

**Department of Electrical Engineering**  
**Sessional Assignment**  
**Date: 05/05/2020**

**Course Details**

**Course Title:** Signals & Systems  
**Instructor:** \_\_\_\_\_

**Module:** 04  
**Total Marks:** 20

**Student Details**

**Name:** \_\_\_\_\_

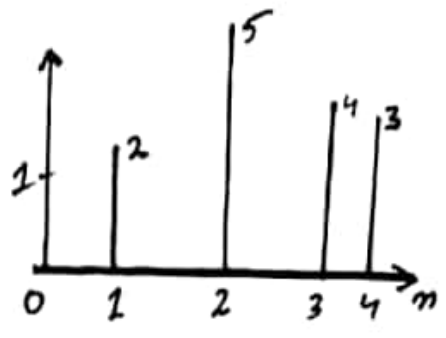
**Student ID:** \_\_\_\_\_

Q1.	<p>Evaluate the even and odd components for the given function.</p> <div style="text-align: center;"> </div>	<p>Marks 05 CLO 1</p>
Q2.	<p>Calculate the inverse Laplace transform of the given equation.</p> $Y(s) = \frac{s + 4}{s^2 + 4s - 12}$	<p>Marks 07 CLO 3</p>
Q3.	<p>i. Discuss the procedure of converting an analog signal into a digital one.            ii. Suppose an analog signal has a highest frequency of 60Hz. Outline the steps that will ensure that no aliasing occurs.</p>	<p>Marks 02+02 CLO 2</p>
Q4.	<p>Show that:  <math>x[n] * [h_1[n] * h_2[n]] = [x[n] * h_1[n]] * h_2[n]</math></p>	<p>Marks 04 CLO 2</p>

NAME : Badrul Zaman  
 ID : 13685  
 Assignment = Signal and System  
 Teacher = Mujtabah Ihsan Sb  
 Dated = 04/06/2020

Q1:

Evaluate the Even and odd components For Given Function:

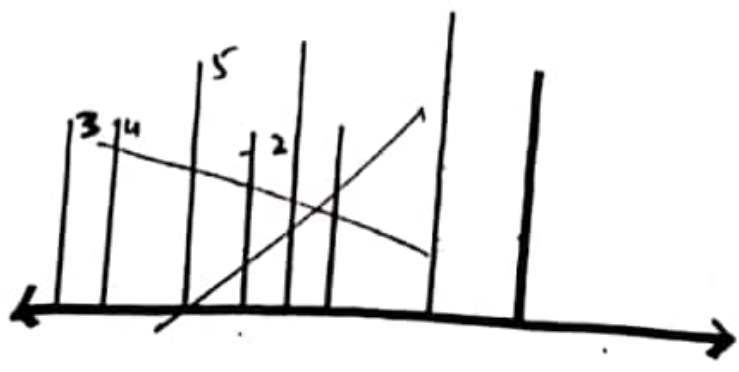


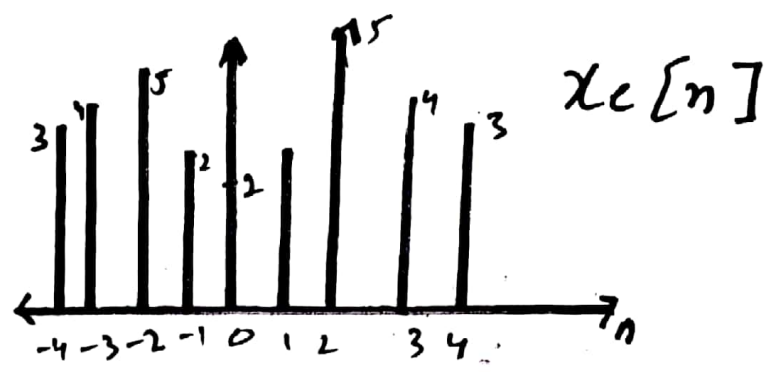
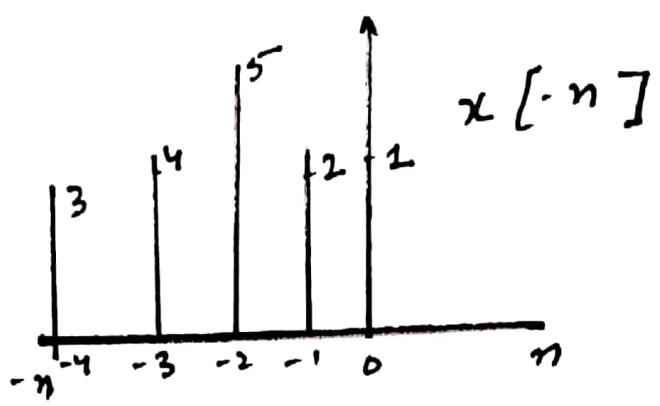
Sol:

As we know that the even components of a function can be written as

$$x_e[n] = \frac{x[n] + x[-n]}{2}$$

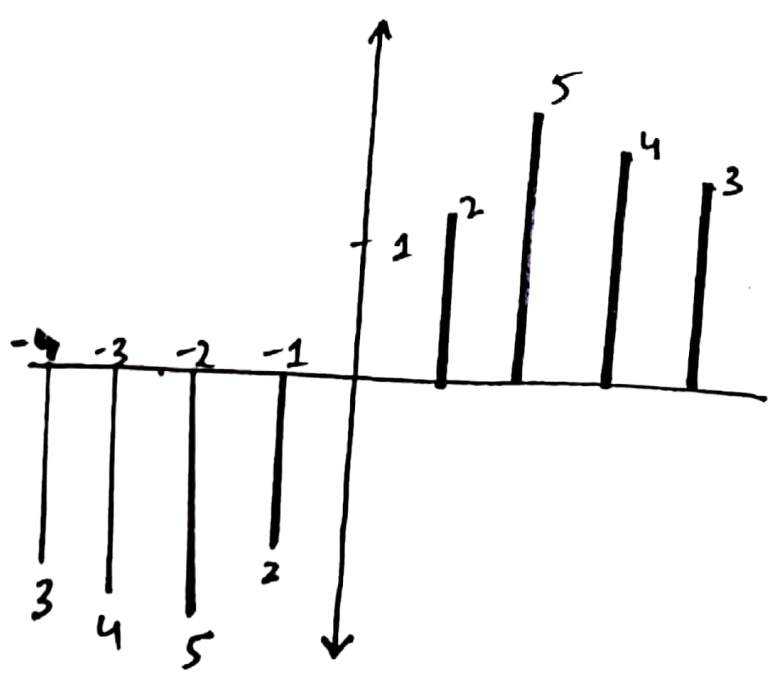
Reflect  $x[n]$  to get  $x[-n]$





odd components of a function can be written as:

$$x_o[n] = \frac{x[n] - x[-n]}{2}$$



Q2:  $y(s) = \frac{s+4}{s^2+4s-12}$

Sol:  $y(s) = \frac{s+4}{s^2+4s-12}$   
 $= \frac{s+4}{s^2+6s-2s-12}$   
 $= \frac{s+4}{s(s+6)-2(s+6)}$   
 $= \frac{s+4}{(s-2)(s+6)}$   
 $= \frac{s+4}{(s-2)(s+6)} = \frac{A}{s-2} + \frac{B}{s+6}$

Multiply both side by (s-2)(s+6)  
or Taking Lcm Both side

$\Rightarrow y(s) = (s+4) = A(s+6) + B(s-2)$  — (1)

Let  $s = -6$  in eq (1)

$(-6+4) = A(-6+6) + B(-6-2)$

$-2 = A(0) + B(-8)$

$-2 = B(-8) = B = \frac{-2}{-8} = \frac{1}{4} \Rightarrow B = \frac{1}{4}$

Let  $s = 2$  in eq (1)

(4)

$$s + 4 = A(s + 6) + B(s - 2)$$

$$2 + 4 = A(2 + 6) + B(2 - 2)$$

$$6 = A(8) + B(0)$$

$$6 = A(8) + 0$$

$$6 = A(8)$$

$$A = \frac{6}{8} \Rightarrow \frac{2}{4} \Rightarrow \frac{1}{2}$$

$$\boxed{A = \frac{1}{2}}$$

$$y(s) = \frac{1}{2} \frac{1}{(s-2)} + \frac{4}{(s+6)}$$

$$= \frac{1}{2} \mathcal{L}^{-1} \left( \frac{1}{s-2} \right) + 4 \mathcal{L}^{-1} \left( \frac{1}{s+6} \right)$$

$$= \frac{1}{2} e^{2t} + 4e^{-6t}$$

$$\boxed{y(s) = \frac{1}{2} e^{2t} + 4e^{-6t}}$$

, inverse Laplace Transform

Q3:-①

5

Ans:

- 1) Sampling
- 2) Quantization

(1) Sampling converts a continuous time continuous amplitude (real valued) signal to discrete time continuous amplitude (still real valued) signal. Remember only time axis is discretized and not the amplitude axis.

(2) Quantization converts the discrete time continuous amplitude signal to set of finite values so that it can be represented by finite bits and can be stored on computer.



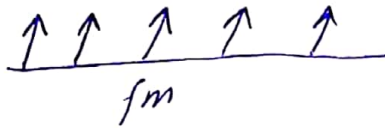
Q3:  
(ii)

(6)

Sol:-

$$F = 60 \text{ Hz}$$

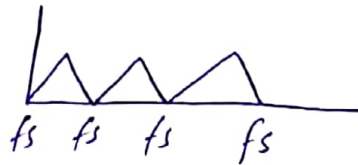
from Nyquist criteria



$$f_s \geq 2 f_m$$

$$f_s \geq 2 \times 60$$

$$f_s = 120$$



if  $f_s = 120 \text{ Hz}$  there will be no aliasing occurs at Nyquist criteria proves it.

24:-  
Sol:-

(7)

$$x[n] * [h_1[n] * h_2[n]] = [x[n] * h_1[n]] * h_2[n]$$

Consider

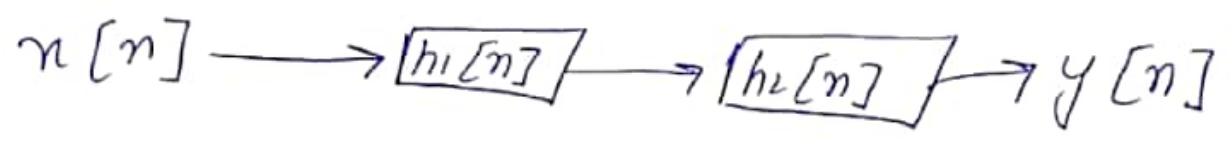
$$y[n] = [x[n] * h_1[n]] * h_2[n]$$

$$x[n] * h_1[n] = w[n]$$

Now

$$y[n] = [x[n] * h_1[n]] * h_2[n]$$

$$y[n] = w_1[n] * h_2[n]$$

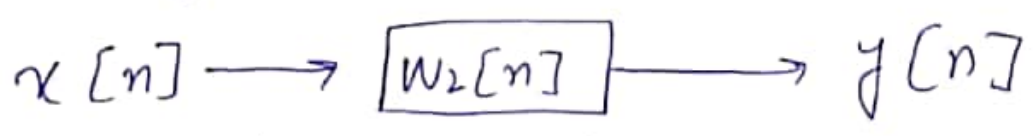


Now

$$w_2[n] = h_1[n] * h_2[n]$$

$$y[n] = x[n] * [h_1[n] * h_2[n]]$$

$$y[n] = x[n] * w_2[n]$$



As both block diagram give the same response we can write

$$x[n] * [h_1[n] * h_2[n]] = [x[n] * h_1[n]] * h_2[n]$$