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DEPARTMENT : COMPUTER SCIENCE

PROGRAM : SOFTWARE ENGG

SEMESTER : 2ND

SECTION : A

SUBJECT : DISCRETE STRUCTURE

Question no 1

Which of the following are propositions ?

(a) is not a proposition. (It is a command, or imperative.)

(b) and

(c) yes, this is propositions.

(d) is not a proposition.

(e) yes this is proposition.

(f) is not a proposition

Question no 2

p is " $x < 50$ "; q is " $x > 40$ ".

Write as simply as you can:

(a) $x \geq 50$

(b) $x \leq 40$

(c) $40 < x < 50$

(d) $x < 50$ or $x > 40$. true.

(e) $x \geq 50$ Don't need to say

(b) (f) *in addition*, that $x > 40$ $x \geq 50$ and $x > 40$

QUESTION NO 3

(A)

(a) some people dislike maths

(B)

(b) The answer is not 2 or it is not 3

© The answer is not 2 and not 3

(C)

(d) No one in my class is tell and thin

Question no 4

Construct truth tables for:

(A) $\neg p \vee \neg q$

$\neg p$	q	$\neg p$	$\neg q$	$\neg p \vee \neg q$
T	T	F	F	F
T	F	F	T	T
F	T	T	F	T
F	F	T	T	T

(B) $q \wedge (\neg p \vee q)$

p	q	$\sim p$	$\sim p \vee q$	$q \wedge (\sim p \vee q)$
T	T	F	T	T
T	F	F	F	F
F	T	T	T	T
F	F	T	T	F

(C) $p \wedge (q \vee r)$

p	q	r	$q \vee r$	$p \wedge (q \vee r)$
T	T	T	T	T
T	T	F	T	T
T	F	T	T	T
T	F	F	F	F
F	T	T	T	F
F	T	F	T	F
F	F	T	T	F
F	F	F	F	F

(D) $(p \wedge q) \vee r$

p	q	r	$p \wedge q$	$(p \wedge q) \vee r$
T	T	T	T	T
T	T	F	T	T
T	F	T	F	T
T	F	F	F	F
F	T	T	F	T
F	T	F	F	F
F	F	T	F	T
F	F	F	F	F

Question no 5

Use truth tables to show that:

$$\neg((p \vee \neg q) \vee (r \wedge (p \vee \neg q))) \equiv \neg p \wedge q$$

P	q	r	$\sim p$	$\sim q$	$(p \vee \sim q)$	$r \wedge (p \vee \sim q)$	$(p \vee \sim q) \vee (r \wedge (p \vee \sim q))$	$\sim((p \vee \sim q) \vee (r \wedge (p \vee \sim q)))$
T	T	T	F	F	T	T	T	F
T	T	F	F	F	T	F	T	F
T	F	T	F	T	T	T	T	F
T	F	F	F	T	T	F	T	F
F	T	T	T	F	F	F	F	T
F	T	F	T	F	F	F	F	T
F	F	T	T	T	T	T	T	F
F	F	F	T	T	T	T	T	F

p	q	$\sim p$	$\sim p \wedge q$
T	T	F	F
T	T	F	F
T	F	F	F
T	F	F	F
F	T	T	T
F	T	T	T
F	F	T	F

F	F	T	F
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Question no 6

Use the laws of logical propositions to prove that:

$$(z \wedge w) \vee (\neg z \wedge w) \vee (z \wedge \neg w) \equiv z \vee w$$

State carefully which law you are using at each stage

$$= (z \wedge w) \vee (z \wedge w) \vee (z \wedge \sim w) \vee (\sim x \wedge w) \quad \text{commutative law}$$

$$= (z \wedge (w \vee \sim w)) \vee (\sim z \wedge w) \quad \text{Distributive law}$$

$$= (x \wedge T) \vee (\sim z \wedge w) \quad \text{complement law}$$

$$= x \vee (\sim z \wedge w) \quad \text{identity law}$$

$$= (z \vee \sim z) \wedge (z \vee w) \quad \text{distributive law}$$

$$= T \wedge (z \vee w) \quad \text{complement law}$$

$$= (z \vee w) \wedge T \quad \text{commutative law}$$

$$= z \vee w \quad \text{identity law}$$

THE END