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Power

Subject # System Analysis

Department # Electrical
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Module # 6th

(Pg 1)

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Q No 5
Ans

This method we find out the the power flow equation for these method start again with the losses of network equation.

$$I_{Bus} = Y_{Bus} V_{Bus}$$

and for any particular bus is

$$I_k = \sum_{n=1}^N Y_{kn} V_n$$

The complex power $P_k + jQ_k = V_k I_k$

$$P_k + jQ_k = V_k \left\{ \sum_{n=1}^N Y_{kn} V_n \right\}$$

where $k = 1, 2, \dots, N$

From complex power

$$I_k = \frac{P_k - jQ_k}{V_k}$$

$$I_k = \sum_{n=1}^N Y_{kn} V_n$$

$$I_k = Y_{k1} V_1 + Y_{k2} V_2 + Y_{kN} V_N + \dots$$

(Pg 2)

Kanran # 10# 6990

From the above equation.

$$V_k = \frac{1}{Y_{kk}} \left[I_k - \left(\sum_{n=1}^{k-1} Y_{kn} \right) v_n \right]$$

$$\sum_{n=k+1}^N Y_{kn} v_n$$

or

$$V_k = \frac{1}{Y_{kk}} \left[\frac{P_k - jQ_k}{V_k} - \left(\sum_{n=1}^{k-1} Y_{kn} v_n \right) \right]$$

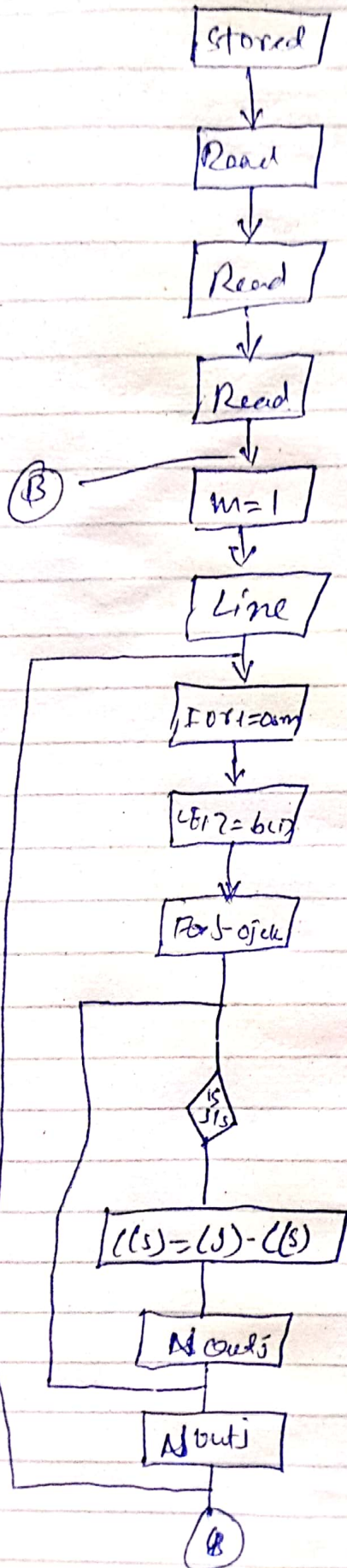
$$\sum_{n=k+1}^N Y_{kn} v_n$$

where $k = 1, 2, \dots, N$

(Pg 3)

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Flowchart Cross Serial



(Pg 4)

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(Ques
Ans)

there is one problem in doing power flow solution that we can not know all the load are known to us but generation are in our control and one can say that all generation known to us. but there is one problem. the problem is still all the generation are available we don't know what is the losses in the system we can not know how much generation because the sum of load and the no of losses must be equal to the total generation.

Solution!

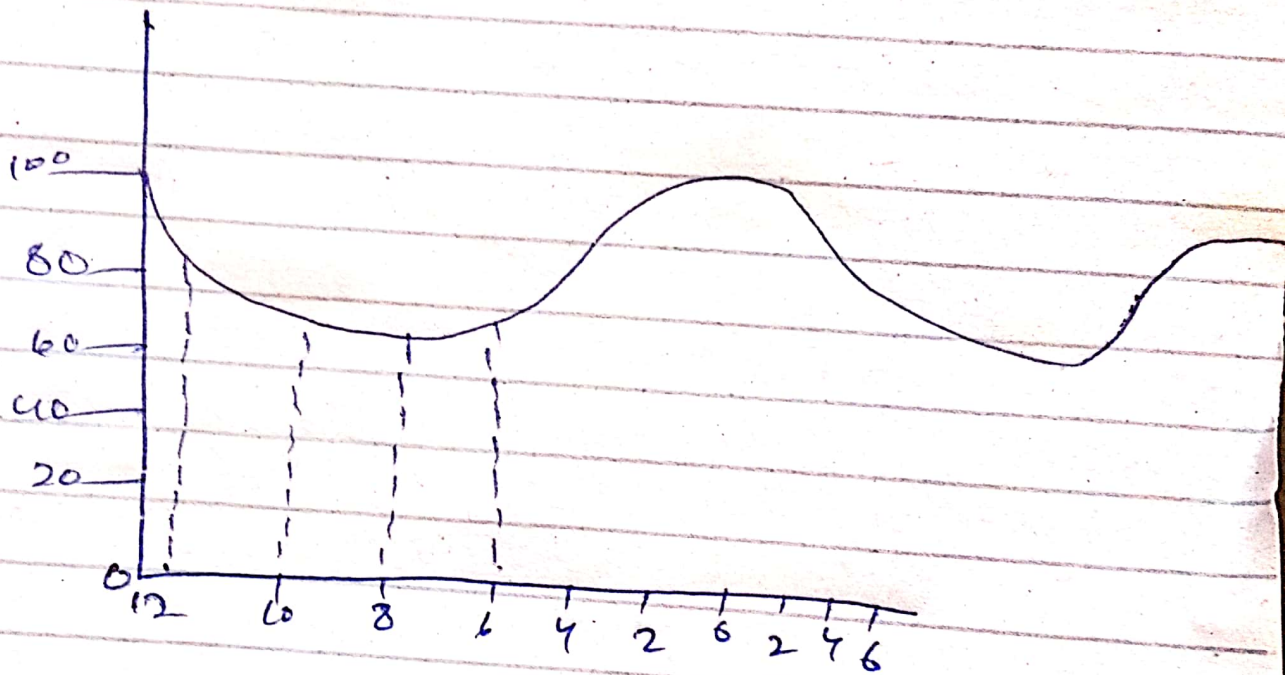
The Over come the we choose one bus on a reference bus which takes up all these losses which can find after solution so at once bus we can not specify the generally this is a bus which have very large generation available so that there will be no problem for it to take a losses this bus is power

(Pg 5)

Kamran # ID# 6990

Power System terminology is called a Stack bus.

Load Curves!



(Pg 6)

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Q No 3

Ans: A generator is connected of 10kW which injected P_{GK} , Q_{GK} to the bus bar.

⇒ A load is 20kW is connected which take P_{LK} , Q_{LK} from Bus bar.

⇒ This bus bar is connected to other bus bars i.e. to bus i, j and on through line.

⇒ The voltage at bus bar is V_K , where is equal to the magnitude V_K and angle δ_K

⇒ one think we see that generator of 10kW injects P_{GK} and Q_{GK} while load ~~take~~ is 20kW takes P_{LK} and Q_{LK} from the bus bar then we can take the algebraic sum of generator of 10kW and load 20kW i.e. subtracts the the load 20kW from the generator 10kW

i.e.

$$P_K = P_{GK} - P_{LK}$$

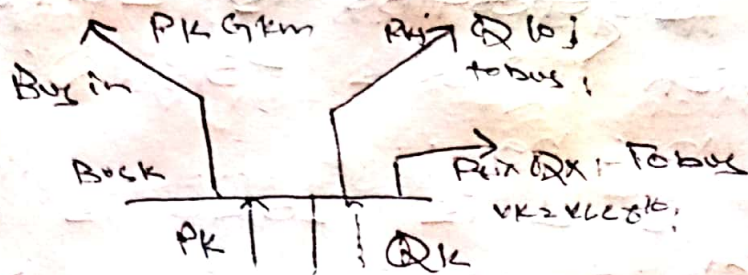
∴ Real Power injection.

(Pg 7)

Similarly Reactive power injection

$$Q_k = Q_{Gk} - Q_{Lk}$$

Diagram =



⇒ Now we will say injection into bus has voltage saying the generation and load if at particular bus has load is connected the load injection to that bus will be.

$$P_k = 0 - P_{Lk}$$

$$P_k = -P_{Lk}$$

$$Q_k = 0 - Q_{Lk}$$

$$Q_k = -Q_{Lk}$$

so load can be considered as negative injection.

⇒ From the diagram we see that a three line one going to bus i , j and k and so the 3rd one to m . These line will carry the power P_{ki}, Q_{ki} to bus i , P_{kj}, Q_{kj} to bus j and to bus k , in that case the value of P_{kj}, Q_{kj} will be negative.

(Pg 8)

KAMRAN AT 6790

So

$$P_k = P_{ki} + P_{kj} + P_{km}$$

$$Q_k = Q_{ki} + Q_{kj} + Q_{km}$$

∴ Real and Reactive Power is equal to the algebraic sum of P, Q Power going out.

Power Flow Equation:

we showed that Power flow equation are coming from the Network equation

$$\underline{I}_{BUS} = Y_{BUS} \cdot V_{BUS} \quad \text{--- (1)}$$

when \underline{I}_{BUS} is the vector of current injections into the busbar Y_{BUS} is the nxm matrix of ac admittance and V_{BUS} is the voltage phase at the ~~in busbars~~ buses of the power system.

⇒ For a particular bus k, we can write the equation as,

$$\underline{I}_k = \sum_{n=1}^N Y_{kn} V_n \quad \text{--- (2)}$$

where N = no of busbars.

Y_{kn} = admittances of the kn element
 V_n = voltage phases at bus n.

(Pg 9)

From equation we can write the complex power injection at bus bar K as

$$S_K = P_K + jQ_K = V_K I_K^* \quad (3)$$

Now we know the value of I_K from eq (3) substituting I_K in eq (3)

$$P_K + jQ_K = V_K \left[\sum_{n=1}^N Y_{kn} V_n \right]^* \text{ where } k, n = 1, 2, \dots, N$$

V_n is a phasor which has a magnitude and angle.

$$V_n = V_n e^{j\delta_n}$$

$$\text{and } Y_{kn} = Y_{kn} e^{j\alpha_{kn}} \quad k, n = 1, 2, \dots, N$$

Substituting V_n and Y_{kn} values in eq (3)

$$P_K + jQ_K = V_K \sum_{n=1}^N Y_{kn} V_n e^{j(\delta_K - \delta_n - \alpha_{kn})}$$

\therefore All angles δ_K with V_K
 δ_n with V_n
 α_{kn} with Y_{kn}

All Negative b/c of conjugates we can separate out the real & imaginary parts

Then we can write the real power injection into Bus K as

(Pg 10)

Kamran # 10 # 6990

$$P_k = V_k \sum_{n=1}^N Y_{kn} V_n \cos(\delta_k - \delta_n - \theta_{kn}) \quad (4)$$

similarly the Reactive Power Injection is

$$Q_k = V_k \sum_{n=1}^N Y_{kn} V_n \sin(\delta_k - \delta_n - \theta_{kn}) \quad (5)$$

So, we can see that these injection is related to the voltage magnitude and angle at various bus bars.

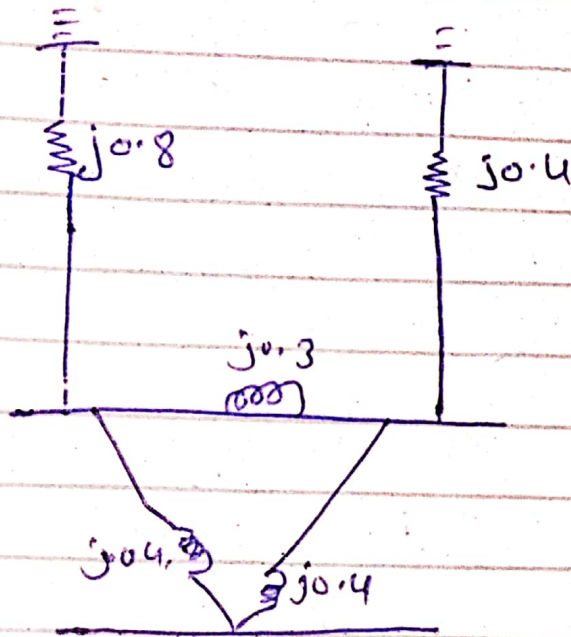
Eq (4) & (5) is said as the Power flow equation for the power network

(Pg 11)

Kamran # 10 # 6990

Q No 2

Solution!



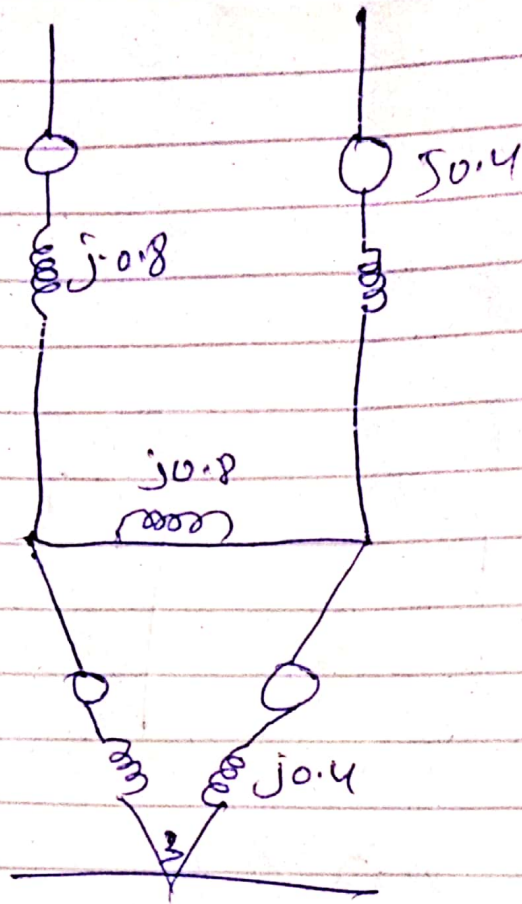
Z_{base}

$Z_{base} = \gamma \text{ bus}$

$$Z_{base} \begin{bmatrix} Z_{11} & Z_{12} & Z_{13} \\ Z_{21} & Z_{22} & Z_{23} \\ Z_{31} & Z_{32} & Z_{33} \end{bmatrix}$$

(Pg 12)

Kamran # 10# 8990



$$\begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} & Z_{13} \\ Z_{21} & Z_{22} & Z_{23} \\ Z_{31} & Z_{32} & Z_{33} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}$$

$$V_1 = Z_{11} I_1 + Z_{12} I_2 + Z_{13} I_3 \quad \text{--- (1)}$$

$$V_2 = Z_{21} I_1 + Z_{22} I_2 + Z_{23} I_3 \quad \text{--- (2)}$$

$$V_3 = Z_{31} I_1 + Z_{32} I_2 + Z_{33} I_3 \quad \text{--- (3)}$$

(Pg 13)

Kamran # ID# 6990

(Q1) write in matrix form the node equation necessary to solve for the voltage of the number buses of your own choice, the network is equivalent to the following two emf sources i.e.

$$E_a = 2.5 \angle 0^\circ$$

$$E_b = 4.5 \angle 0^\circ \text{ all in the per unit.}$$

Solution!

Given data!

node equation to solve for the voltage of the number buses of your own choice

Two emf source!

$$E_a = 2.5 \angle 0^\circ$$

$$E_b = 4.5 \angle 0^\circ \text{ all in the per unit.}$$

Solution!

$$\left[\begin{array}{l} E_a = 2.5 \angle 0^\circ \\ E_b = 4.5 \angle 0^\circ \end{array} \right]$$

(Pg 14)

Kamran # ID# 8990

$$\begin{bmatrix} E_a & 2.520^\circ \\ E_b & 4.540^\circ \end{bmatrix}$$

$$\begin{bmatrix} 2.520 & E_b \\ E_a & 4.540^\circ \end{bmatrix} \begin{bmatrix} E_1 \\ E_2 \\ E_3 \end{bmatrix}$$