

Department of Electrical Engineering
Final Assignment Summer 2020
Subject: Communication Systems

Max Marks: 50

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Question 1 (10)

A signal $x(t)$ band limited by 250 Hz is sampled by an impulse train with angular frequency of f_s

- a. Determine the Nyquist rate required for perfect reconstruction of signal.
- b. Considering $x(t)$ and impulse train in figure below, construct all the signals involved in sampling.
- c. Determine the cut off frequency of reconstruction filter $H(f)$ to be used for the signal given in question.
- d. If the frequency of sampler is $f_s = 800\text{Hz}$, draw the resulting sampled signal $s(t)$

Question 2 (10)

- a. Let $x(t)$ be a signal with Nyquist rate f_N , determine the Nyquist rate for following
 - i. $x(t) + x(t - 1)$
 - ii. $\frac{dx(t)}{dt}$
- b. Let $m(t) = 10 \sin 400\pi t$ is sampled at 300Hz and reconstructed using an ideal low pass filter with a cut off frequency of 150Hz. What are the frequency/frequencies present in the reconstructed signal $y(t)$

Question 3 (15)

Consider the bit sequence (0 1 1 0 1 1 0 0 0 1 1) and draw the PCM waveform for following modulation schemes

- a. NRZ-S
- b. Polar-RZ
- c. Split Phase Manchester
- d. Bi- ϕ -L
- e. Dicode - NRZ

Question 4 (15)

- a. A carrier wave is represented by the equation $e_c(t) = 7.5 \sin 20 \cdot 10^3 t$. If the modulation index of wave is 0.5, draw the waveform of AM modulated waveform.
- b. A sinusoidal carrier $10 \cos 50 \cdot 10^5 t$ is amplitude modulated by the sinusoidal voltage of

$\cos 628 \cdot 10^3 t$ over a load resistance of 50

- a. Find the depth of modulation and calculate the transmission efficiency
- b. Plot the AM wave in time domain as well as its frequency domain spectrum
- c. Calculate the total power in spectrum
- d. Calculate the percentage power in USB

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P#1

Q No. 1.

Given data.

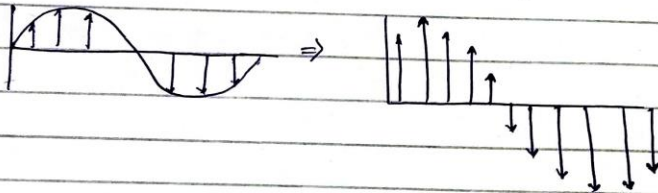
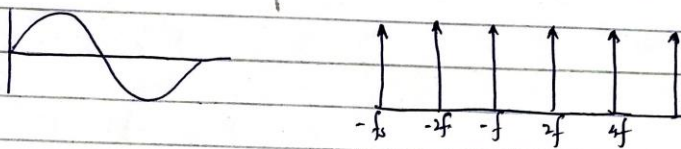
$$f_m = 250 \text{ Hz}$$

a) Nyquist Rate.

$$N_r > 2f_m.$$

$$= 2 \times 250 = 500 \text{ Hz.}$$

b)

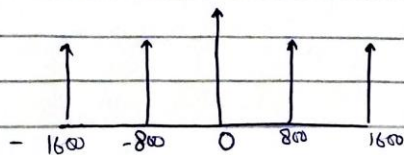


c) Cut off frequency.

$$f_c = \frac{1}{2\pi f R}$$

$$f_c = \frac{1}{2(3.14) 500} = 3.184 \times 10^{-4}.$$

d) $f_s = 800 \text{ Hz.}$



Q No 2

$$a) x(t) + x(t-1)$$

So:-

Nyquist rate = $2 \times$ maximum signal frequency

\Rightarrow Sampling rate must exceed Nyquist rate in order to be able to fully reconstruct the signal

$$a) y(t) = x(t) + x(t-1)$$

$$\text{Fourier transform } y(j\omega) = j\omega x(j\omega)$$

The Max frequency for $y(j\omega)$

The min frequency is $y(j\omega)$

is the same as $x(j\omega)$ then $y(t)$ Nyquist

$$ii) y(t) = x^2(t)$$

We can re write the above Fourier transform $y(j\omega) = j\omega x(j\omega)$

The Max frequency is $y(j\omega)$ is the same as $x(j\omega)$ then $y(t)$ Nyquist rate is ω_0 .

Q No 2

b:-

So:-

$$m(t) = 10 \sin 400\pi t$$

$$FM = \frac{\omega_m}{2\pi} = \frac{400\pi}{2\pi} = 200 \text{ Hz}$$

Frequency component of $y(t)$

first we calculate sample frequency
by formula

$$f_s + F_m$$

put different values of n

$$n = 0$$

$$f_s = |f_m = 0 \pm F_m = \pm f_m = \pm 200 \text{ Hz}$$

$$n = 1$$

$$F_s + F_m = \begin{cases} F_s + F_m - 300 + 200 = 100 \text{ Hz} \\ F_s - F_m - 300 - 200 = 500 \text{ Hz} \end{cases}$$

The cut off frequency is 150 Hz so
the frequency range from -150 Hz to
 $+150 \text{ Hz}$ will be pass

So frequency $+100 \text{ Hz}$ and -100 Hz is
the range so 100 Hz will be component
output.

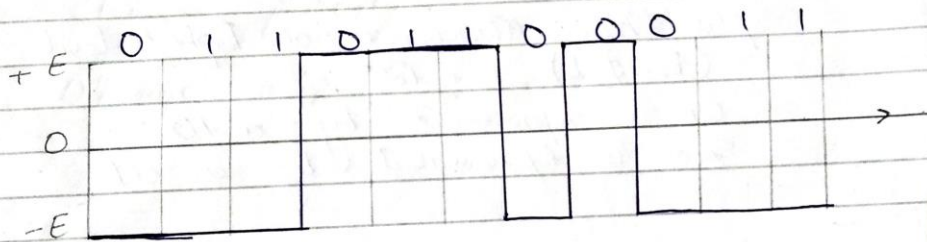
Q No 3:- Consider the bit sequence (01101100011) and draw the PCM waveform for the following Modulation schemes.

- NRZ-S
- Polar-RZ
- Split phase Manchester
- Bi- Φ -L
- Dicode-NRZ

Answer

a:-

NRZ-S

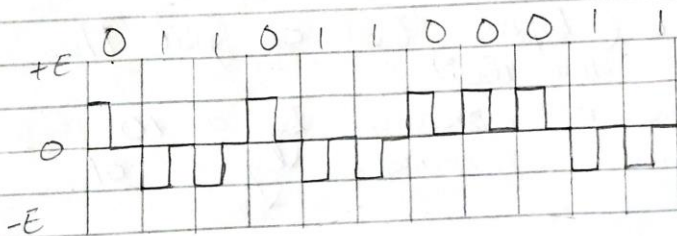


NRZ S

* "One" is represented by a no change in level.

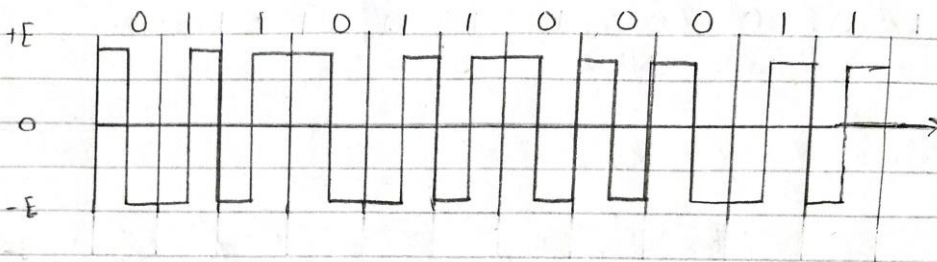
* "Zero" is represented by change in level.

b) Polar-RZ



One and zero are represented by opposite level polar pulses that have one half-bit in width.

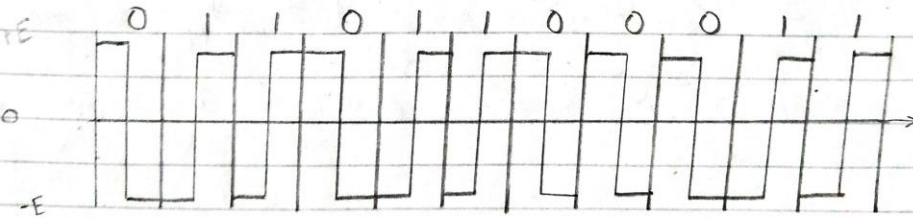
c). Split Phase Manchester.



Split Phase Manchester or Biphas Level
(Bi- ϕ -L) $11 + 180^\circ$.

One is represented by a 10
Zero is represented by a 01.

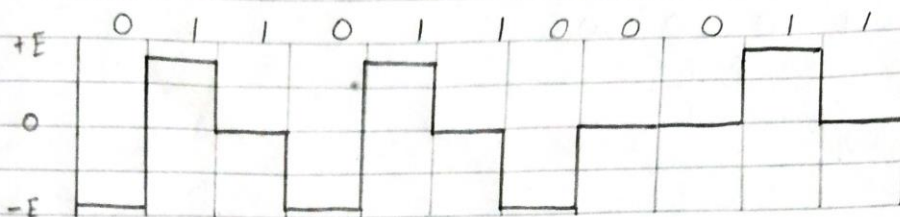
D). Bi- ϕ -L.



Bi- ϕ -L (Biphase level or Split Phase
Manchester $11 + 180^\circ$)

One is represented by a 10
Zero is represented by a 01.

e). Dicode - NRZ.



Dicode - NRZ

- A 'one' to 'zero' or 'zero' to 'One' changes polarity.
- Otherwise a 'zero' is sent.

Q No 4 a:

$$\underline{\text{So}} \quad E_c(t) = 7.5 \sin 20 \times 10^3 \pi t$$

$$E_M = 0.5$$

Draw AM modulation wave form

So let us evaluate E_m from E_c

$$m = \frac{E_m}{E_c}$$

Therefore

$$E_m = m \times E_c = 0.5 \times 7.5 \sin 20 \times 10^3 \pi t$$

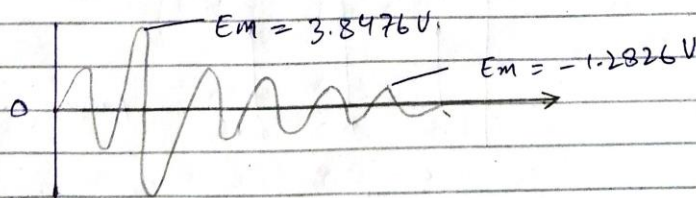
$$E_{\max} = E_c + E_m = 3.8476 \text{ V}$$

$$E_{\min} = E_c - E_m = 1.2826 \text{ V}$$

AM modulation:

The AM wave for $m = 0.5$ has shown in fig.

$$E_{\max} = 3.8476 \text{ V}$$



Q no. 4.

b)

a) Depth of modulation.

$$m = \frac{E_m}{E_c}$$

$$m = \frac{10V}{5V}$$

$$m = 2V.$$

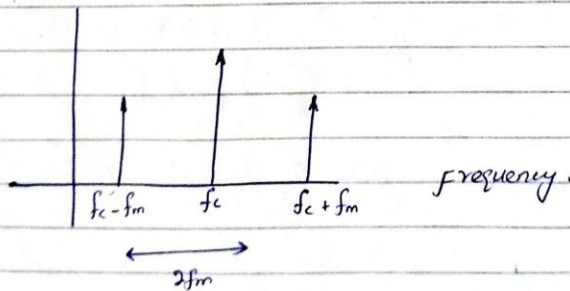
Transmission efficiency

$$\eta_f = \frac{m^2}{2 + m^2}$$

$$= \frac{(2)^2}{2 + 2^2}$$

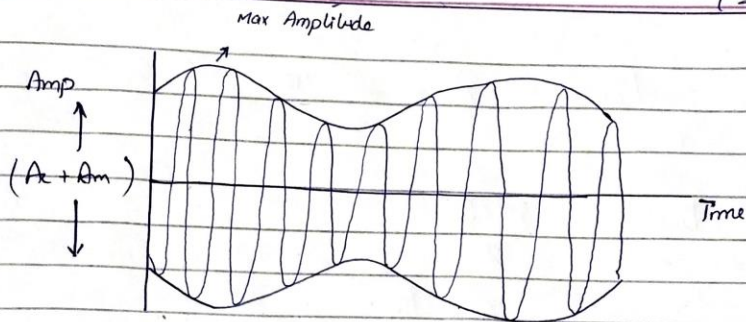
$$\eta_f = \frac{4}{6} = \frac{2}{3}$$

b).



Amplitude frequency.

P# 9



C. Power in Spectrum:-

$$P_c = \frac{E_c^2}{2R}$$

$$= \frac{(5)^2}{2 \times 50} = \frac{25}{100}$$

$$P_c = \frac{1}{4}$$

Total Power.

$$P_t \left(1 + \frac{m^2}{2}\right) P_c$$

$$= \left(1 + \frac{(0.2)^2}{2}\right) \times 0.2$$

$$= \left(1 + \frac{4}{2}\right) 0.2$$

$$= (3) 0.2$$

$$P_t = 0.6$$

d) : Percentage Power in USB.

$$\begin{aligned}P_{USB} &= \frac{m^2 E_c^2}{8} \\&= \frac{m^2 P_c}{4} \\&= \frac{(2)^2}{4} \times 0.6 \\&= \frac{4}{4} \times 0.6\end{aligned}$$

$$P_{USB} = 0.6$$

