

Name = Tariq Bilal

Id = 13588

Class = Bs(cs)

Q4) If two fair dice are thrown, what is the probability of getting

1. A double six
2. A sum of 8 or more dots

Ans) When two fair dice is thrown, The possibilities are as below.

{  
(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),  
(2,1),(2,2),(2,3),(2,4),(2,5),(2,6),  
(3,1),(3,2),(3,3),(3,4),(3,5),(3,6),  
(4,1),(4,2),(4,3),(4,4),(4,5),(4,6),  
(5,1),(5,2),(5,3),(5,4),(5,5),(5,6),  
(6,1),(6,2),(6,3),(6,4),(6,5),(6,6),  
}

So, For getting 6 in both dices, The probability is  $1/36$ .

And, For getting sum of 8, It can be (2,6),(3,5),(4,4),(5,3),(6,2) and It is  $5/36$ .

Q1)

Ans) x.	f
360-369.	2
370-379.	3
380-389.	5
390-399.	7
400-409.	5
410-419.	4
420-429.	3
430-439.	1

Total. 30

$$\text{mean} = \frac{\sum f. m}{\sum f}$$

Grade.	F.	midpoint	f. m. c. f
360-369.	2.	364.	728
370-379.	3.	374.5.	1122
380-389.	5.	384.5.	1922.5
390-399.	7.	394.5.	2758
400-409.	5.	404.5.	2022
410-419.	4.	414.5.	1658
420-429.	3.	424.5.	1273
430-439.	1.	434.5.	434.5

$$\text{Mean} = \frac{\sum fm}{\sum f}$$

$$= 11918 / 30$$

$$= 397.2$$

Mode =

$$L=390, f_1=7, f_0=5, f_2=5, h=9$$

$$\text{Mode} = l + \frac{(f_1 - f_0)}{2f_1 - f_0 - f_2} * h$$

$$\text{Mode} = 390 + \frac{(7-5)}{2(7)-5-5} * 9$$

$$\text{Mode} = 390 + (0.5) * 9$$

$$\text{Mode} = 394.5$$

$$\text{Median} = L + \left( \frac{n/2 - F}{f} \right) * c$$

$$\text{Median} = 400 + (4.6) * 9$$

$$\text{Median} = 441.4$$

Quartiles

$$Q_1 = 370-379$$

$$Q_2 = 400-409$$

$$Q_3 = 420-429$$

Q3)

Ans)

$$1. \text{ Variance} = \sigma^2 = \sum (x - \bar{x})^2 / n$$

$$\text{Variance} = 94(826.5 - 196)^2 / 7$$

$$\text{Variance} = 94(391530) / 7$$

$$\text{Variance} = 5338260$$

$$\text{Standard deviation} = \sqrt{\text{variance}}$$

$$\text{Standard deviation} = \sqrt{5338260}$$

$$\text{Standard deviation} = 2310.4614$$

Q5)

Let  $C_1, C_2, \dots, C_M$  be a partition of the sample space  $SS$ , and  $A$  and  $B$  be two events. Suppose we know that

- $A$  and  $B$  are conditionally independent given  $C_i$ , for all  $i \in \{1, 2, \dots, M\}$
- $B$  is independent of all  $C_i$ 's.

Prove that  $A$  and  $B$  are independent.

Ans)

$A$  and  $B$  are conditionally independent

$C_1, C_2, \dots, C_M$  be a partition of the sample space.  $A$  and  $B$  are two events.

$A$  occur separately and  $B$  occur separately it is a separate events.

$C_1, \dots, C_M$  are partition of the sample space.  $C$  are the sample space and  $A, B$  are events. Events are separate from samples.

Events are always separate from the sample. Events occur after sample and  $A$  and  $B$  are independent to each other.

Hence it is proved  $A$  and  $B$  are independent.

Q5) By multiplying each of the numbers 3, 6, 2, 1, 7, 5 by 2 and then adding 5, we obtain 11, 17, 9, 7, 19, 15. What is the relation between the standard deviation and the means of the two sets.

Ans) means =  $\sum x/n$

$$\text{Mean} = 24/6$$

$$\text{Mean} = 4$$

$$\text{Mean} = 78/6$$

Mean = 13

$$\bullet \sigma^2 = \sum (x - \bar{x})^2 / n$$

$$\text{variance} = (78 - 13) / 6$$

$$\text{variance} = 4225 / 6$$

$$\text{variance} = 704$$

$$\text{standard deviation} = \sqrt{\text{variance}}$$

$$\text{standard deviation} = \sqrt{704}$$

$$\text{standard deviation} = 26.53$$

the standard deviation of the two sets is double of its 2<sup>nd</sup> set mean.

So the standard deviation is double of the 2<sup>nd</sup> mean.

And 1<sup>st</sup> mean is smaller than 2<sup>nd</sup> mean.