

NAME:

NAVEED AHMAD

I.D.:

7880

SECTION:

4B

SUBJECT:

PRCY I

S

UBMITTED To:

SIR TANAD

ASSIG:

01.

DATE:

26/6/2020.

# QUESTION- 1.

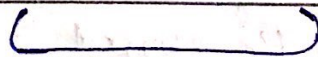
## STIRRUP :

Stirrup are closed loop bars tied at regular interval in beam reinforcement to hold the bar in position

### TYPES:

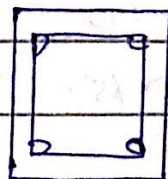
#### 1) SINGLE LEGGED:

Single leg stirrup have rarely been used because they are mostly used when binding two rods



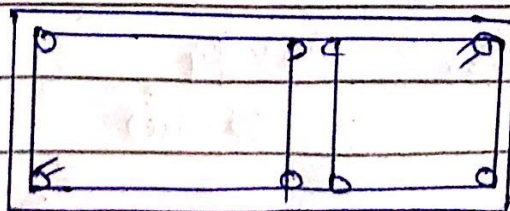
#### 2) TWO LEGGED:

It's most commonly and widely used minimum 4 bars are required.

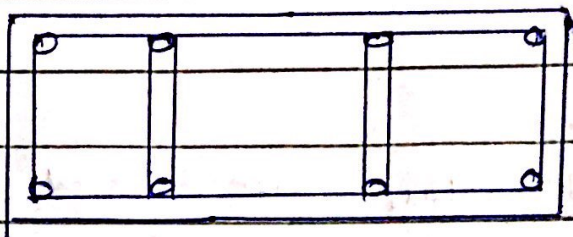


#### 3) FOURED LEGGED:

used in case of web reinforcement



### 47 SIX LEGGED:



### ACI CODE PROVISION FOR SHEAR DESIGN.

Critical section at a design distance  $d$  from the face of support.

#### 1) SHEAR STRENGTH CAPACITY OF CONCR.

$$V_c = 2 \times \sqrt{f'_c} \times b \times w \times d$$

#### 2) MINIMUM WEB REINFORCEMENT:-

If  $V_u \leq \phi V_c$  No web reinforcement req.

$$A_{u \min} = \frac{0.75 \times \sqrt{f'_c} \times b \times w \times s}{f_y} \quad \text{OR} \quad A_{u \min} = \frac{50 \times b \times w \times s}{f_y}$$

Also from formulas

$$\text{max Capacity } S_{\max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b \times w} \quad \text{OR}$$

$$S_{\max} = \frac{A_u \times f_y}{50 \times b \times w}$$

First stirrup is provided at a distance  $s$  from face of

Shear at critical section is represented by " $V_c$ "

Between critical section " $V_u$ " and " $V_c$ " spacing btw web reinforcement can be found by following formula

$$s = \frac{V_u - V_c}{V_s} \times A_v \times f_y \times d$$

$V_s$  = Shear force carried by web reinforcement / stirrups.

According to ACI codes.

If  $V_s \leq 4 \times \sqrt{f_c'} \times b_w \times d$ , the max spacing of stirrups will be smallest of the following four conditions.

① 24"

②  $d/2$ .

③  $S_{max} = \frac{A_v \times f_y}{0.75 \times \sqrt{f_c'} \times b_w}$

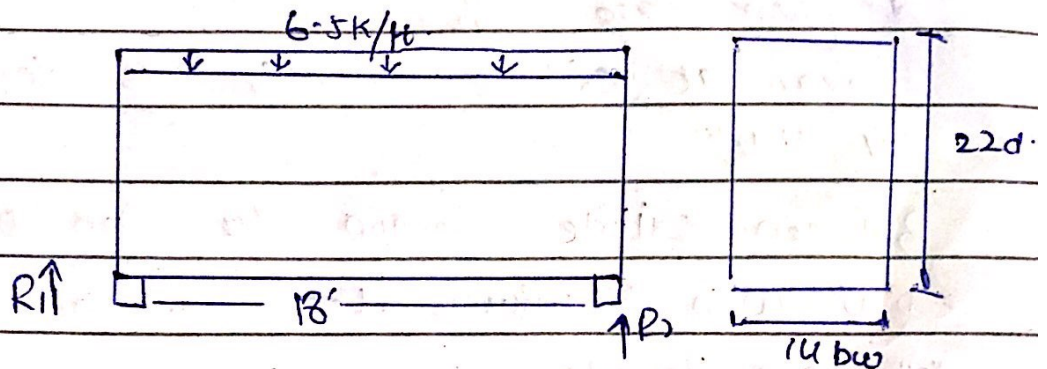
④  $S_{max} = \frac{A_v \times f_y}{50 \times b_w}$ .

If  $V_s > 4 \times \sqrt{f_c'} \times b_w \times d$  max spacing will be halved.

If  $V_s > 2 \times \sqrt{f_c'} \times b_w \times d$  Then either increase Gross sectional dimension or decrease.

(4)

## QUESTION - 2.



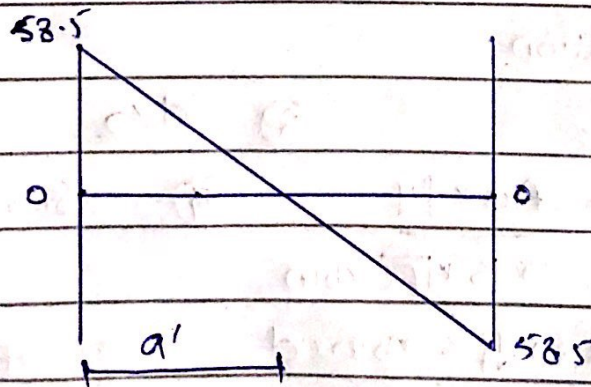
STEP 01:

Find values of  $R_1$  and  $R_2$

$$\text{total load } 6.5 \text{ k/ft} = 6.5 \times 18 / 2 \Rightarrow 58.5$$

STEP 02:

Draw shear force diagram



STEP 03:

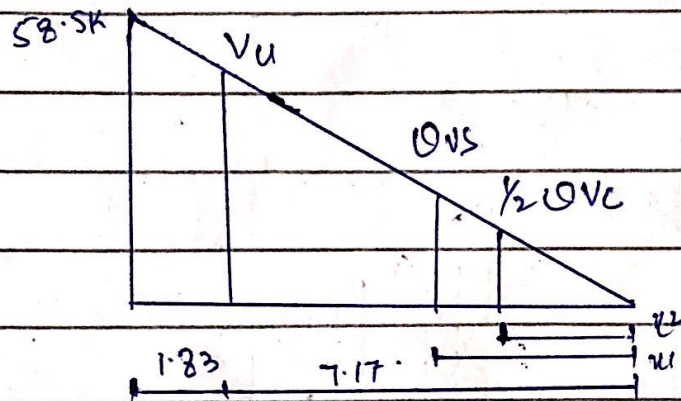
Find the value of  $Criticle$

Shear  $V_u$  and find its location

As we know that section is located at distance " $d$ " from face of support =  $d = 22"$   
 $= 1.83'$

(5)

Value of critical shear at distance 'd'  
by similarity of triangle



$$\frac{58.5}{9} = \frac{V_u}{7.17}$$

$$V_u = 46.605$$

STEP 04:

Find the value of  $OVC$  &  $QVC$   
and also its distance from zero shear to  
right side

$$OVC = \phi \times 2 \times \sqrt{F_c} \times b \times w \times d$$

$$\Rightarrow \frac{0.75 \times 2 \times \sqrt{4000} \times 14 \times 22}{1000}$$

$$OVC = 29.219 \text{ k}$$

Location of  $OVC$  by similarity of triangle -

$$\frac{58.5}{9} = \frac{29.219}{x_1}$$

$$\rightarrow x_1 = 4.495'$$

⑧

Now  $1/2 \text{ Ovc} = 14.6095 \text{ k}$ .

Location of  $1/2 \text{ Ovc}$  by similarity of triangle  $58.5 = 14.6095 \Rightarrow x_2 = 2.247$

STEP 05:

Value of  $\text{Ovs}$ .

$V_u = \text{Ovs} \text{ Ovc}$

$\text{Ovs} = V_u - \text{Ovc}$

$= 46.605 - 29.219 \Rightarrow 17.386$ .

STEP 06:

Check on section adequacy.

$0.75 \times 8 \times \sqrt{f_c} \times b \times d$

$= \frac{0.75 \times 8 \times \sqrt{4000} \times 14 \times 22}{1000} = 116.87$ .

$\text{Ovs} < 0.8 \sqrt{f_c} b \times d$

It means section is adequate.

STEP 07:

check on maximum spacing

To stirrups.

$0.75 \times 4 \times \sqrt{f_c} \times b \times d$

$= \frac{0.75 \times 4 \times \sqrt{4000} \times 14 \times 22}{1000}$

$\Rightarrow 58.438 \text{ k}$ .

(7)

As  $0.4 \sqrt{f_c}$  bwd  $>$   $0.5$

So maximum spacing will be selected from the following four conditions using #3, 2 legged stirrup

1)  $S_{max} = 24$

2)  $a/2 = 22/2 = 11$

3)  $S_{max} = \frac{A_v \times f_y}{0.75 \times \sqrt{f_c} \times b_w} = \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 4} = 19.8$

4)  $S_{max} = \frac{0.22 \times 60000}{50 \times 14}$

$\rightarrow S_{max} = \frac{A_v \times f_y}{S_o \times b_w} = \frac{0.22 \times 60000}{50 \times 14} = 18.857$

From above four conditions least value of spacing for #3, 2 legged stirrup will be selected.

STEP 08:

Spacing of stirrup from central section :

$$S = \frac{V_u \times A_v \times f_y \times d}{V_u - 0.5 V_c}$$

$$\Rightarrow \frac{0.75 \times 0.22 \times 60000 \times 22}{46.605 - 29.219}$$

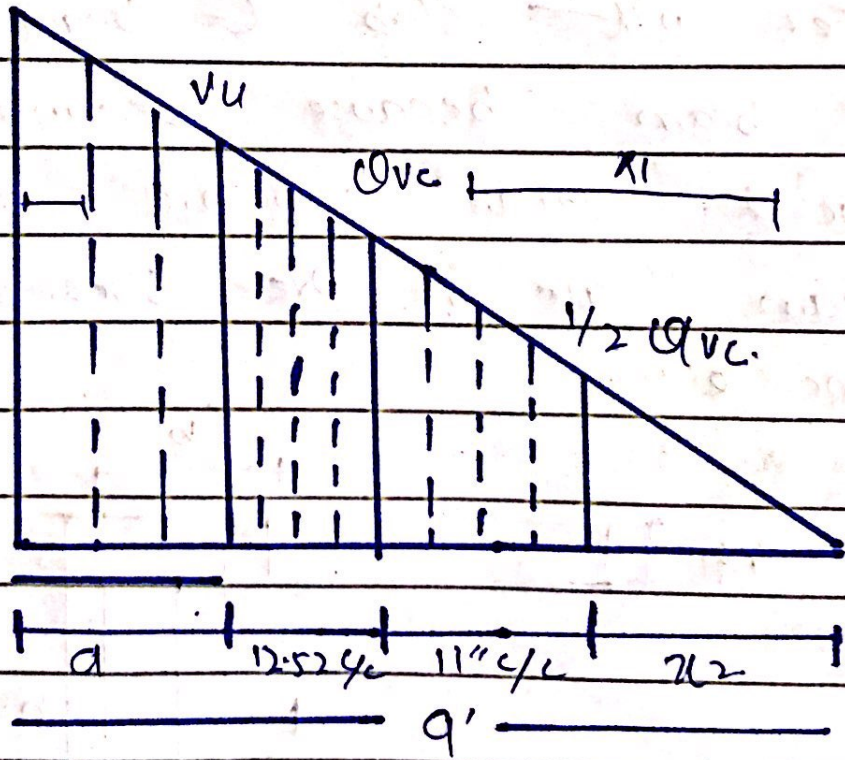
$$S = 17.52 \text{ c/c}$$



STEP 09.

Final sketch.

$$S = \frac{12.52}{\lambda} = 6.2$$

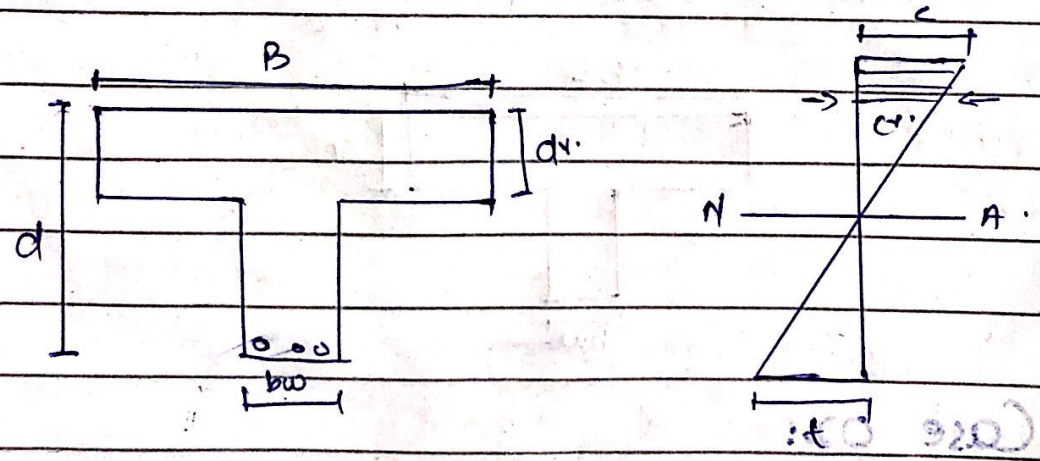


### QUESTION - 3

#### T-BEAM:

Beam consists of flange and rib in the form of T, generally made of RC concrete or metal

Top part of slab which acts along the beam to resist the compressive stress is called flange. The part which lies below the slab and resists the shear stress is called rib.

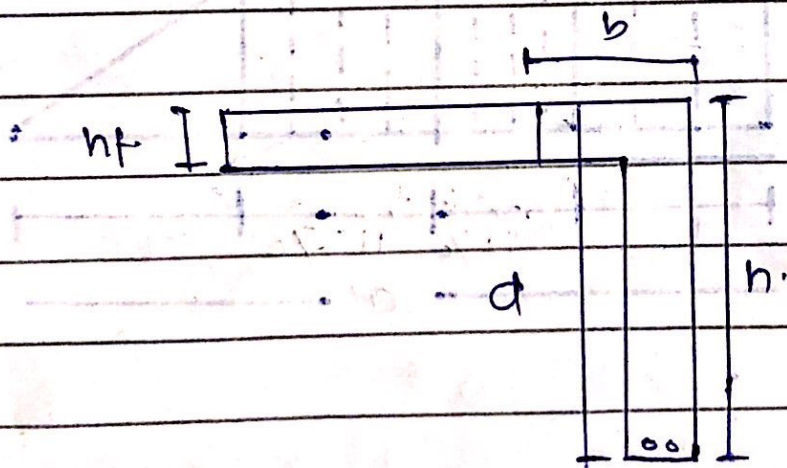


T-beam and stress distribution diagram

#### L-BEAM:

The end beam which have slab on one side only acts as L-beam in most of the reinforced concrete structure. Concrete slabs are beams cast monolithic in a floor consisting of several beams

Cast monolithically with a slab, the intermediate beam acts as T-beam. Where as beam at top of the corners of the walls or beams around stair case or lift opening are called L-beam. Thus L-beam and T-beam form a part of floor system together with slab - L-beam are typical floor beam because because of the reduced overall structure depth the beam are in pre-stressed or reinforced concrete.

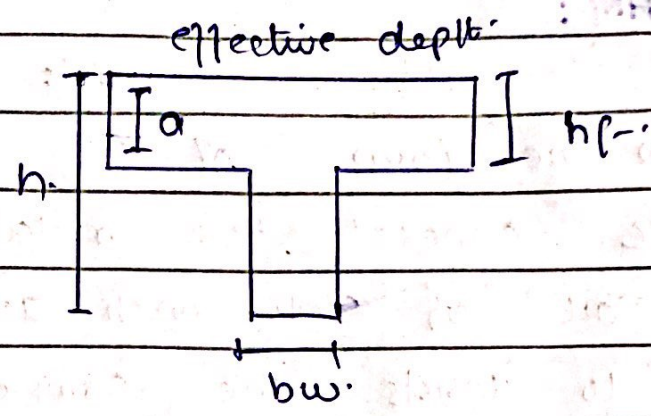


### Flexural Strength analysis for T-Beam.

There are two cases in two beam analysis for T beam

Case 01:

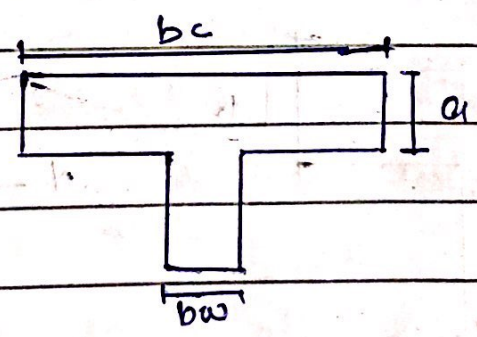
$$a \leq hf$$



$$b = bc$$

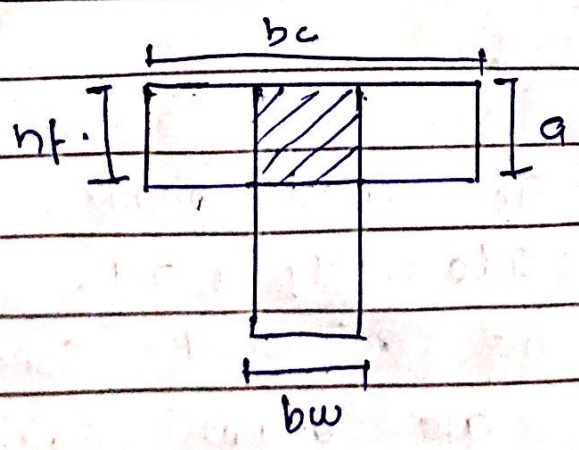
$$M_n = A_s w \times f_y \times (d - a/2)$$

$$M_n = 0.85 \times f_c \times bw \times a \times (d - a/2)$$

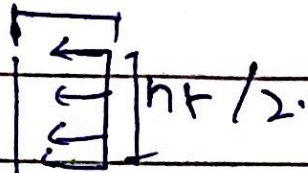


Case 02:

$$a > hf$$



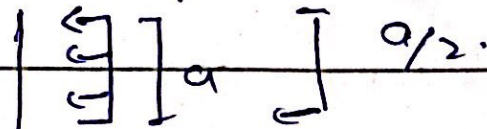
$$0.85 \times f'c$$



$$C_1 = 0.85 \times f'c \times (b_e - b_w) \times h_f \times (d - h_f/2)$$

$$T_1 = A_{st} \times f_y$$

$$0.85 \times f'c$$



$$C_w = 0.85 \times f'c \times b_w \times a \times (d - a/2)$$

$$T_2 = A_{sw} \times f_y = (A_s - A_{st}) \times f_y$$

Total Tensile stress Area =  $A_s = A_{st} + A_{sw}$

$$M_n = M_{n1} + M_{n2}$$

$$M_{n1} = A_{st} \times f_y \times (d_y - h_f/2)$$

$$\Rightarrow 0.85 \times f'c \times (b_e - b_w) \times h_f \times (d - h_f/2)$$

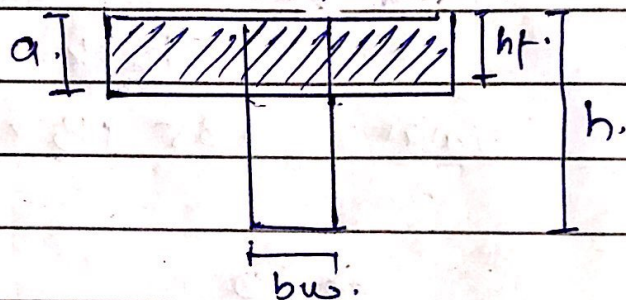
$$M_{n2} = A_{sw} \times f_y \times (d - a/2) = \text{---}$$

$$\Rightarrow 0.85 \times f'c \times b_w \times a \times (d - a/2)$$

QUESTION - 4

CASE I:

In case I ( $a \leq hf$ ) which shows that the height of compression block is less than or upto flange level. It's indication is that the beam is rectangular and it will be analysed by rectangular beam analysis method.



CASE II:

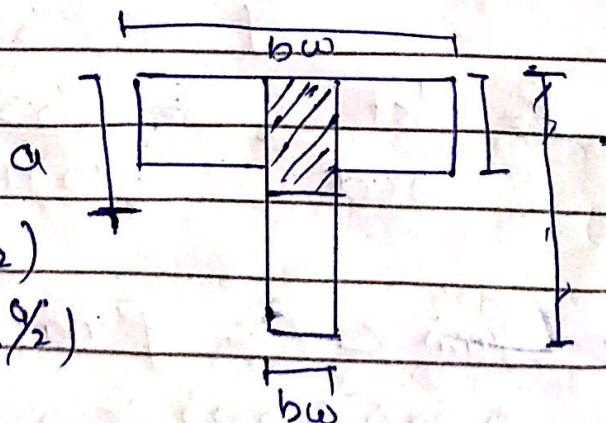
In case II ( $a > hf$ ) which shows that the height of compression block is more than the flange level and it indicates that the beam will be analysed by T-beam analysis method.

Moment:

$$M_n = M_{n1} + M_{n2}$$

$$M_{n1} = A_s f_y \times (d - hf/2)$$

$$M_{n2} = A_{sw} \times f_y \times (d - \frac{d}{2})$$



## QUESTION - 5

DATA:

$$f_c = 3 \text{ ksi} ,$$

$$f_y = 60 \text{ ksi}$$

$$\text{factored moment} = 5800 \text{ k-inch } 5.8 \text{ k/ft}$$

STEP 01.

calculate effective width "be"

$$1) 1b \times hf + bw \Rightarrow 16 + 3.5 + 10 = 66''$$

$$2) c/c \text{ distance} \Rightarrow 9 \times 12 = 108''$$

$$3) \text{span}/4 \Rightarrow 16/4 \times 12 = 48''$$

$$be = 48''$$

STEP 02:

Check whether rectangular  
or T-beam analysis is req.

Trial 01:

$$\text{let } a = hf = 3.5''$$

$$A_s = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{5800}{0.90 \times 60 \times (18 - 3.5/2)}$$

$$\Rightarrow 6.609$$

Trial 02:

~~As~~

$$a = \frac{A_s \times f_y}{0.25 \times f_c \times b_e} = \frac{6.609 \times 60.7}{0.85 \times 3 \times 42} \Rightarrow 3.23$$

$$A_{st} = 5200$$

$$0.90 \times 60 \left( 18 - \frac{3.23}{2} \right) \Rightarrow 6.55$$

Trial 03:

check  $f_{max}$  and  $f_{min}$

$$f_{max} = 0.85 \times B \times \frac{f_c}{f_y} \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_t} \right) \quad \text{Asw}$$

$\Rightarrow$  0

$$\Rightarrow 0.85 \times 0.85 \times 3 \left( \frac{0.003}{0.003 + 0.005} \right) \quad (2)$$

$$\Rightarrow 0.0135$$

$$f_{min} = \frac{200}{f_y} = \frac{200}{6000} = 0.003$$

$$P = \frac{A_{st}}{b \times d} = \frac{6.55}{10 \times 18} = 0.03$$

$$f_{min} < P < f_{max}$$

$$0.003 < 0.03 > 0.0135$$



(16)

$$\text{So } f_{\max} \frac{A_{st}}{b \times d}$$

$$\begin{aligned} A_{st} &= f_{\max} \times (b \times d) \\ &= 0.013 \times (10 \times 18) \\ A_{st} &= 2.34 \text{ in}^2 \end{aligned}$$

STEP 04:

Design it as doubly reinforce beam.

$$M_{u2} = \phi \times A_{st} \times f_y \times (d - a/2)$$

$$\text{For } a, a = \frac{A_{st} \times f_y}{0.85 \times f_c \times b} \Rightarrow \frac{2.34 \times 60}{0.85 \times 3 \times 10} \Rightarrow 5.72$$

$$M_{u2} = 0.90 \times 2.34 \times 60 \times (18 - 5.72/2)$$

$$M_{u2} = 1913.09 \text{ K}'' < M_u = 5800 \text{ K}''$$

STEP 05:

Find value of  $M_{u1}$ 

$$M_{u1} = M_u - M_{u2}$$

$$= 5800 - 1913.09$$

$$= 3886.9096 \text{ K}''$$

$$M_{u1} = \phi \times A_s' \times f_y \times (d - d')$$

$$A_s' = \frac{3886.9096}{0.90 \times 60 \times (12.25)} \Rightarrow 4.643 \text{ in}^2$$

STEP 06:

Total steel area.

$$A_s = A_{st} + A'_s$$

$$2.34 + 4.643 \Rightarrow 6.98 \text{ in}^2$$

STEP 07:

Selection of bars.

A) For tension of bars.

For tension zone.

$$\text{using } \# 10 \quad \text{Area} = 1.227 \text{ in}^2$$

$$\text{no of bars} = \frac{6.98}{1.227}$$

$$\Rightarrow 5.688 \approx 6 \# 10 \text{ bars}$$

B) For compression zone.

$$\text{using } \# 6 \quad \text{Area} = 0.44 \text{ in}^2$$

$$\text{No of bars} = \frac{4.643}{0.44}$$

$$\Rightarrow 10.55 \approx 11 \text{ bars}$$

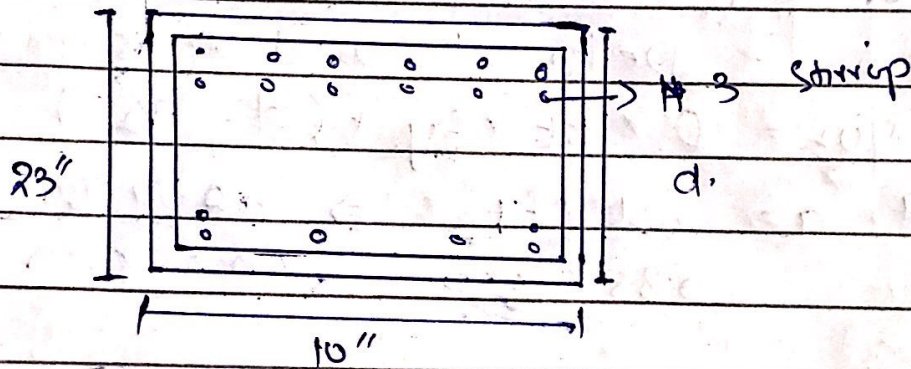
STEP 08:

Check minimum width

$$b_{min} = 2 \times 1.5 \times 2 + 3/8 + 6 \times 10/8 + 5 \times 10/8$$

$$17.5 > 10$$

Not good in one layer, must be provided in two layers.



STEP # 09:

Design moment.

$$a = \frac{(A_s - A'_s) f_y}{0.85 \times f'_c \times b} \Rightarrow \frac{(6 \times 1.227 - 11 \times 0.44) 60}{0.25 \times 3 \times 10} \Rightarrow 5.934$$

$$M_d = 0.90 \left[ (11 \times 0.44) \times 60 (19.625 - 3) + 6.98 - 4.643 \right] \times 60 \times (16.658)$$

$$m_d = 6447.316 \text{ k} > M_u = 5800 \text{ k}$$

design is fine.

## QUESTION - 6

DATA:

$$b = 14'' \quad M_u = 600 \text{ k-in}$$

$$h = 26'' \quad f'_c = 4 \text{ ksi}$$

$$f_y = 60 \text{ ksi} \quad d = 22''$$

Assume  $d' = 2.5''$ 

STEP 01:

Check the capacity of  
selection as single reinforced beam.

$$f_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \left( \frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \left( \frac{0.003}{0.003 + 0.005} \right)$$

$$\Rightarrow 0.018$$

STEP 02:

$$f_{max} = \frac{A_{st}}{b \times d}$$

$$\text{So } A_{st} = f_{max} \times b \times d$$

$$= 0.018 \times 14 \times 22 \Rightarrow 5.544 \text{ in}^2$$

STEP 03:

$$M_{U2} = Q \times A_{st} \times f_y (d - a/2)$$

Bot first  $a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b}$

$$\Rightarrow \frac{5.544 \times 60}{0.85 \times 4 \times 24}$$

$$a = 6.988''$$

$$M_{U2} = 0.9 \times 5.544 \times 60 \times (22 - 6.988/2)$$

$$M_{U2} = 5540.26 \text{ K}'' < 6000 \text{ K} = M_U$$

Design a section as doubly reinforced

STEP 04:

$$M_{U1} = M_U - M_{U2}$$

$$6000 - 554.25$$

$$M_U = 459.74 \text{ K}''$$

STEP 05:

$$M_{U1} = Q \times A_s' \times f_y \times (d - d')$$

$$\text{So } A_s' = \frac{M_{U1}}{Q \times f_y (d - d')}$$

$$A's = 459.74$$

$$0.90 \times 60 \times (22.25)$$

$$A's = 0.43 \text{ in}^2$$

STEP 06:

Total area of steel:

$$A_z = A_{zt} + A's$$

$$= 5.544 + 0.43$$

$$\Rightarrow 5.98 \text{ in}^2$$

This steel area should be provided in tensile zone as tension reinforced.

STEP 07:

Selection of Bars

$A_z$  For tension steel.

$$\text{Let } \# 8 \text{ bars Area} = 0.785 \text{ in}^2$$

$$\text{No of bars} = \frac{A_z}{A_b} = \frac{5.98}{0.785} \Rightarrow 7.62$$

7.62  $\approx$  8 bars.

B :

For Compression Steel

Let  $n_y$  # 6 bars , area = 0.44 .

$$\text{No. of bars} = \frac{A_s}{A_b} = \frac{0.43}{0.44}$$

0.97  $\approx$  1 # 6 bars.

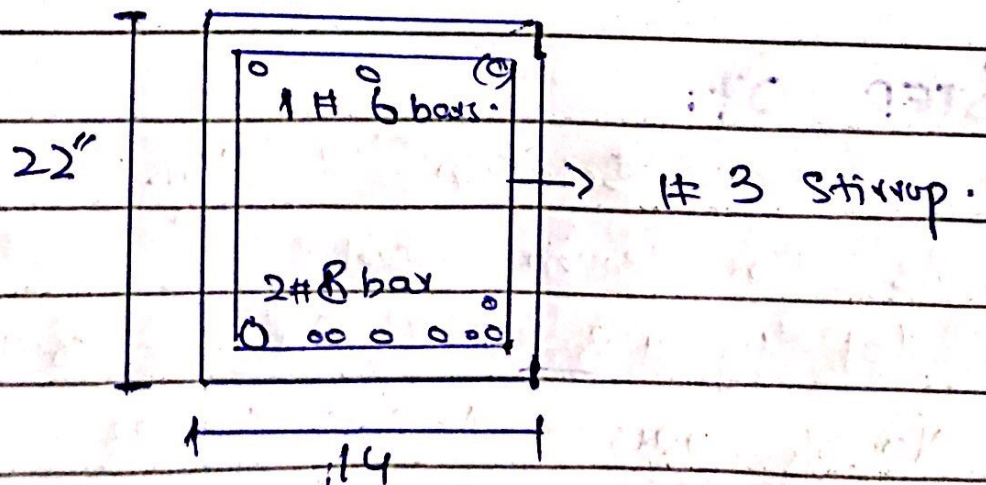
STEP 08:

Check minimum width

$$b_{min} = 2 \times 1.5 + 2 \times 3/2 + 8 \times 8/8 + 7 \times 8/8$$

$$\rightarrow 18.75" > 14"$$

Not good in one layer.



(23)

STEP 09:

Design moment

$$M_d = \phi [A_s' \times f_y \times d - d'] + (A_s - A_s') f_y (d - a/2)$$

$$a = \frac{(A_s - A_s') f_y}{0.85 \times f_c \times b} \Rightarrow \frac{(8 \times 0.785 - 1 \times 0.44) \times 60}{0.85 \times 4 \times 14}$$

$$a = 7.361''$$

$$M_d = 0.90 (1 \times 0.44) 60 \times (22 - 2.5) + (8 \times 0.785 - 1 \times 0.44) 60 \times (22 - \frac{7.361}{2})$$

$$\rightarrow 6.882 - 47 > M_u = 6000$$

Design is fine.