + 46.71

AM ₁	=	47.136t
AM ₂		-18.413t
AM ₃		1.11t
AM ₄		-61.498t



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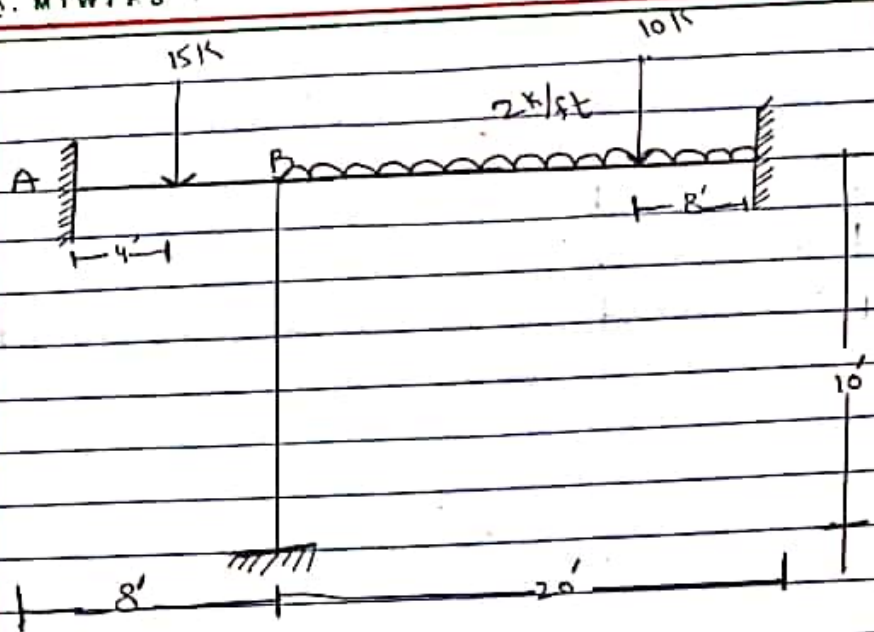
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Date: ___/___/___

Day: M T W T F S

Q/3



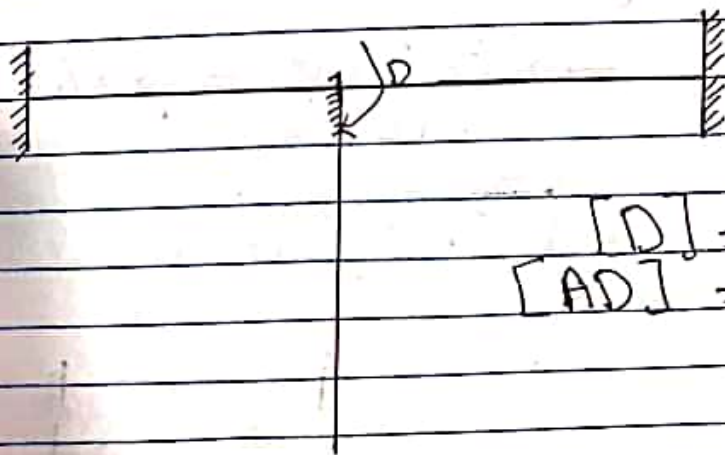
Solution:

Step #1

Kinematic indeterminacy
 $K.I. = 1^0$

Step #2

Determine unknown joint displacement

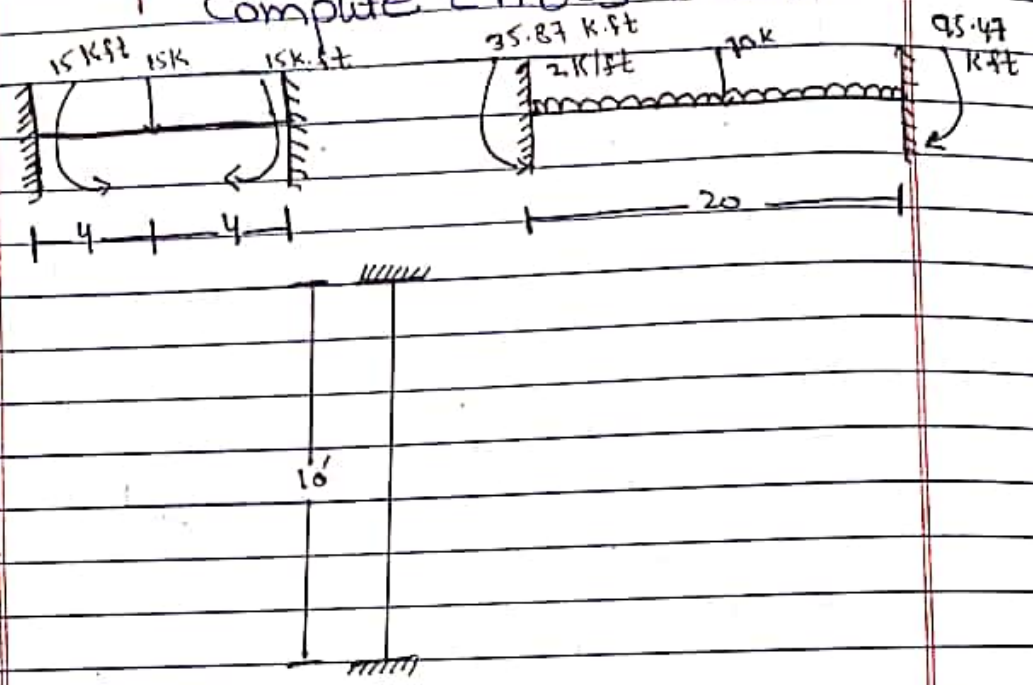


$$[D] = [?]$$

$$[AD] = [0]$$

Step #3

Compute [ADL] Matrix



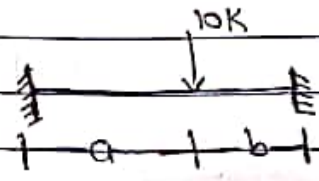
* point load at centre:

$$PL = \frac{(15)(8)}{8} = \boxed{15 \text{ Kip-ft}}$$

* Uniformly distributed load:

$$\frac{wL^2}{12} \Rightarrow \frac{(2)(20)^2}{12} = \boxed{66.67 \text{ Kip-ft}}$$

* point load (not at mid):



(16)

Day: MTWTFSS

Date: ___/___/___

* For left end:

$$\frac{pab^2}{L^2} \Rightarrow \frac{(10)(12)(8)^2}{(20)^2} = \boxed{19.2 \text{ K.ft.}}$$

* For right end

$$\frac{pa^2b}{L^2} = \frac{(10)(12)^2(8)}{(20)^2} = \boxed{28.8 \text{ K.ft.}}$$

So the total moment at left end:

$$19.2 + 66.67 = \boxed{85.87 \text{ K.ft.}}$$

⇒ Similarly at right end

$$28.8 + 66.67 = \boxed{95.47 \text{ K.ft.}}$$

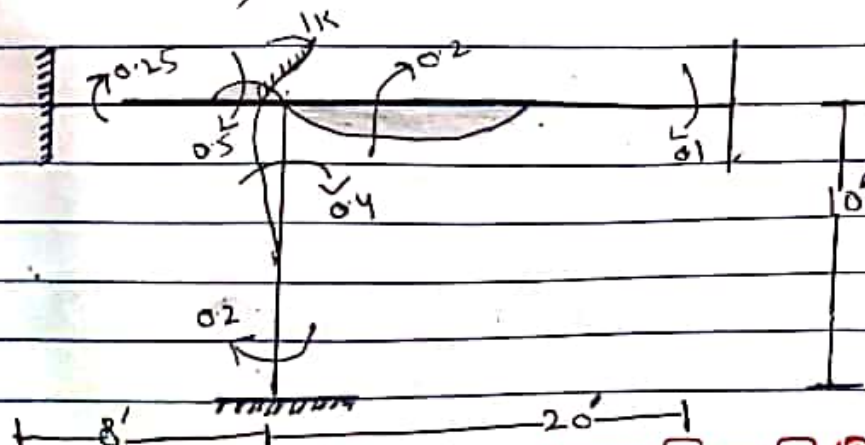
$$\text{So } [ADL] = -85.87 + 15 = \boxed{-70.87 \text{ K.ft.}}$$

Step #4

Determine [S] matrix

$$[S] = [S_{ij}]$$

Now, $D = 1K$



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$$\Rightarrow \frac{4\epsilon T}{8} = 0.5$$

$$\frac{2\epsilon T}{8} = 0.25$$

$$\frac{4\epsilon T}{20} = 0.2$$

$$\frac{2\epsilon T}{20} = 0.1$$

$$\frac{4\epsilon T}{10} = 0.4$$

$$\frac{2\epsilon T}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2)\epsilon T$$

$$= 1.1\epsilon T$$

$$[S] = 1.1\epsilon T$$

Step # 5

compute [D] matrix

$$[D] = [S]^{-1} \times [AD] - [AD]$$

$$[D] = \frac{1}{1.1} \times [0] - [-70.87]$$

$$= 70.87$$

$$[D] = [64.42] \frac{1}{\epsilon T}$$