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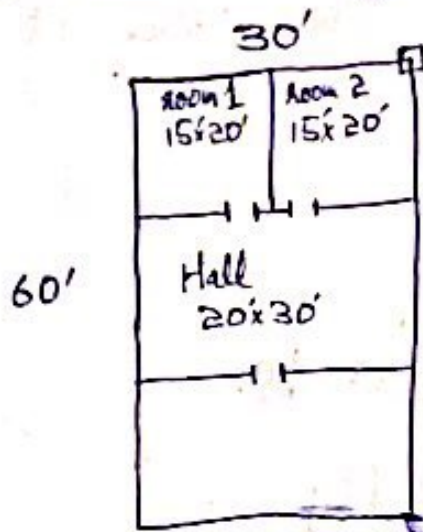
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MS (CEM)

Subject: Advanced design of reinforced concrete structures.

Instructor: Engr. Fawad Ahmad.

Architectural design of structure (6.6 marla)

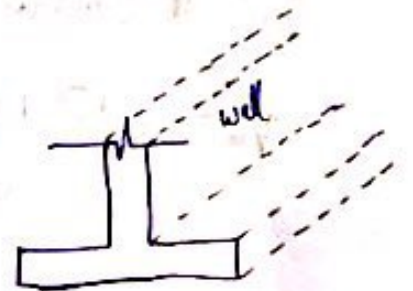
Design of wall footings

wall = 12" wide

D.L = 20 k/ft, L.L = 15 k/ft

 $\gamma_s = 100 \text{ lb/ft}^3$, $q_a = 4 \text{ ksf} = 4000 \text{ psf}$ $f_c' = 3 \text{ ksi} = 3000 \text{ psi}$, $f_y = 60,000 \text{ psi}$ $H_s = 4' - h_c$, $\gamma_c = 150 \text{ lb/ft}^3$, $h_c = 12"$ $d = 12 - 3.5 = 8.5"$

(code 7.7.1)



Step 1: Effective soil pressure q_e .

$$q_e = q_u - h_c \gamma_c - H_s \gamma_s \Rightarrow 4000 - \left(\frac{12}{12} \times 150\right) - (3 \times 100)$$

$$q_e = 3550 \text{ psf} = 3.55 \text{ ksf}$$

Step 2: Width of footing

$$W = \frac{D+L}{q_e} = \frac{20+15}{3.55} = 9.86 \approx 10'$$

Step 3: Depth required for shear at distance d from the face of wall.

$$d = \frac{V_u}{\phi 2\sqrt{f_c'} bw}$$

$$V_u = \left(\frac{10}{2} - \frac{6}{12} - \frac{0.5}{12}\right) \times q_u$$

q_u = ultimate bearing capacity

$$q_u = \frac{1.2 DL + 1.6 LL}{\text{width of footing}}$$

$$= \frac{1.2 \times 20 + 1.6 \times 15}{10}$$

$$q_u = 4.8 \text{ ksf}$$

Now $V_u = \left(\frac{10}{2} - \frac{6}{12} - \frac{0.5}{12}\right) \times 4.8$

$$V_u = 18.2 \text{ k} = 18200 \text{ lb}$$

$$d = \frac{V_u}{\phi 2\sqrt{f_c} bw} = \frac{18200}{0.75 \times 2\sqrt{3000} \times 12}$$

$$d = 18.46''$$

$$h = d + \text{cover} = 18.46'' + 3.5'' = 21.96''$$

21.96 > 12 not ok so try with greater.

Assume 20" footing

$$h = 20''$$

$$d = 20 - 3.5 = 16.5''$$

repeating step 1, 2 & 3

Step 1: Effective Soil pressure $\{q_e\}$

$$q_e = q_a - h_c \gamma_c - H_s \gamma_s = 4000 - \left(\frac{20}{12} \times 150\right) - \left(\frac{28}{12} \times 100\right)$$

$$q_e = 3517 \text{ psf} = 3.517 \text{ ksf}$$

Step 2: Width of footing

$$W = \frac{D+L}{q_e} = \frac{20+15}{3.517} = 9.95' \approx 10'$$

Step 3: Depth required for shear.

$$V_u = \left(10 \frac{1}{2} - 6 \frac{1}{2} - 16.5 \frac{1}{12}\right) \times q_u$$

$$V_u = \left(10 \frac{1}{2} - 6 \frac{1}{2} - 16.5 \frac{1}{12}\right) \times 4.8$$

$$V_u = 15 \text{ k}$$

$$q_u = 4.8$$

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$$d = \frac{V_u}{\phi 2\sqrt{f_c'} bw} = \frac{15000}{0.75 \times 2 \times \sqrt{3000} \times 12} = 15.21$$

$$h = 15.21 + 3.5 = 18.71'' \text{ use } 20'' \text{ total depth}$$

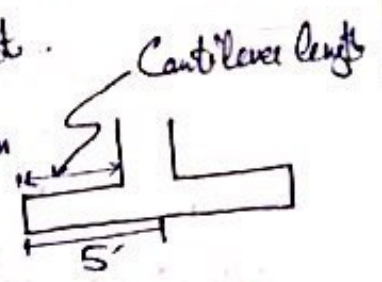
$$h = 20'' , d = 16.5''$$

Step 4: Determination of steel area (main)

$$\text{Cantilever length} = 10\frac{1}{2} - 6\frac{1}{2} = 4.5 \text{ ft.}$$

$$M_u = (\text{Cantilever length}) \times q_u \times \frac{1}{2} L \cdot \text{Area}$$

$$= 4.50 \times 4.80 \times \frac{4.50}{2}$$



$$M_u = 48.6 \text{ ft-k}$$

$$\frac{M_u}{\phi b d^2} = \frac{48.6 \times 1000 \times 12}{0.9 \times 12 \times (16.5)^2} = 198.3 \text{ psi}$$

Referring to Appendix A

$$\text{when } \frac{M_u}{\phi b d^2} = 198.3$$

then by interpolation $\rho = 0.00345$

$$A_s = \rho b d = 0.00345 \times 12 \times 16.5$$

$$A_s = 0.68 \text{ in}^2 \text{ refer to table A-6}$$

using #7 bar @ 10" c/c spacing

α_1	195.8
α_2	198.3
α_3	201.3
$y_2 = \frac{(\alpha_2 - \alpha_1)(y_3 - y_1) + y_1}{(\alpha_3 - \alpha_1)}$	
	$= \frac{(198.3 - 195.8)(0.0035 - 0.0034) + 0.0034}{201.3 - 195.8}$
	$y_2 = 0.00345$

Step 5 Longitudinal Temperature & Shrinkage steel.

$$A_s = \rho b d = 0.0018 \times 12 \times 20$$

$$A_s = 0.432 \text{ in}^2 \quad \text{using table A-b}$$

$$\#5 @ 8" \text{ c/c} \quad A_s \text{ selected} = 0.46 \text{ in}^2.$$

Step 6 Development length

$$\psi_t = \psi_c = \psi_s = 1 = 1$$

$$l_d/d_b = \frac{3}{40} \frac{\rho_y}{\sqrt{f_c}} \frac{\psi_t \psi_c \psi_s}{c_b/d_b} \quad \text{--- (1)}$$

if $c_b/d_b > 2.5$ then use 2.5

$$c_b = \text{side cover} = 3.5"$$

$$d_b = \text{dia of main bar} = 7/8 = 0.875"$$

$$c_b/d_b = 3.5/0.875 = 4 > 2.5 \quad \text{So } c_b/d_b = 2.5$$

using eq (1)

$$l_b/d_b = \frac{3}{40} \times \frac{60000}{\sqrt{3000}} \times \frac{1 \times 1 \times 1}{2.5}$$

$$l_b/d_b = 32.86$$

$$= \frac{A_s \text{ req}}{A_s \text{ selected}} = 32.86 \times 0.14$$

$$l_d = 31.03 \times 0.875 = 27.$$

$$\text{Say } l_d = 28"$$

Design of square column footing

Step 1: Effective soil pressure q_e

$$q_e = q_a - h_c \gamma_c - H_s' \times \gamma_s$$

$$= 5000 - (24/12 \times 150) - (36/12) \times 100$$

$$q_e = 4400 \text{ psf} = 4.4 \text{ ksf}$$

$$\boxed{q_e = 4.4 \text{ ksf}}$$

Step 2: Area of footing.

$$\text{Area of footing} = \frac{P_D + P_L}{q_e} = \frac{200 + 160}{4.4} = 81.82 \text{ ft}^2$$

$$\text{use } 9' \times 9' \text{ footing area} = 81 \text{ ft}^2$$

Step 3: Ultimate Bearing Capacity

$$q_u = \frac{1.2 P_D + 1.6 P_L}{\text{Area of footing}} = \frac{(1.2 \times 200) + (1.6 \times 160)}{81}$$

$$\boxed{q_u = 6.12 \text{ ksf}}$$

Step 4: Depth required for two way or punching shear

$$i) d = \frac{V_{u2}}{\phi 4 \sqrt{f_c'} b_o}$$

$$ii) d = \frac{V_{u2}}{\phi \left(\frac{\alpha_s d}{b_o} + 2 \right) \sqrt{f_c'} b_o}$$

 b_o = perimeter around the punching area = $4(a+d)$

$$b_o = 4(a+d) = 4(16+19.5)$$

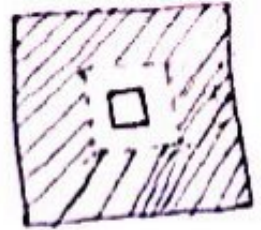
$$\boxed{b_o = 142 \text{ in}}$$

$$V_{u2} = \{A - (a+d)\} \times q_u$$

$$V_{u2} = \left\{ 81 - \left(\frac{16+19.5}{12} \right) \right\} \times 6.12$$

$$V_{u2} = 442.09 \text{ K} = 442090 \text{ lb}$$

$$V_{u2} = 442090 \text{ lb}$$



$$(1) \quad d = \frac{V_{u2}}{\phi 4 \sqrt{f_c'} b_o} = \frac{442090}{0.75 \times 4 \sqrt{3000} \times 142} = 18.95'' < 19.5 \text{ (OK)}$$

$$(2) \quad d = \frac{V_{u2}}{\phi \left(\frac{a \cdot s_d}{b_o} + 2 \right) \sqrt{f_c'} b_o} = \frac{442090}{0.75 \left(\frac{40 \times 19.5}{142} + 2 \right) \sqrt{3000} \times 142} = 10.12'' < 19.5'' \text{ (OK)}$$

both values of d are less than 19.5"
 so punching shear is OK

Step 5: Depth required for one way shear.

$$V_{u1} = (9 \times 2.208) \times q_u$$

$$= (9 \times 2.208) \times 6.12$$

$$V_{u1} = 121.62 \text{ K} = 121620 \text{ lb}$$

$$d = \frac{V_u}{\phi 2 \sqrt{f_c'} b_w} = \frac{121620}{0.75 \times 2 \times \sqrt{3000} \times 9 \times 12}$$

$$d = 13.71'' < 19.5 \text{ OK}$$

use $h = 24''$ in total depth

Moments $M_{u1} = 3.83 \times 9 \times 6.12 \times \frac{3.83}{2}$

$$= 404 \text{ ft-K}$$

$$M_u = \frac{404 \times 1000 \times 12}{0.9 \times (9 \times 12) \times (19.5)^2} = 131.2 \text{ psi}$$

$$\frac{M_u}{\phi b d^2} = 134.3$$

then use greater of

$$(1) \frac{200}{60,000} = 0.0033$$

$$(2) \frac{3\sqrt{3000}}{60,000} = 0.00274$$

$$\text{So } f = 0.0033$$

Area of steel

$$A_s = f b d$$

$$= 0.0033 \times (9 \times 12) \times 19.5$$

$$A_s = 6.95 \text{ in}^2$$

use table A-4 9#8 bar in both direction

Development lengths

$$l_d/d_b = \frac{3}{40} \frac{f_y}{\sqrt{f_c}} \frac{4\epsilon}{c_b/d_b} \quad (1)$$

if $c_b/d_b > 2.5$ then use 2.5

$$c_b/d_b = \frac{3.5}{1} = 3.5 > 2.5 \text{ so use } 2.5$$

using eq (1)

$$l_d/d_b = \frac{3}{40} \times \frac{60,000}{\sqrt{3000}} \times \frac{1 \times 1 \times 1}{2.5} = 32.86$$

$$l_d/d_b \frac{A_s \text{ req}}{A_s \text{ sel}} = 32.86 \times \frac{6.95}{7.07} = 32.30$$

$$l_d = 32.30 \times d_b = 32.30 \times 1$$

$$\boxed{l_d = 32"} \quad \text{OK}$$

Design of Columns

Assume the column will have an average compression stress = about $0.6 f'_c = 2400 \text{ psi} = 2.4 \text{ ksi}$

$$A_g \text{ required} = \frac{600 \text{ k}}{2.4 \text{ ksi}} = 250 \text{ in}^2$$

Try 16×16 column ($A_g = 256 \text{ in}^2$) with the bar arrangement

shown in A_g

$$e = \frac{M_u}{P_u} = \frac{(12 \text{ in/ft})(80 \text{ ft-k})}{600 \text{ k}} = 1.60 \text{ in}$$

$$P_n = \frac{P_u}{\phi} = \frac{600 \text{ k}}{0.65} = 923.1 \text{ k}$$

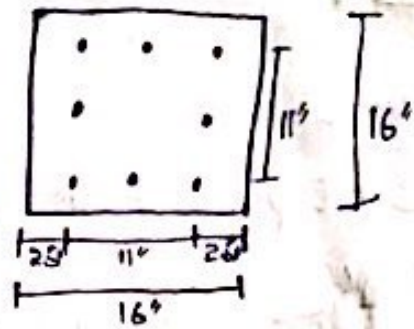
$$k_u = \frac{P_n}{f'_c A_g} = \frac{923.1 \text{ k}}{(4 \text{ ksi})(16 \times 16)} = 0.901$$

$$P_n = \frac{P_n e}{f'_c A_g h} = \frac{(923.1 \text{ k})(1.6 \text{ in})}{(4 \text{ ksi})(16 \times 16)(16)} = 0.901$$

$$r = \frac{11}{16} = 0.68$$

Interpolating ~~values~~ b/w values given in graphs

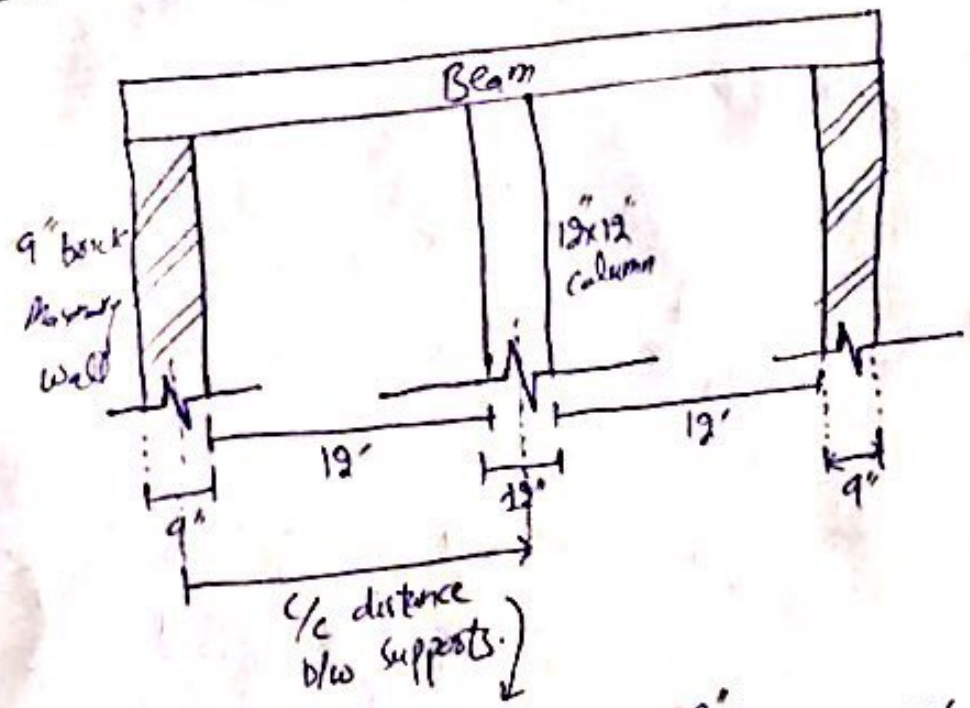
r	0.600	0.6875	0.700
ρ_g	0.025	0.023	0.022
A_s	$(0.023)(16)(16) = 5.89 \text{ in}^2$		
use	8 #8 bars = 6.28 in^2		



Notes

- a) Note that $\phi = 0.65$ as initially assumed since the graphs used show $f_s/f_y < 1.0$ & thus $\epsilon_t < 0.002$
- b) code requirements must be checked. ~~as~~ ~~is~~

BEAM DESIGN:



$$L = 12' + \frac{19'/2}{12} + \frac{9'/2}{12} = 12' + 0.5' + 0.375'$$

$$L = 12.875'$$

Exterior support = 9" brick masonry wall.

$$f_c' = 3 \text{ ksi} = 3000 \text{ psi}$$

$$f_y = 40 \text{ ksi} = 40,000 \text{ psi}$$

interior support \Rightarrow column support = 12" x 12"

Step 1:- $l = 12.875'$ (c/c distance b/w supports).

Size:- Minimum thickness of beam (ACI 9.5.2.1).
 $h_{min} = 1.5' = 18''$

$$\text{Also } h = \frac{l}{18.5} \left(0.4 + \frac{f_y}{100000} \right) = \frac{10.1503}{18.5} \left(0.4 + \frac{40000}{100000} \right) \times 12$$

$$h_{\text{actual}} = 6.68''$$

Also Table 4.1

$$h_{\text{actual}} = \frac{l}{28} = \frac{19.875}{28} = 0.46 \times 12 = 5.52''$$

So,

Minimum thickness $h_{\text{min}} \geq 7.5'' = 18''$ will govern.

$$\begin{aligned} \text{effective depth} = d &= h - 3 \\ &= 18 - 3 \\ &= 15'' \end{aligned}$$

Step # 02:- Loads.

$$d = 1.95'$$

Material	thickness (inch)	γ (Kcf)	Load = $\gamma \times \text{thickness}$
slab	5	0.15	$0.15 \times \frac{5}{12} = 0.0625$
Mud	4	0.12	$0.12 \times \frac{4}{12} = 0.04$
brick	2	0.12	$0.12 \times \frac{2}{12} = 0.02$

$$\text{Service D.L} = 0.0625 + 0.04 + 0.02 = 0.1225 \text{ Ksf.}$$

$$\text{Service L.L} = 40 \text{ psf} = 0.04 \text{ Ksf.}$$

Beam is supporting 5' slab per running foot
therefore, service D.L from slab = $0.1225 \times 5 = 0.6125 \text{ K/ft}$

Slab Design :

ACI Formulae for thickness of continuous one way slab ACI 9.5.2.

$$\text{one end continuous} = l/24$$

$$\text{both end continuous} = l/20$$

Assume 6" slab. Span length for end span of slab will be equal to clear span plus depth of member.

Slab thickness calculation according to ACI 9.5.2

one end continuous

$$l/24 \times \left(\frac{0.4 + \gamma}{100000} \right)$$

$$\Rightarrow 20/24 \times \left(\frac{0.4 + 40000}{100000} \right) \times 12 = 5"$$

both end continuous

$$l/20 \times \left(\frac{0.4 + \gamma}{100000} \right)$$

$$\Rightarrow 30/28 \times \left(\frac{0.4 + 40000}{100000} \right) \times 12 = 6"$$

Take slab thickness = 6" (ACI 9.5.2.1)

$$\text{Effective depth } (d) = h - 0.25 - (3/8) / 2 = 5" \text{ (\#3 main bar)}$$

⑤

3) At exterior mid span.

$$\begin{aligned}
 \text{Positive moment (+M}_{\text{ext}}) &= \text{Coefficient} \times (w_u l^2) \\
 &= (1/11) \times (0.214 \times 9.5^2) \\
 &= 1.755 \text{ ft-k/ft} = 21.06 \text{ in-k/ft.}
 \end{aligned}$$

4) At interior mid span.

$$\begin{aligned}
 \text{Positive moment (+M}_{\text{int}}) &= \text{Coefficient} \times (w_u l^2) \\
 &= (1/16) \times (0.214 \times 9^2) \\
 &= 1.08 \text{ ft-k/ft} = 13. \text{ in-k/ft}
 \end{aligned}$$

Step 2 : Loading :

$$\text{Service DL} = 0.075 + 0.03 + 0.02 \\ = 0.125 \text{ ksf}$$

$$\text{Service L.L} = 40 \text{ psf or } 0.04 \text{ ksf (per wall)}$$

$$\text{Service load} = \text{D.L} + \text{L.L} = 0.125 + 0.04 = 0.165 \text{ ksf}$$

$$\text{Factored load} = 1.2 \text{ DL} + 1.6 \text{ DL} \\ = 1.2 \times 0.125 + 1.6 \times 0.04 = 0.214 \text{ ksf}$$

Step 3 : Analysis :

One way slab

$$\textcircled{1} \text{ At interior support} \\ \text{Negative moment } (-M_{\text{int}}) = \text{coefficient} \times (w_u l^2) \\ = \left(\frac{1}{12}\right) \times (0.214 \times 9.5^2) \\ = 1.609 \text{ ft-k/ft} = 19.31 \text{ in-k/ft}$$

$$\textcircled{2} \text{ At interior support right.}$$

$$\text{Negative moment } (-M_{\text{int}}) = \text{coefficient} \times (w_u l^2) \\ = \left(\frac{1}{12}\right) \times (0.214 \times 9^2) \\ = 1.44 \text{ ft-k/ft} = 17.33 \text{ in-k/ft}$$

Moments:-

Negative moment = coefficient $\times w_u l_n^2$

$$M_{neg} = \frac{1}{9} \times (1.325 \times 12^2)$$

$$M_{neg} = 21.2 \text{ ft-K} \times 12$$

$$M_{neg} = 254.4 \text{ in-K}$$

Positive moment = coefficient $\times w_u l_n^2$

$$M_{pos} = \frac{1}{11} \times (1.325 \times 12^2)$$

$$M_{pos} = 17.34 \text{ ft-K} \times 12$$

$$M_{pos} = 208.14 \text{ in-K}$$

Step #4 \therefore Design (moment/flexure).

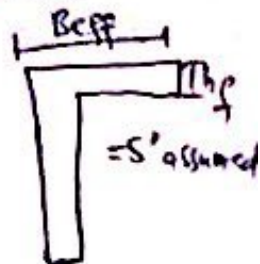
① For positive moment:-

According to ACI 8.10 \rightarrow b_{eff} for L-Beam
is minimum of.

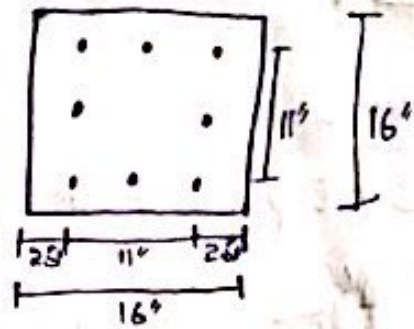
$$(i) 6b_f + b_w = 6(5) + 12 = 42''$$

$$(ii) b_w + \frac{\text{Span length of beam}}{12} = 12 + \frac{(12.875 \times 12)}{12} = 24.875''$$

$$\text{So, } b_{eff} = 24.875''$$

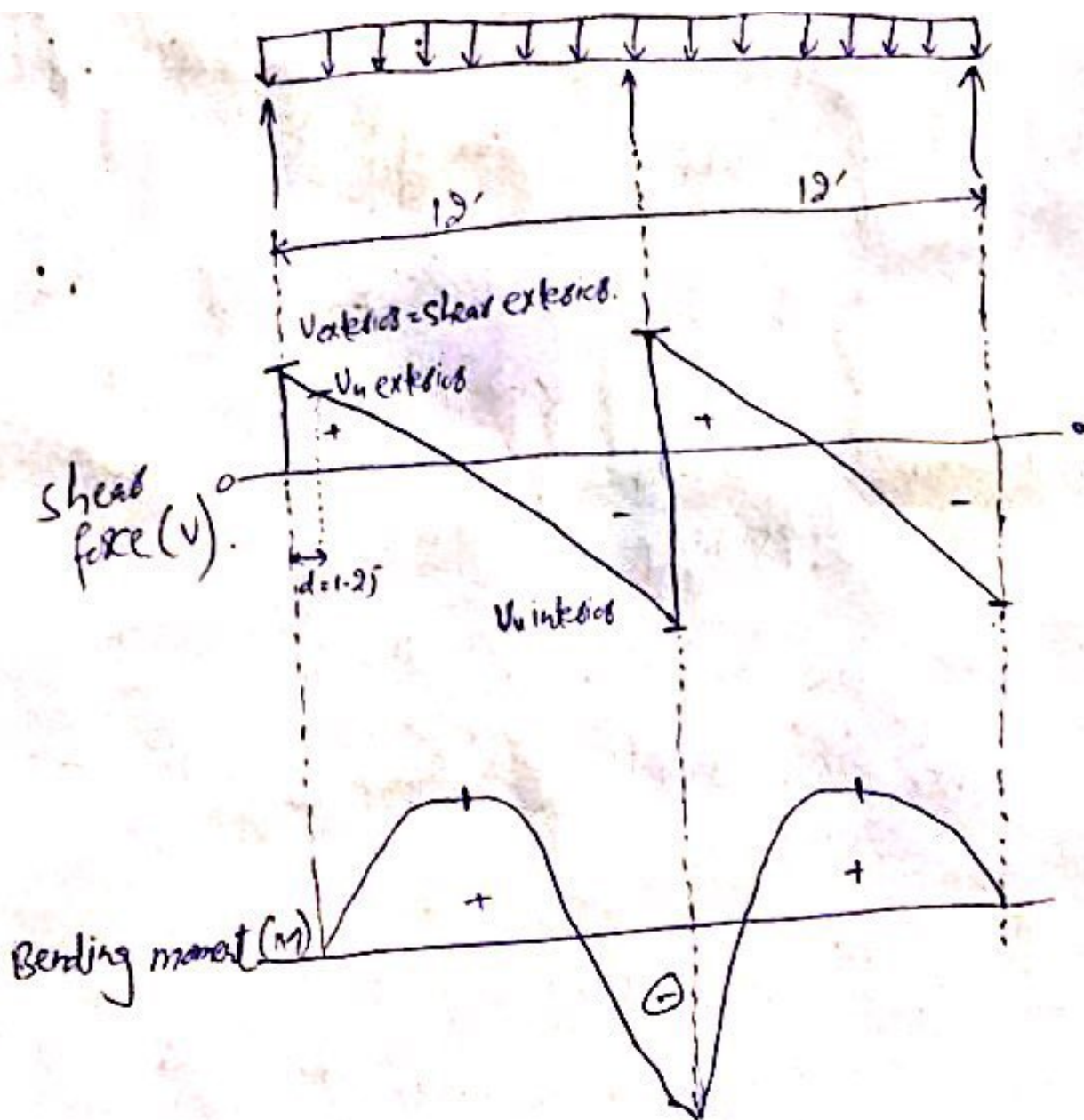


(10)



Notes

- a) Note that $\phi = 0.65$ as initially assumed since the graphs used show $f_s/f_y < 1.0$ & thus $\epsilon_t < 0.002$
- b) code requirements must be checked. ~~as~~ ~~is~~



Shears:- $V_{\text{exterior}} = \frac{w_u l_n}{2} = \frac{1.325 \times 18}{2} = 7.95 \text{ k.}$

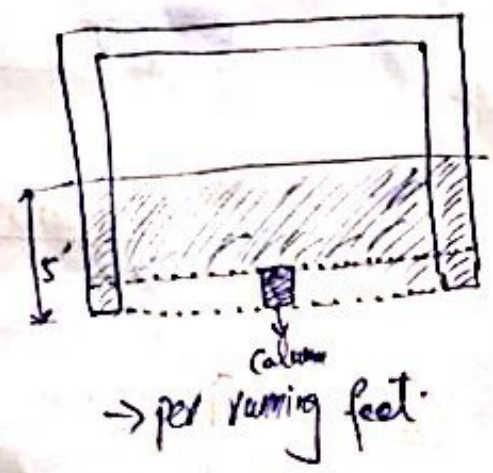
Interior
 $V_{\text{exterior}} = V_{\text{ext}} - d^2 = 7.95 - (1.25)^2 = 6.39 \text{ k}$

$V_{\text{interior}} = 1.15 \frac{w_u l_n}{2} = \frac{1.15 \times 1.325 \times 18}{2} = 9.14 \text{ k.}$

$V_{\text{interior}} = V_{\text{interior}} - d^2 = 9.14 - (1.25)^2 = 7.58 \text{ k.}$

(c.c)

self wt of beam = $h \times b \times \gamma_c$
 $= \left(\frac{18 \times 19}{144} \right) \times 0.15$
 $= 0.225 \text{ K/ft.}$



Total D.L = $0.6125 + 0.225$
 $= 0.8375 \text{ K/ft}$

Also service live load for 5' slab per running feet.
 service, live load = $0.04 \times 5 = 0.2 \text{ K/ft.}$

Factored load:

$W_u = 1.2 \text{ D.L} + 1.6 \text{ L.L}$

$W_u = (1.2 \times 0.8375) + (1.6 \times 0.2)$

$W_u = 1.325 \text{ K/ft}$

Step #03: Shear & Moments :-

using Table 12.1 moments and shear values
 using ACI coefficients Design of concrete structures.

$$d = \frac{V_u}{\phi 2 \sqrt{f_c} b w} = \frac{121620}{0.75 \times 2 \times \sqrt{3000} \times 9 \times 12}$$

$$d = 13.71'' < 19.5 \text{ OK}$$

use $h = 24''$ in total depth.

$$\text{Moments, } M_u = 3.83 \times 9 \times 6.12 \times \frac{3.83}{2}$$

$$M_u = 404 \text{ ft-k}$$

$$\frac{M_u}{\phi b d^2} = \frac{404 \times 1000 \times 12}{0.9 \times (9 \times 12) \times (19.5)^2} = 131.2 \text{ psi}$$

use Appendix A table A-12

$$\frac{M_u}{\phi b d^2} = 134.3 \text{ then use greater of}$$

$$\textcircled{1} \frac{2000}{60,000} = 0.0033$$

$$\textcircled{2} \frac{3 \sqrt{3000}}{60,000} = 0.00274$$

$$\text{So } f = 0.0033$$

$$\text{Area of steel: } A_s = f b d = 0.0033 \times (9 \times 12) \times 19.5$$

$$A_s = 6.95 \text{ in}^2$$