

**Department of Electrical Engineering**  
**Assignment**  
**Date: 07/05/2020**

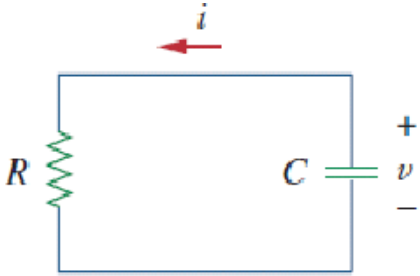
**Course Details**

<b>Course Title:</b> Electrical Network Analysis	<b>Module:</b> <u>4th</u>
<b>Instructor:</b> _____	<b>Total</b> <u>20</u>
<b>Submission Deadline</b> 05/06/2020	<b>Marks:</b> _____

**Student Details.**

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**Student Signature:** \_\_\_\_\_

Q1.	<p>For the circuit in Fig. 1, if <math>v = 10e^{-4t}</math> V and <math>i = 0.2e^{-4t}</math>, <math>t &gt; 0</math></p> <p>(a) Find <math>R</math> and <math>C</math>.</p> <p>(b) Determine the time constant.</p> <p>(c) Calculate the initial energy in the capacitor.</p> <p>(d) Obtain the time it takes to dissipate 50 percent of the initial energy.</p> <div style="text-align: center; margin: 10px 0;">  </div> <p style="text-align: center;">Figure 1</p>	<p>Marks 02</p> <hr style="border: 0.5px solid black;"/> <p>CLO 01</p>
Q2.	<p>A 120-V dc generator energizes a motor whose coil has an inductance of 50 H and a resistance of 100 Ω. A field discharge resistor 400 Ω of is connected in parallel with the motor to avoid damage to the motor, as shown in Fig. 2. The system is at steady state. Find the current through the discharge resistor 100 ms after the breaker is tripped.</p>	<p>Marks 03</p> <hr style="border: 0.5px solid black;"/> <p>CLO 03</p>

Circuit breaker

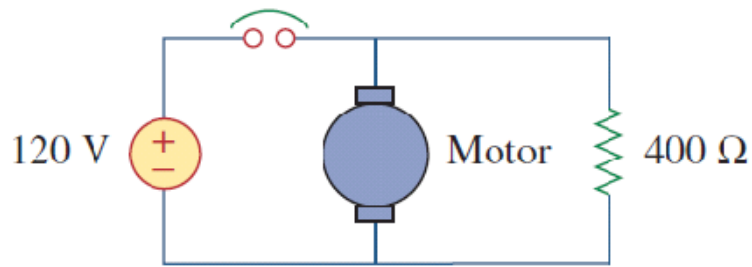


Figure 2

Q3.	<p>The responses of a series <math>RLC</math> circuit are</p> $v_c(t) = 30 - 10e^{-20t} + 30e^{-10t} \text{ V}$ $i_L(t) = 40e^{-20t} - 60e^{-10t} \text{ mA}$ <p>where <math>v_c</math> and <math>i_L</math> are the capacitor voltage and inductor current respectively. Determine the values of <math>R</math>, <math>L</math>, <math>C</math></p>	Marks 02
		CLO 01
Q4.	<p>The circuit in Fig. 3 is the electrical analog of body functions used in medical schools to study convulsions. The analog is as follows:</p> <p><math>C_1</math> = Volume of fluid in a drug</p> <p><math>C_2</math> = Volume of blood stream in a specified region</p> <p><math>R_1</math> = Resistance in the passage of the drug from the input to the blood stream</p> <p><math>R_2</math> = Resistance of the excretion mechanism, such as kidney, etc.</p> <p><math>v_0</math> = Initial concentration of the drug dosage</p> <p><math>v(t)</math> = Percentage of the drug in the blood stream</p> <p>Find <math>v(t)</math> for <math>t &gt; 0</math> given that <math>C_1 = 0.5 \mu\text{F}</math>, <math>C_2 = 5 \mu\text{F}</math>, <math>R_1 = 5 \text{M}\Omega</math>, <math>R_2 = 2.5 \text{M}\Omega</math> and <math>v_0 = 60u(t) \text{ V}</math></p>	Marks 03
		CLO 03

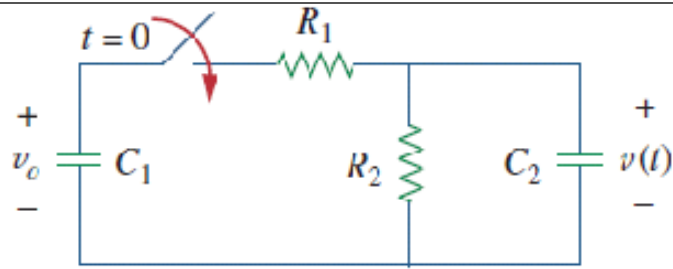


Figure 3

Q5.

A power transmission system is modeled as shown in Fig. 4. Given the source voltage and circuit elements

Source voltage  $V_s = 115 \angle 0^\circ \text{ V}$ ,

Source impedance  $Z_s = 1 + j0.5 \Omega$ ,

Line impedance  $Z_l = 0.4 + j0.3 \Omega$ ,

Load impedance  $Z_L = 23.2 + j18.9 \Omega$ ,

find the load current  $I_L$

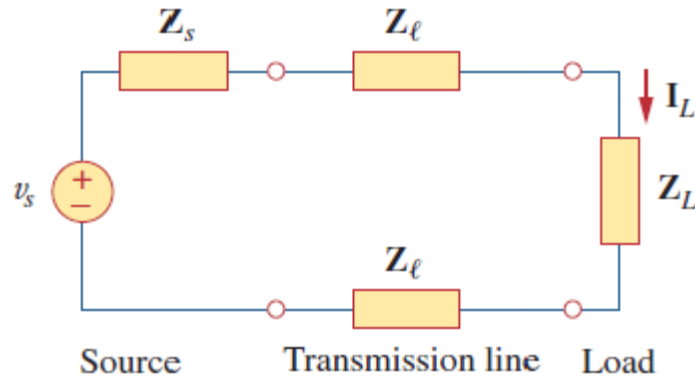


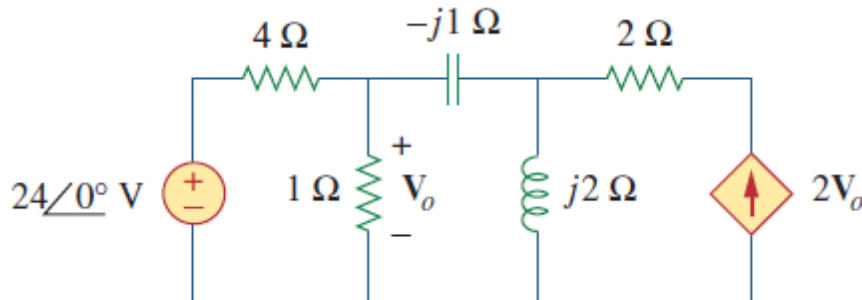
Figure 4

Marks  
02

CLO 03

Q 6

For the circuit in Fig. 5, find the average, reactive, and complex power delivered by the dependent current source.



Marks  
03

CLO 03

Figure 5

Q 7

A balanced Y-load is connected to a 60-Hz three-phase source with  $V_{ab} = 240 \angle 0^\circ$  V. The load has  $\text{pf} = 0.5$  lagging and each phase draws 5 kW. (a) Determine the load impedance  $Z_Y$ . (b) Find  $I_a$ ,  $I_b$ , and  $I_c$ .

Marks 5

CLO02

7.1: For the circuit in Fig 3,

$$i = 10e^{-4t} \text{ A} \quad \& \quad 0.2e^{-4t} \text{ V} \quad t > 0$$

(a) Find  $R$  &  $C$  (b) ... (c) ... (d) ...

So % of the initial energy.



Step 1

$$(A) \quad \tau = R_C = \frac{1}{4}$$

$$\Rightarrow -1 = C \frac{dv}{dt}$$

$$\Rightarrow -0.2e^{-4t} = C(10)(-4)e^{-4t}$$

$$\Rightarrow C = 5 \text{ mF}$$

$$R = \frac{1}{4C} = 50 \Omega$$

Step 2

$$(B) \quad \tau = R_C = \frac{1}{4} = 0.250$$

Step 3

$$(C) \quad W_C(0) = \frac{1}{2} C v^2$$

$$\Rightarrow \frac{1}{2} (5 \times 10^{-3}) (100)$$

$$\Rightarrow 250 \text{ mJ}$$

Step 4

$$(2) \quad W_R = \frac{1}{2} \times \frac{1}{2} C V_0^2$$

$$\Rightarrow \frac{1}{2} C V_0^2 (1 - e^{-\frac{2t_0}{\tau}})$$

$$0.5 = 1 - e^{-8t_0} \Rightarrow e^{-8t_0} = \frac{1}{2}$$

OR

$$e^{8t_0} = 2$$

$$t_0 = \frac{1}{8} \ln(2)$$

$$\Rightarrow 88.6 \text{ ms}$$

A 120V ac generator energize a motor whose coil  
 the breaker is tripped



Let the inductor current.

For  $t < 0$

$$i(0) = \frac{120}{100} = \frac{12}{10}$$

$$\Rightarrow \frac{6}{5} = 1.2 \text{ A}$$

For  $t > 0$  We have an RL circuit

$$\tau = \frac{L}{R} = \frac{50}{100+400}$$

$$\Rightarrow \frac{50}{500} \Rightarrow \frac{5}{50}$$

$$\Rightarrow \frac{1}{10} = 0.1$$

$$i(\infty) = 0$$

$$i(t) = i(\infty) + [i(0) - i(\infty)] e^{-t/\tau}$$

$$i(t) = 1.2 e^{-10t}$$

At  $t = 100 \text{ ms} = 0.1 \text{ s}$

$$i(0.1) = 1.2 e^{-1} = 0.441 \text{ A}$$

which is the same as the current through the resistor

(B)

$$T = R_{\text{rms}} = 60 \mu\text{s}$$

An integrator

$$\bullet T < 0.1 \quad \tau = 6 \mu\text{s}$$

$$T_{\text{max}} = 6 \mu\text{s}$$



Q3:- The response of a series RLC circuit are

Given data:

$$V_C(t) = 30 - 20e^{-20t} + 30e^{-10t} \text{ V}$$

$$i_L(t) = 40e^{-20t} - 60e^{-10t} \text{ mA}$$

where  $V_C$  and  $i_L$  are the capacitor voltage and inductor current respectively.

Determine the values  $R, L, C$

$S_1 = -20$  and  $S_2 = -20$  we have

$$S_{1,2} = -\alpha \pm \sqrt{\alpha^2 - \omega_d^2} = -20, -20$$

$$S_1 + S_2 = -2\alpha = -30 \text{ or } \alpha = 15$$

$$= R/(2L) \text{ or } R = 60L \rightarrow$$

$$S_2 = -15 + \sqrt{15^2 - \omega_d^2} = -20 \text{ which leads to}$$

$$15^2 - \omega_d^2 = 25$$

$$\text{or } \omega_d = \sqrt{225 - 25} = \sqrt{200} = 10\sqrt{2} / \sqrt{LC}$$

$$\text{thus } LC = 1/200 \rightarrow \text{(ii)}$$

$$i_L = i_C = C dv_C / dt$$

$$i_L / C = dv_C / dt = [200e^{-20t} - 300e^{-30t}]$$

$$\text{or } i_L = 200C [2e^{-20t} - 3e^{-30t}]$$

But  $i$  is also

$$= 20 \left( [2e^{-20t} - 3e^{-30t}] \times 10^{-3} \right)$$

$$= 2000 [2e^{-20t} - 3e^{-30t}]$$

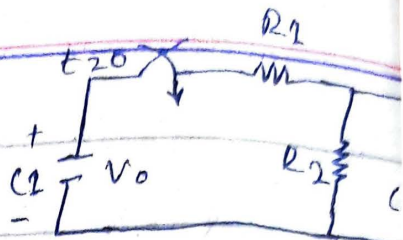
Therefore  $C = (0.02 / 10^2)$

$$= 200 \mu\text{F}$$

$$L = i / (2000) = 25 \text{ H}$$

$$R = 30L = 750 \text{ ohms}$$

Q4:-



sol  
}

$$(v_0 - v/R_1 = (v/R_2) + C_2 dv/dt)$$

$$v_0 = v (1 + R_1/R_2) + R_1 C_2 dv/dt$$

$$60 = (1 + 5/2.5) + (5 \times 10^6 \times 5 \times 10^{-6}) dv/dt$$

$$60 = 3v + 25 dv/dt$$

$$v(t) = v_1 + [A e^{-3t/25}]$$

where  $3v_0 = 60$  yields  $v_1 = 20$

$$v(0) = 20 = 20 + A \text{ or } A = 0$$

$$v(t) = 20 (1 - e^{-3t/25}) \text{ V}$$

Q5 :- A power ~~transmission~~ tra  
 system is modeled as  
 in Fig. 4 Given the source  
 voltage and circuit ele

Given data

$$V_s = 115 \angle 0^\circ \text{ V}, \text{ Source}$$

$$Z_s = 1 + j0.5 \Omega, \text{ line Im}$$

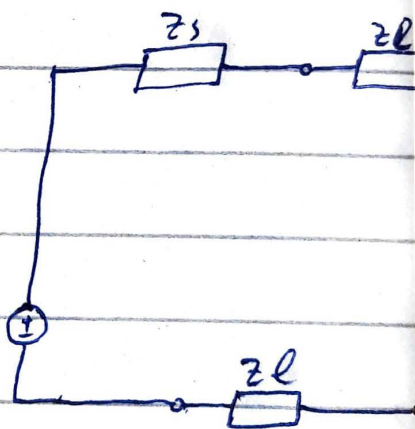
$$Z_l = 0.4 + j0.3 \Omega, \text{ and } l$$

Impede

$$Z_L = 23.2 + j18.9 \Omega,$$

Load Impedance

find load current  $I_L$



$$Z = Z_{s1} + 2Z_l + Z_L$$

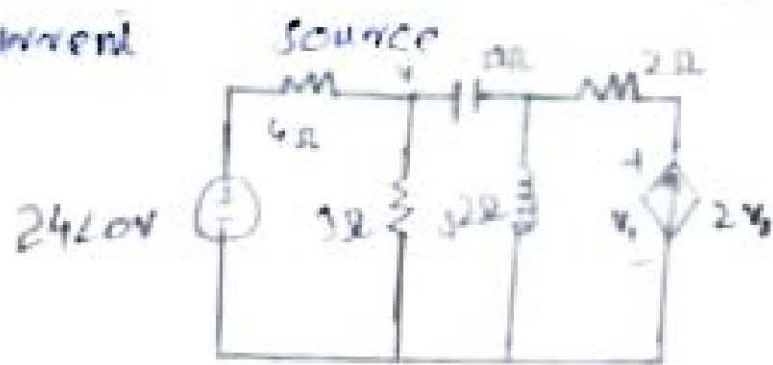
$$Z = (1 + 0.8 + 23.2) + j(0.5 + 0.6)$$

$$Z = 25 + j20$$

$$I_L = \frac{V_S}{Z} = \frac{295 \angle 0^\circ}{32.02 \angle 38.66^\circ}$$

$$I_L = 3.592 \angle -38.66^\circ \text{ A}$$

Q.6) For the circuit in Fig. 5 find the dependent current source



Consider the circuit as shown

At node 0

$$\frac{24 - V_0}{4} = \frac{V_0}{1} + \frac{V_0 - V_1}{-1}$$

$$24 = (5 + j4)V_0 - j4V_1 \rightarrow (1)$$

At node 1

$$\frac{V_0 - V_1}{-j} + 2V_0 = \frac{V_1}{j2}$$

$$V_1 = (2 - j4)V_0 \rightarrow (2)$$

Substituting (2) into (1)

$$24 = (5 + j4 - j8 + 16)V_0$$

$$V_0 = \frac{-24}{11 + j4}, \quad V_1 = \frac{(-24)(2 - j4)}{11 + j4}$$

Voltage across the dependent source is

$$V_2 = V_1 + (2)(24) = V_1 + 48$$

$$V_2 = \frac{-24}{11+j4} (2 - \cancel{4}j4 +) = \frac{(-24)(6-j4)}{11+j4}$$

$$S = \frac{1}{2} V_2 I^* = \frac{1}{2} V_2 (24^*)$$

$$S = \frac{(-24)(6-j4)}{11+j4} \cdot \frac{-24}{11-j4}$$

$$= \left( \frac{576}{137} \right) (6-j4)$$

$$S = 25.23 - j16.82 \text{ VA}$$

A balanced Y-load to a 60Hz three phase \_\_\_\_\_ phase draw 5KW.

(a) Determine the load impedance  $Z$

(b) Find  $I_a$ ,  $I_b$  &  $I_c$ .

(a) Step 1

$$|V_{ab}| = \sqrt{3}V_p = 240 \rightarrow V_p = \frac{240}{\sqrt{3}} = 138.56$$

$$V_{an} = V_p \angle -30^\circ$$

$$P_f = 0.5 = \cos\alpha \rightarrow \alpha = 60^\circ$$

$$P = S \cos\alpha \rightarrow S = \frac{P}{\cos\alpha} = \frac{5}{0.5} = 10 \text{ KVA}$$

$$Q = S \sin\alpha = 10 \sin 60 = 8.66$$

$$S_p = 5 + j8.66 \text{ KVA}$$

But

$$S_p = \frac{V_p^2}{Z_p} \rightarrow Z_p = \frac{V_p^2}{S_p} = \frac{138.56^2}{(5 + j8.66) \times 10^3}$$

$$= 0.96 - j1.663$$

$$Z_p = 0.96 + j1.663 \Omega$$

(100)

$$I_a = \frac{V}{Z_r} = \frac{138.56 \angle -30^\circ}{0.96 + j1.6627} = 72.17 \angle -90^\circ \text{ A}$$

$$I_b = I_a \angle -120^\circ = 72.17 \angle -210^\circ \text{ A}$$

$$I_c = I_a \angle +120^\circ = 72.17 \angle 30^\circ \text{ A}$$