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Subject # Hydraulics Engineering.

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Given data:-

$$\text{Discharge} = 7804 \text{ lit/sec} = 7.804 \text{ m}^3/\text{sec}$$

$$\text{width of apron} = 8 \text{ m}$$

$$\text{mean velocity} = 7804 - 220 = 7584$$

$$\frac{7584}{3.28} = 2312.5 \text{ m/sec}$$

Solution:-

As we know that

As  $q$  is discharge per unit width

$$q = Q/b$$

$$q = \frac{7.804}{8} = 0.975$$

As critical depth  $y_c$  is

$$y_c = \left( \frac{q^2}{g} \right)^{1/3}$$

$$y_c = \left( \frac{(0.975)^2}{9.81} \right)^{1/3}$$

$$y_c = 0.46 \text{ m}$$

critical velocity

$$\text{As } v = vy$$

$$v = q/y$$

$$v_c = \frac{q}{y_c}$$

$$v_c = \frac{q}{y}$$

$$v_c = \frac{0.975}{0.46}$$

$$v_c = 2.119 \text{ m/sec}$$

$$v_c = 2.12 \text{ m/sec}$$

As  $v_1 > v_c$ . Super critical flow  
water depth on upstream side is Hydraulic  
Jump.

$$Q = AV$$

$$Q = byv$$

$$y = \frac{Q}{v \cdot b}$$

$$y_1 = \frac{7.804}{2.12 \times 8}$$

$$y_1 = 0.46 \text{ m}$$

By formula

$$y_2 = -\frac{y_1}{2} + \sqrt{\frac{y_1^2}{4} + \frac{2y_1 v_1^2}{g}}$$

$$= -\frac{0.46}{2} + \sqrt{\frac{(0.46)^2}{4} + \frac{2(0.46)(2.12)^2}{9.81}}$$

$$y_2 = 0.50 \text{ m}$$

Difference in depth.

$$\Delta y = y_2 - y_1$$

$$= 0.50 - 0.46$$

$$\Delta y = 0.04 \text{ m}$$

AS

$$\text{ALSO } \Delta E_p = E_1 - E_2$$

$$A_1 V_1 = A_2 V_2$$

$$b_1 y_1 V_1 = b_2 V_2 y_2 \quad ? \quad b = b_1 = b_2$$

$$V_2 = \frac{y_1 V_1}{y_2}$$

$$V_2 = \frac{0.46 \times 2312.5}{0.50}$$

$$V_2 = 2127.5 \text{ m/sec}$$

$$\Delta E_2 = E_1 - E_2$$

$$E_1 - E_2 = \left( y_1 + \frac{V_1^2}{2g} \right) - \left( y_2 + \frac{V_2^2}{2g} \right)$$

$$= \left( 0.46 + \frac{2312.5^2}{2(9.81)} \right) - \left( 0.50 + \frac{2127.5^2}{2(9.81)} \right)$$

$$E_1 - E_2 = 272561.50 - 230696.063$$

$$E_1 - E_2 = 41865.437 \text{ m}$$

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Power Dissipation in hydraulic jump

$$\Delta P = \rho g Q (E_1 - E_2)$$

$$= 1000 (9.81) (7804) (41865.43)$$

$$\Delta P = 3205101772213.2$$

$$\Delta P = 32051017722.132 \text{ KW}$$

Q1 part B.

Given data:-

channel width (b) = 4m

Discharge = 7804 ft<sup>3</sup>/sec

height of upstream side = 2.9m

height of downstream = 1.1m

Solution:-

As we know that  
 AS specific Energy is

$$E_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \quad \text{--- (1)}$$

Also from discharge

$$Q = AV$$

$$\Rightarrow A_1 V_1 = A_2 V_2$$

$$b_1 y_1 v_1 = b_2 y_2 v_2 \quad \because b = b_1 = b_2$$

$$y_1 v_1 = y_2 v_2$$

$$v_2 = \frac{y_1 v_1}{y_2}$$

$$v_2 = \frac{2.9}{1.1} \times v_1$$

$$\boxed{v_2 = 2.63 v_1} \quad \text{put in eq (1)}$$

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$$= 2.9 + \frac{v_1^2}{2g} = 1.1 + \frac{(2.63 v_1)^2}{2g}$$

$$= 2.9 + \frac{v_1^2}{2g} = 1.1 + \frac{6.91 v_1^2}{2g}$$

$$\Rightarrow \frac{v_1^2}{2g} - \frac{6.91 v_1^2}{2g} = 1.1 - 2.9$$

$$\Rightarrow + \frac{5.91 v_1^2}{2g} = +1.8$$

$$\Rightarrow 5.91 v_1^2 = 1.8 \times 2 (9.81)$$

$$v_1 = \sqrt{\frac{1.8 \times 2 (9.81)}{5.91}}$$

$$v_1 = 2.44 \text{ m/sec}$$

Put in  $v_2$  equation

$$v_2 = 2.63 (2.44)$$

$$v_2 = 6.41 \text{ m/sec}$$

Type of flow using froude number

(i) on upstream side.

$$Fr_1 = \frac{v_1}{\sqrt{g y_1}} = \frac{2.44}{\sqrt{9.81 \times 2.9}}$$

$$Fr_1 = 0.45 \quad Fr < 1 \quad (\text{subcritical flow})$$

(2) on Down stream side:-

$$Fr_2 = \frac{v_2}{\sqrt{gy_2}} = \frac{6.41}{\sqrt{9.81 \times 1.1}} = 1.95$$

$Fr > 1$  Super critical flow

Question # 2

Part A

Given data:-

Depth of channel = 1.8 m

Discharge = 7804 ft<sup>3</sup>/sec

= 221.20 m<sup>3</sup>/sec

width of channel = 66 ft =

20.1 m

Required:-

$p_2$  weir height = ?

Solution:-

As we know that

$$Q = AV$$

$$v = \frac{Q}{A} = v_1 = \frac{Q_1}{A}$$

$$v_1 = \frac{Q}{b \times y}$$

$$v_1 = \frac{221.20}{20.1 \times 1.8} = 6.11 \text{ m/sec}$$



critical depth...

$$y_c = \left( \frac{q^2}{g} \right)^{1/3}$$

AS  $q = Q/b$

$$q = \frac{221.20}{20.1}$$

$$q = 11.00 \text{ m}^2/\text{sec}$$

$$y_c = \left( \frac{11^2}{9.81} \right)^{1/3}$$

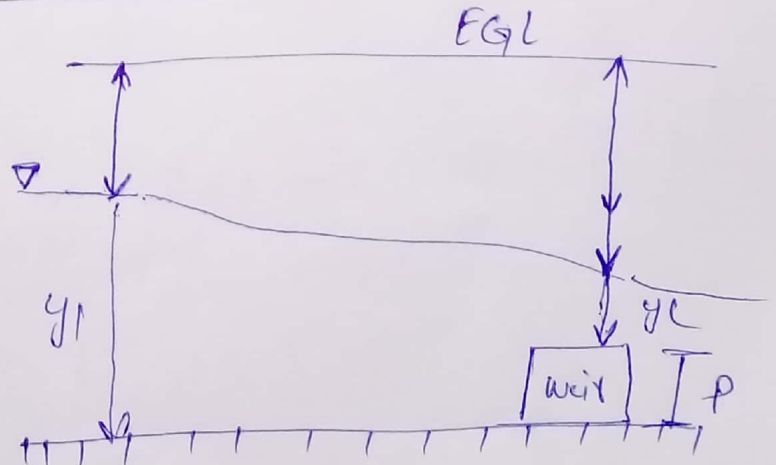
$y_c = 2.29 \text{ m}$

→ ALSO  $v = \sqrt{gy}$   
 $v_c = \sqrt{gy_c}$

$$v_c = \sqrt{9.81 \times 2.29}$$

$$v_c = 4.73 \text{ m/sec}$$

from the figure



$$\frac{v_1^2}{2g} + y_1 = \frac{v_c^2}{2g} + y_c + P$$

$$\frac{(6.11)^2}{2 \times 9.81} + 1.08 = \frac{4.73^2}{2 \times 9.81} + 2.29 + P$$

$$3.702 = 3.430 + P$$

$$P = 1.07 \text{ m}$$

The weir should have height of 1.07 measured from the channel bed.

Question NO # 2

Part # B

Given data:-

$$\text{Breadth} = 2.8 \text{ m}$$

$$\text{Depth} = 1.5 \text{ m}$$

water level on one side and above its top edge

$$H_1 = 5 \text{ m}$$

$$\text{water level on other side} = H_2 = 5 \text{ m} + 1.5 = 6.5$$

Similarly

$$H_2 = 5 + 0.6$$

$$= 5.6$$

$$C_d = 0.780$$

Required:-

$$\text{Discharge } Q = ?$$

Solution:-

As we know that

As by formula.

Discharge through submerged portion.

$$Q_1 = cd \times b \times (H_2 - H_1) \times \sqrt{2gh}$$

$$= 0.78 \times 2.8 (6.5 - 5.6) \times \sqrt{2(9.81)(5.6)}$$

$$Q_1 = 20.6$$

Discharge through free portion:

$$Q_2 = \frac{2}{3} cd \times b \sqrt{2g} \times [H_2^{3/2} - H_1^{3/2}]$$

$$Q_2 = \frac{2}{3} (0.78) \times 2.8 \sqrt{2 \times 9.81} \times [(5.6)^{3/2} - (5)^{3/2}]$$

$$Q_2 = 13.36 \text{ m}^3/\text{sec}$$

Total discharge  $Q = Q_1 + Q_2$ 

$$Q = 20.6 + 13.36$$

$$Q = 33.96$$

Q<sub>03</sub>  
Part A

Given data.

$$d_1 = R - 200$$

$$= 7804 - 200 = 7604 \text{ mm}$$

$$d_2 = R + 3000 \text{ mm}$$

$$= 7804 + 3000 = 10804 \text{ mm}$$

flow rate  $Q = 0.95 \text{ m}^3/\text{sec.}$

pressure in larger pipe =  $R + 800 \text{ N/m}^2$

$$7804 + 800$$

$$8604 \text{ N/m}^2$$

Sol:-

① Head loss due to sudden enlargement

$$d_1 = 7604 \text{ mm} = 7.60 \text{ m}$$

$$A_1 = \frac{\pi (d_1)^2}{4} = \frac{\pi (7.60)^2}{4}$$

$$A_1 = 45.3 \text{ m}^2$$

$$d_2 = 10804 \text{ mm}$$

$$A_2 = \frac{\pi (10804)^2}{4 \cdot 100}$$

$$A_2 = 91.6 \text{ m}^2$$

By Discharge formula

$$Q = AV$$

$$V = Q/A$$

$$V_1 = Q/A_1$$

$$V_1 = \frac{0.95}{45.5} = 0.020 \text{ m/sec}$$

Similarly

$$\Rightarrow V_2 = Q/A_2$$

$$V_2 = \frac{0.95}{91.6} = 0.010 \text{ m/sec}$$

By formula of Sudden Enlargement

$$h_c = \left(1 - \frac{A_1}{A_2}\right)^2 \times \left(\frac{V_1 - V_2}{2g}\right)^2$$

$$= \left(1 - \frac{45.5}{91.6}\right)^2 \times \left(\frac{0.020 - 0.010}{2(9.81)}\right)^2$$

$$= (0.225) (5.096 \times 10^{-6})$$

$$h_c = 1.302 \times 10^{-6} \text{ m}$$

(2) Power loss Due to Sudden Enlargement

By formula -

$$P = \rho g Q h_e$$

$$= (1000)(9.81)(0.95)(1.302 \times 10^{-6})$$

$$P = 0.012 \text{ W}$$

(3) Pressure in smaller pipe  
By using Bernoulli's equation

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + h_e$$

$$\frac{P_1}{(1000)(9.81)} + \left( \frac{0.020}{2(9.81)} \right)^2 = \frac{P_2}{(1000)(9.81)} + \frac{(0.010)^2}{2(9.81)} + 1.302 \times 10^{-6}$$

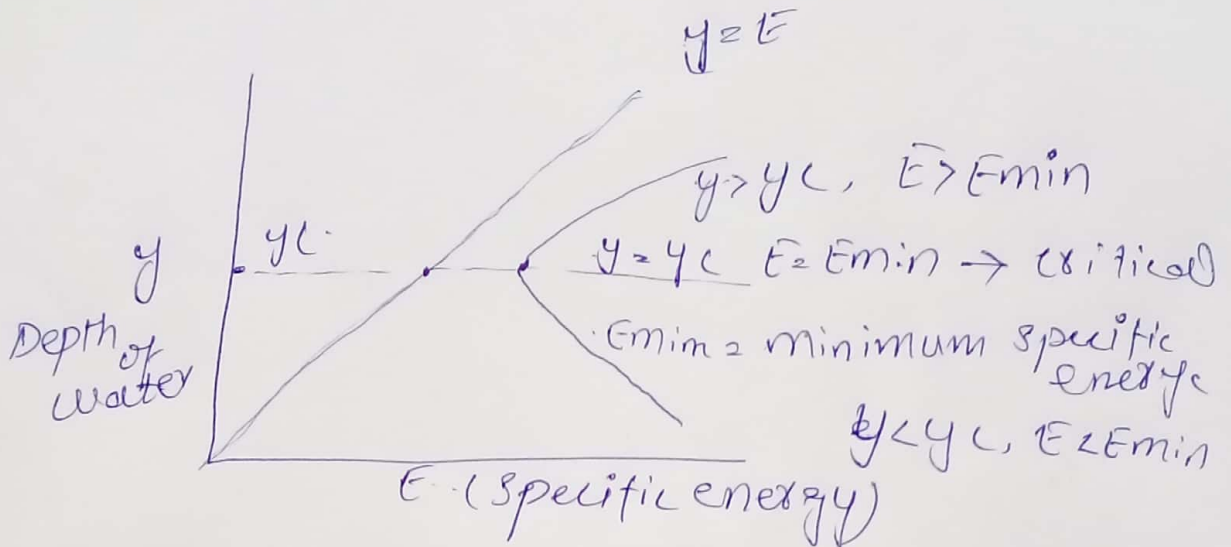
$$\frac{P_1}{9810} + 0.0000203 = \frac{8605}{9810} + 0.0000509 + 0.0000132$$

$$\frac{P_1}{9810} = 0.877 + 0.0000509 + 0.00001302 - 0.0000203$$

$$\frac{P_1}{9810} = 0.876$$

$$P_1 = 0.876 \times 9810$$

$$P_1 = 8593.56 \text{ N/m}^2$$



critical depth is the depth corresponding to minimum specific energy.

- ↳  $y > y_c \Rightarrow E > E_{min}$  (sub critical flow)
- ↳  $y = y_c \Rightarrow E = E_{min}$  (critical flow)
- ↳  $y < y_c \Rightarrow E < E_{min}$  (super critical flow)