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Section :- A

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Subject :- MOS - II

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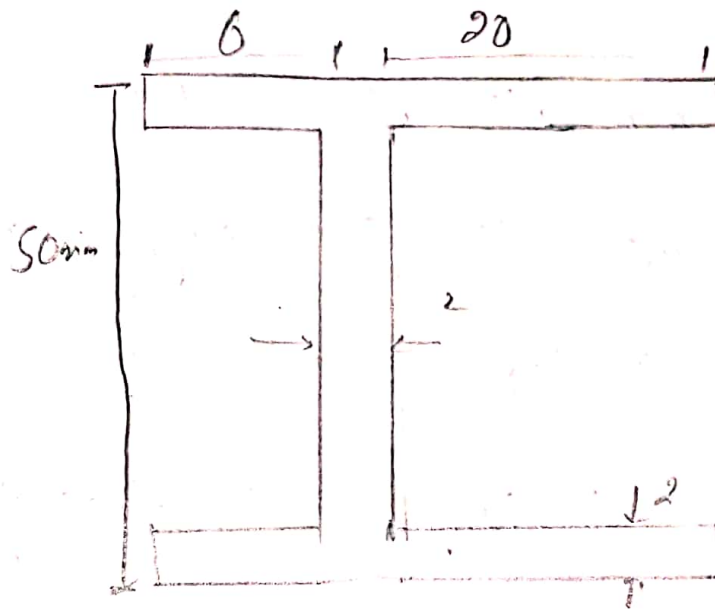
Teacher :- Sir Saqib



Q. No 1) (C102) (15)

①

Solution:-



As Given that

Height of section = 50 mm.

Thickness =  $b + 20$

$$b = 26 \text{ mm}$$

So,  $T_f = 2 \text{ mm}$ .

Required:-

②

Shear Centre = ?

As we know that

for unsymmetrical members, the shear centre is <sup>at</sup> some distance away from that geometrical center.

This distance is called eccentricity which is given as;

$$e = \frac{T_F h^2 b^2}{4I}$$

Here  $I$  = moment of inertia and is given as

$$I = 2 \left( \frac{bh^3}{12} + Ay^2 \right) + \left( \frac{bh^3}{12} + Ay^2 \right)$$

$$\Rightarrow I = 2 \left[ \frac{26(2)^3}{12} + (20 \times 2)(25)^2 \right] + \left( \frac{2(50)^3}{12} + 0 \right)$$

③

$$\bar{I} = 50034.66 + 20833$$

$$I = 70867.99 \text{ mm}^4$$

Now eq ①  $\Rightarrow$

$$e = \frac{T_f h^2 b^2}{4I}$$

$$e = \frac{2 \times (50)^2 \times (25)^2}{4(70867.99)}$$

$$e = 11.0234 \text{ mm}$$

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Shear center is 11.0234 mm away from geometrical center.



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Question # 01 part (b).

Answer:-

Given data:-

Height =  $h = 20 \text{ ft}$

assumed diameter =  $22 \text{ ft}$

specific weight of water tank =  $62.4 \text{ lb/ft}^3$

Tangential stress =  $600 \text{ lb/ft}$

Required data:-

Thickness of walls of water

tank = ?

Solution:-

The pressure develop by water is

given as

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$$P = \gamma h$$

$$\sigma_c = \frac{PD}{2t}$$

$$\sigma_c = \frac{PD}{2t} = \frac{\gamma h D}{2t}$$

$$\Rightarrow 2t \times \sigma_c = \gamma h D$$

$$2t = \frac{\gamma h D}{\sigma_c}$$

$$t = \frac{\gamma h D}{\sigma_c \times 2}$$

Put values

$$t = \frac{\left(\frac{62.4}{12}\right) \times (26 \times 12) \times (22 \times 12)}{600 \times 2}$$

$$t = \frac{270.4}{1200}$$

$$\Rightarrow t = 0.2253''$$

2. →

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Question NO 02 (a).

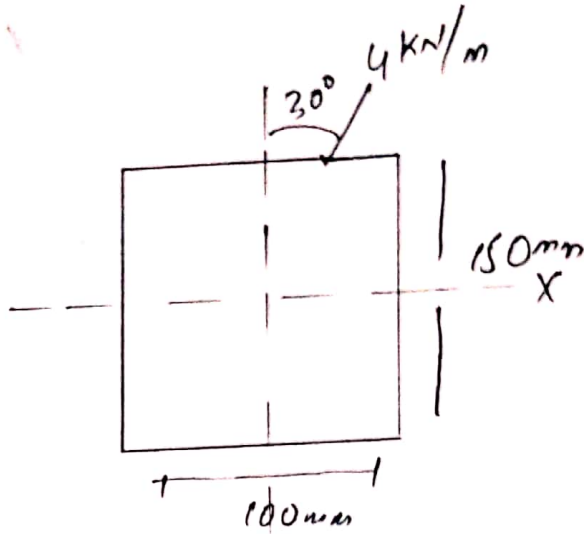
Given data:-

$$b = 100\text{mm}$$

$$h = 150\text{mm}$$

$$\text{load} = p = 4\text{ kN/m}$$

$$\text{Length of Beam} = 3\text{m}$$



Required:-

Bending Stress = ?

$$N.A = ?$$

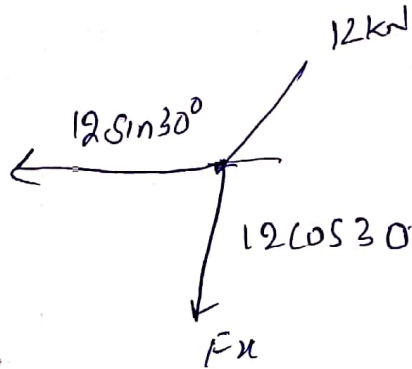
Now we know that

$$\sigma = \frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

$$\begin{aligned} \therefore M_z &= M \cos \theta \\ M_y &= M \sin \theta \end{aligned}$$

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$$\Rightarrow \delta = \frac{M \cos \theta}{I_z} + \frac{M \sin \theta}{I_y} \rightarrow \textcircled{P}$$



now

moment about x-axis

$$M_x = -11.8563 \times 3$$

$$M_z = -35.57 \text{ Nm}$$

$$M_y = 1.851 \times 3$$

$$M_y = 5.55 \text{ N.m.}$$

we know

$$m \cos \theta = p \cos \theta = M_z$$

$$\Rightarrow M \cos \theta = M_z$$



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$$m \sin \theta = P \sin \theta = m y$$

$$m \sin \theta = m y$$

Hence eq (1)  $\Rightarrow$

$$\delta = \frac{m \cos \theta}{I_z} + \frac{m \sin \theta}{I_y}$$

Now moment of inertia.

$$I_z = \frac{bh^3}{12} = 0.1 \frac{(0.15)^3}{12}$$

$$\Rightarrow I_z = 2.8125 \times 10^{-5} \text{ inch}^4$$

$$I_y = \frac{hb^3}{12} = 0.15 \frac{(0.2)^3}{12}$$

$$I_y = 1.25 \times 10^{-5}$$

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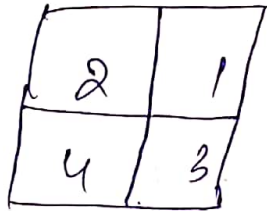
eq (a)  $\Rightarrow$

$$\delta = \frac{1.751}{2.712 \times 10^5} + \frac{-11.7563}{11.25 \times 10^6}$$

$$\delta = 882678 \text{ m}^2$$

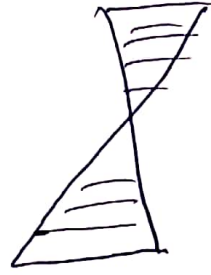
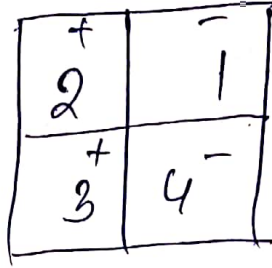
Neutral Axis (N.A):-

Sign Convention also.



$\Rightarrow$  If we take Compression as negative and tension as positive, then beam is simply supported

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In this case neutral axis pass 2 and 4.

Quadrant

→ In unsymmetrical loading case the neutral axis lies on angle of  $\alpha$  which is given by.

$$\tan \alpha = \frac{I_z}{I_y} \tan \theta$$

$$\tan \alpha = \frac{2 \cdot 2125 \times 10^{-5}}{1.25 \times 10^{-3}} (\tan 30^\circ)$$

$$\tan \alpha = 14.4124$$

$$\alpha = \tan^{-1}(-14.4129)$$

$$\boxed{\alpha = 1^\circ 30' 5''} \quad \longleftrightarrow$$

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QUESTION #02(b).

SOLUTION:

Given data:

Length of beam

$$L = 16 \text{ ft}$$

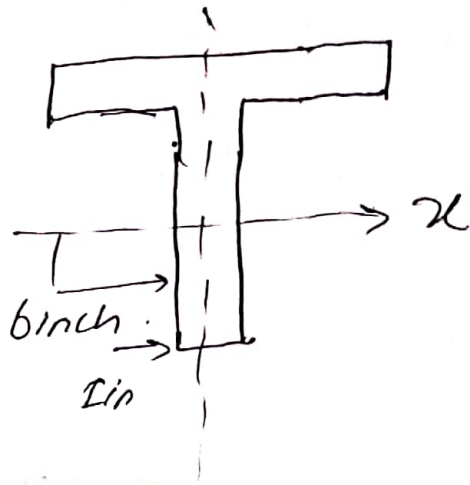
$$I_x = 112 \cdot b \text{ in}^4$$

$$I_y = 18.7 \text{ in}^4$$

$$\sigma_c = 12000 \text{ psi}$$

$$\sigma_t = 5000 \text{ psi}$$

From given figure the maximum compression would occur on 'a' and maximum tension at B.



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The tension and Compression will reduce the effect of each other.

So stress should be calculated at 'A' and 'C'.

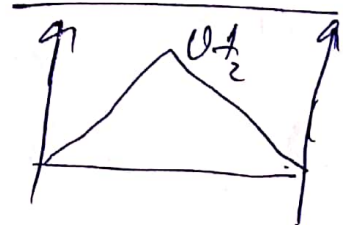
$$\text{So, } \sigma_A = \frac{m_x y}{I_x} + \frac{m_y x}{I_y} \text{ (Compression)}$$

$$\sigma_C = \frac{m_x y}{I_x} + \frac{m_y x}{I_y} \text{ (Tension)}$$

$$\text{So, } m_x = \frac{P \cos(60^\circ) (16 \times 12)}{4}$$

$$m_x = 43 \cos 60^\circ$$

$$m_y = \frac{P \sin(60^\circ) (16 \times 12)}{4}$$



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$$[m_y = 48 \cdot \sin 60^\circ]$$

$$\delta_A = \frac{m_{xy}}{I_x} + \frac{m_{yx}}{I_y}$$

$$\Rightarrow 1200 = \frac{48 P \cos 60^\circ + 3 \cdot 0.7}{112.6}$$

$$P = 1638.626$$

and

$$\delta_c = \frac{m_{xy}}{I_z} + \frac{m_{yx}}{I_y}$$

$$5000 = \frac{48 P \cos 60^\circ \times (595)}{18.7}$$

$$\Rightarrow P = 2104.916$$

So, the maximum load 'P' which can be applied should not be greater than 1638.626.

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## QUESTION #03

Given data:-

$$\text{length} = 10\text{ft}$$

$$E = 10.3 \times 10^6$$

$$b = 0.75$$

$$h = 2$$

$$\text{Factor of safety} = 2.$$

Required:-

a) safe load at hinged = ?

b) safe load at fixed = ?

Solution:-

a) For hinged column.

$$(e = L)$$

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$$I = I_x = \frac{(0.75)(2)^3}{12} = 0.5 \text{ in}^4$$

$$P_{cr} = \frac{n^2 E I \pi^2}{L^2}$$

$$P_{cr} = \frac{(1)^2 (10.3 \times 10^6)(0.5) \pi^2}{(10 \times 12)^2}$$

$$P_{cr} = \frac{50776940}{14400} = 3526.176 \text{ lb}$$

$$P_{\text{safe load}} = \frac{P_{cr}}{\text{Factor of safety}} = \frac{3526.176}{2} = 1763.088 \text{ lb}$$

Strut at column :-

$$L_c = \frac{L}{2} \text{ (For fixed ended)}$$



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$$L_e = \frac{10}{2} = 5 \text{ ft}$$

$$I = I_y = \frac{2 \times (0.75)^3}{12} = 0.07 \text{ in}^4$$

$$P_{cr} = \frac{n^2 \pi^2 EI A^2}{L_e^2} = \frac{(1)^2 (10.3 \times 10^8) (0.07) (3.14)^2}{(5 \times 12)^2}$$

$$P_{cr} = \frac{7108771.6}{(60)^2}$$

$$P_{cr} = 1974.65826$$

$$P_{\text{safe load}} = \frac{1974.658}{2}$$

$$P_{\text{safe load}} = 987.329 \text{ lb}$$

