

Department of Electrical Engineering
Assignment
Date: 14-04-2020

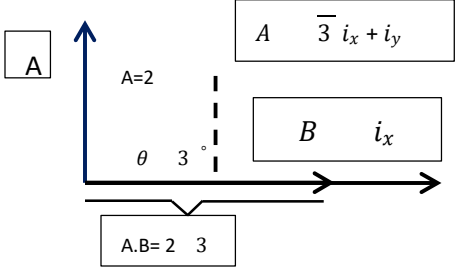
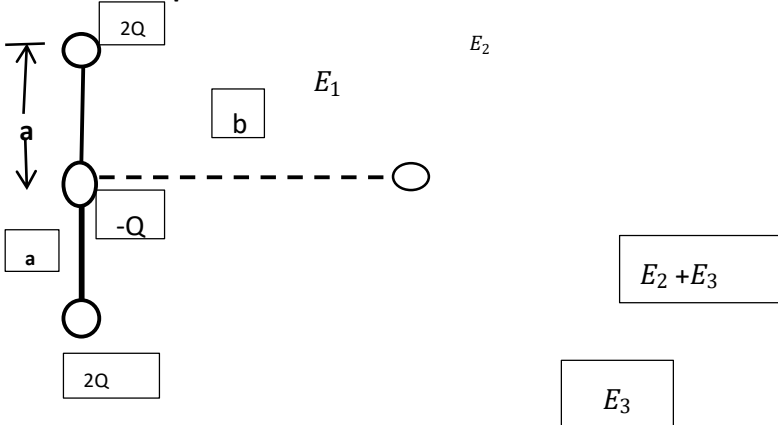
Course Details

Course Title: Electro Magnetic Field Theory Module: _____
 Instructor: _____ Total Marks: 30

Student Details

Name: Kirammat Ullah Student ID: 13290

| | | | |
|---|-----|--|------------------|
| Q1: Solve the following short Question | (a) | Transform the vector $B = yi(x+z)j$ located at point (-2,6,3) into cylindrical coordinates | Marks 2 CLO 1 |
| | (b) | Convert the point (3,4,5) from Cartesian to spherical coordinates | Marks 2 CLO 1 |
| | (c) | Find the spherical coordinates of A(2,3,-1) | Marks 2 CLO 1 |
| | (d) | Find the Cartesian coordinates of B(4.25,120) | Marks 2 CLO 1 |
| | (e) | Find the force between two charges when they are brought in contact and separated by 4cm apart, charges are 2nC and -1nC, in μN . | Marks 2 CLO 2 |
| | (f) | Find the electric field intensity of two Charges -2C and -1C separated by a distance 1m in air | Marks 2 CLO 2 |
| | (g) | Determine the charge that produce an electric field strength of 40 v/cm at a distance of 30cm in vacuum (in 10^{-8}c) | Marks 2 CLO 2 |
| | (h) | A charge of $2 * 10^{-7} \text{ C}$ is acted upon by a force of 0.1N. determine the distance to the other charge of $4.5 * 10^{-7}\text{C}$, both the charges are in vacuum | Marks 2 CLO 2 |
| Q2: | (a) | Find the angle between the vectors shown in figure. | Marks 4 |

| | | |
|-----|---|------------------|
| |  | CLO 1 |
| | <p>(b) Find the gradient of each of the following functions where a and b are constant</p> <p>(i) $f = ax^2 + by^3z$</p> <p>(ii) $f = ar^2 \sin \phi + brz \cos 2 \phi$</p> | Marks 4 CLO 1 |
| Q3: | <p>Three point charges are placed on the y-axis as shown. Find the electric field at point P on the x-axis.</p>  | Marks 6 CLO 2 |

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ID 13290

STUDENT NAME #

KIRAMATULLAH

ID NO #

13290

COURSE TITLE #

Electro Magnetic
Field Theory

DEPARTMENT #

BEE

TEACHER Name #

Dr. Rafiq

Mansoor

Kisamatullah

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Q NO 1

Part (A)

Transform the Vector $B = y_i(x+z)j$
located at point $(-2, 6, 3)$
into cylindrical coordinates.

Solutions:-

$$B = y_i(x+z)j$$

Given points are $(-2, 6, 3)$

then, we know

$$B = y_i(xj + zj)$$

$$B = y(xj + zj)$$

$$\Rightarrow \rho = \sqrt{x^2 + y^2}$$

$$\rho = \sqrt{(-2)^2 + (6)^2}$$

$$\rho = \sqrt{40}$$

$$\boxed{\rho = 6.32}$$

As we know that

$$z = z$$

so

$$\boxed{z = 3}$$

↳ As we know that

$$\phi = \tan^{-1} \left(\frac{y}{x} \right)$$

$$\phi = \tan^{-1} \left(\frac{6}{-2} \right)$$

$$\phi = \tan^{-1} (-3)$$

$$\boxed{\phi = -71.56}$$

So then,

$$B = (6.329, -71.56^\circ, 3z) \text{ Ans}$$

Q NO 1

Part (B)

Convert the point $(3, 4, 5)$ from Cartesian to spherical coordinates.

Solution:-

At Point $(3, 4, 5)$

$$x = 3, \quad y = 4, \quad z = 5$$

When spherical coordinates System

$$r, \theta, \phi$$

$$r = \sqrt{x^2 + y^2 + z^2}$$

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$$r = \sqrt{3^2 + 4^2 + 5^2}$$

$$r = \sqrt{9 + 16 + 25}$$

$$r = \sqrt{50}$$

$$\boxed{r = 7.07}$$

As we know that

$$\theta = \tan^{-1} \left(\frac{y}{x} \right)$$

$$\theta = \tan^{-1} \left(\frac{4}{3} \right)$$

$$\theta = \tan^{-1} (1.33)$$

$$\boxed{\theta = 53.1^\circ}$$

As we know that,

$$\phi = \tan^{-1} \left(\frac{\sqrt{x^2 + y^2}}{z} \right)$$

$$\phi = \tan^{-1} \left(\frac{\sqrt{3^2 + 4^2}}{5} \right)$$

$$\phi = \tan^{-1} \left(\frac{\sqrt{9 + 16}}{5} \right)$$

$$\phi = \tan^{-1} \left(\frac{\sqrt{25}}{5} \right)$$

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$$\phi = \tan^{-1} \left(\frac{5}{5} \right)$$

$$\phi = \tan^{-1} (1)$$

$$\boxed{\phi = \cancel{45} 45}$$

$$\underline{\underline{\rho = 7.07, \theta = 53.1^\circ, \phi = 45^\circ}} \quad \text{Ans}$$

QNO 1

Part (c)

Find the spherical coordinates of A (2, 3, -1)

Solution:-

(ρ, θ, ϕ) These are find=?

As

$$\rho = \sqrt{x^2 + y^2 + z^2}$$

$$\rho = \sqrt{2^2 + 3^2 + (-1)^2}$$

$$\rho = \sqrt{14}$$

$$\boxed{\rho = 3.74}$$

$$\theta = \tan^{-1} \left(\frac{y}{x} \right)$$

$$\theta = \tan^{-1} \left(\frac{3}{2} \right)$$

$$\theta = \tan^{-1} (1.5)$$

$$\theta = 56.3^\circ$$

As we know that,

$$\phi = \tan^{-1} \left(\frac{\sqrt{x^2 + y^2}}{z} \right)$$

$$\phi = \tan^{-1} \left(\frac{\sqrt{2^2 + 3^2}}{-1} \right)$$

$$\phi = \tan^{-1} \left(\frac{\sqrt{4+9}}{-1} \right)$$

$$\phi = \tan^{-1} \left(\frac{\sqrt{13}}{-1} \right)$$

$$\phi = \tan^{-1} (-3.60)$$

$$\phi = 74.4$$

$$\theta = 3.74, \theta = 56.3^\circ, \phi = 74.4$$

Ans

X

Q NO 1Part (D)

Find the Cartesian Coordinates of $B(4, 25, 120)$

Solution :-

The point of $B = (4, 25, 120)$ is given in spherical (ρ, θ, ϕ) so we have to find the (x, y, z)

Now

$$x = \rho \sin \theta \cdot \cos \phi$$

$$x = 4 \sin(25) \cdot \cos(120)$$

$$x = 4(0.42)(-0.5)$$

$$\boxed{x = -0.84}$$

As we know that,

$$y = \rho \sin \theta \cdot \sin \phi$$

$$y = 4 \sin(25) \cdot \sin(120)$$

$$y = 4(0.42)(0.86)$$

$$\boxed{y = 1.45}$$

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As we know,

$$Z = r \cos \theta$$

$$Z = 4 \cos(25^\circ)$$

$$Z = 4 (0.90)$$

$$Z = 3.62$$

$$(x, y, z) = (-0.84, 1.45, 3.62)$$

Ans

X

Question No 1

Part (E)

Find the force between two charges ~~2C~~ and when they are brought contact and separated by 4cm apart charges are 2nC and -1nC, in μN .

Solution:-

Given data :-

$$q_1 = 2\text{nC}, \quad q_2 = -1\text{nC}$$

$$d = 4\text{cm}$$

Required = F ?

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Solution:

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Where,

$$F = K \frac{q_1 q_2}{r^2}$$

As we know

$$K = \frac{1}{4\pi\epsilon_0}$$

$$F = \frac{2 \times 10^{-9} \times -1 \times 10^{-9}}{4(3.14) \times 8.85 \times 10^{-12} \times (4 \times 10^{-2})^2}$$

$$F = -1.124 \times 10^{-5}$$

$$F = -11.24 \mu\text{N}$$

Ans

QNO 1

Part (F)

Find the electric field Intensity of two charges -2C and -1C separated by a distance 1m in air

Solution:-

Given data:-

$$q_1 = -2\text{C}, \quad q_2 = -1\text{C}$$

$$\text{distance } d = 1\text{m in air}$$

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Required $E = ?$

Solution:-

$$E_1 = \frac{Kq_1}{d^2}$$

$$\therefore K = 9 \times 10^9$$

$$E_1 = \frac{9 \times 10^9 \times -2}{(1)^2}$$

$$E_1 = -18 \times 10^9 \text{ V/m}$$

Now, when

$$E_2 = \frac{Kq_2}{d^2}$$

$$E_2 = \frac{9 \times 10^9 \times (-1)}{(1)^2}$$

$$E_2 = -9 \times 10^9 \text{ V/m}$$

As we know that ,
 $E_T = E_1 + E_2$

$$E_T = -18 \times 10^9 + (-9 \times 10^9)$$

$$E_T = -18 \times 10^9 - 9 \times 10^9$$

$$E_T = -27 \times 10^9 \text{ V/m}$$

Ans

QNO 1Part (G)

Determine the charge that produce an electric field strength of 40 V/cm at a distance of 30 cm in vacuum (in 10^{-8} C).

Give data:-

$$E = 40 \text{ V/cm} \quad , \quad d = 30 \text{ cm}$$

Required

$$Q = ?$$

Solution:-

$$\Rightarrow E = \frac{kQ}{d^2}$$

$$\Rightarrow Ed^2 = kQ$$

$$\Rightarrow \frac{Ed^2}{k} = Q \longrightarrow \text{eq (1)}$$

Now putting values in eq (1)

$$\Rightarrow Q = \frac{Ed^2}{k}$$

$$\Rightarrow Q = \frac{40 \times (30)^2}{9 \times 10^9}$$

$$\Rightarrow Q = \frac{40 \times 900}{9 \times 10^9}$$

$$\Rightarrow \boxed{Q = 4 \times 10^{-6} \text{ C}}$$

OR

$$\Rightarrow \boxed{Q = 4 \mu\text{C}}$$

Ans

Q No 1

Part (H)

A charge of 2×10^{-7} is acted upon by a force of 0.1 N . Determine the distance to the other charge of $4.5 \times 10^{-7} \text{ C}$, both the charges are in vacuum

Given data

$$q_1 = 2 \times 10^{-7} \text{ C} \quad F = 0.1 \text{ N}$$

$$q_2 = 4.5 \times 10^{-7} \text{ C} \quad K = 9 \times 10^9$$

Required $d = ?$ Solution:-

By using formula #

then,

$$F = K \frac{q_1 q_2}{d^2}$$

$$d^2 = K \frac{q_1 q_2}{F}$$

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Now putting the value

$$d^2 = 9 \times 10^9 \left(\frac{2 \times 10^{-7}}{0.1} \right) (4.5 \times 10^{-7})$$

$$d^2 = \cancel{0.0081} \times 8.1 \times 10^{-3}$$

As

$$d^2 = 0.0081$$

Taking under root on both sides

$$\sqrt{d^2} = \sqrt{0.0081}$$

$$d = 0.09 \text{ m}$$

$$d = 9 \times 10^{-2} \text{ m}$$

OR

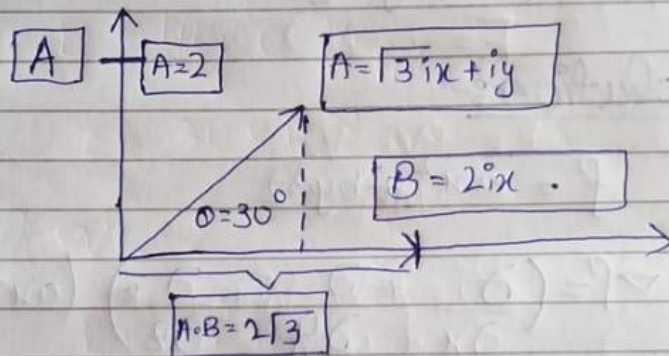
$$d = 9 \text{ cm}$$

Ans

X

Question No 2Part (a)AnswerSolution:-

$$A = \sqrt{3ix + iy}$$



$$A = \sqrt{3ix + iy}$$

$$|A| = 2$$

$$B = 2ix$$

$$|B| = 2$$

$$A \cdot B = 2\sqrt{3}$$

Now

$$A \cdot B = |A||B| \cos \theta_{AB}$$

$$\cos \theta_{AB} = \frac{A \cdot B}{|A||B|}$$

$$\theta_{AB} = \cos^{-1} \left(\frac{2\sqrt{3}}{|2||2|} \right)$$

$$\boxed{\theta_{AB} = 30^\circ}$$

Ans

Question No 2

Part (B)

Answer

Find Gradient

(i) $f = ax^2 + by^3z$

Solution:-

$$f = ax^2 + by^3z$$

$$\nabla f = \left(\frac{\partial}{\partial x} i + \frac{\partial}{\partial y} j + \frac{\partial}{\partial z} k \right) (ax^2 + by^3z)$$

$$\nabla f = \frac{\partial}{\partial x} ax^2 i + \frac{\partial}{\partial y} by^3z j + \frac{\partial}{\partial z} by^3z k$$

Now

$$\nabla f = 2axi + 3bzy^2j + by^3k$$

so

we find

$$\boxed{\nabla f = 2axi + 3bzy^2j + by^3k}$$

Ans

$$\text{ii) } f = a r^2 \sin \theta + b r z \cos^2 \theta$$

Solution :-

\Rightarrow Gradient the case of Spherical :-

$$\Rightarrow \nabla f = \frac{\partial f}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial f}{\partial \theta} \hat{\theta} + \frac{1}{r \sin \theta} \frac{\partial f}{\partial \phi} \hat{\phi}$$

$$\Rightarrow \nabla f = \frac{\partial}{\partial r} (a r^2 \sin \theta + b r z \cos^2 \theta) \hat{r} + \frac{1}{r}$$

$$\Rightarrow \frac{\partial}{\partial \theta} (a r^2 \sin \theta + b r z \cos^2 \theta) \hat{\theta} + \frac{1}{r \sin \theta}$$

$$\frac{\partial}{\partial \phi} (a r^2 \sin \theta + b r z \cos^2 \theta) \hat{\phi}$$

As,

$$\Rightarrow \nabla f = (2 a r \sin \theta + b z \cos 2 \theta) \hat{r} + \frac{1}{r} (0)$$

$$+ \frac{1}{r \sin \theta} (a r^2 \cos \theta - 2 b r z \sin \theta) \hat{\theta}$$

when,

$$\Rightarrow \nabla f = (2 a r \sin \theta + b z \cos 2 \theta) \hat{r} + \frac{1}{r \sin \theta}$$

$$(a r^2 \cos \theta - b r z \sin \theta) \hat{\theta}$$

\Rightarrow Gradient case with Cylindrical :-

$$\nabla f = \frac{\partial f}{\partial \rho} \hat{\rho} + \frac{1}{\rho} \frac{\partial f}{\partial \phi} \hat{\phi} + \frac{\partial f}{\partial z} \hat{z}$$

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$$\Rightarrow \nabla f = 0\hat{p} + \frac{1}{p} (a\delta^2 \cos \phi - 2b\delta z \sin 2\phi)\hat{0} + (a\delta \cos 2\phi)\hat{z}$$

\Rightarrow so that the first term will zero (0).

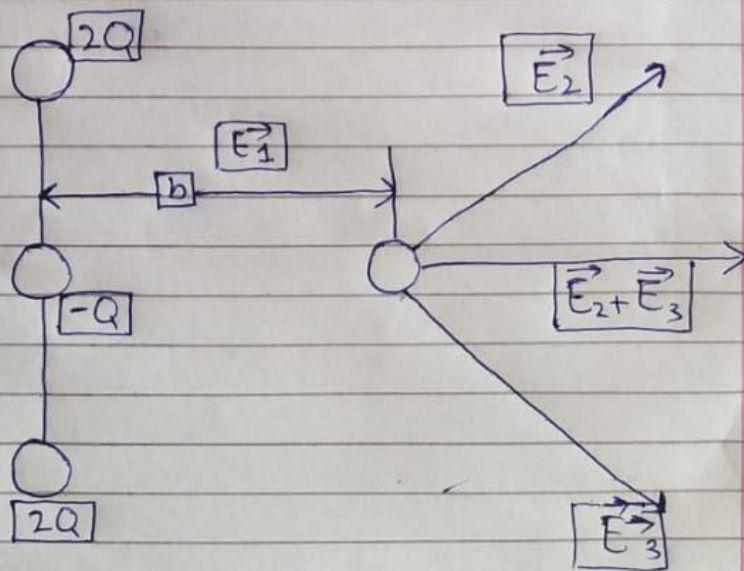
Then,

$$\nabla f = \frac{1}{p} (a\delta^2 \cos \phi - 2b\delta z \sin 2\phi)\hat{0} + (b\delta \cos \phi)\hat{z}$$

~~~~~x~~~~~x~~~~~

### Question No 3

Answer



**Solution:-**

⇒ Therefore, Distance between charge  $2Q$  and as point 'p' as

$$r^2 = b^2 + a^2$$

Then,

$$r = \sqrt{b^2 + a^2}$$

⇒ Therefore we assume the charge  $2Q$  make the angle of  $(\theta)$  and  $(-\theta)$  with  $x$ -axis.

Where the magnitude of

$$|\vec{E}_1| = |\vec{E}_2| = \frac{KQ}{r^2} = \frac{KQ}{b^2 + a^2}$$

$$= \frac{K(2Q)}{r^2}$$

$$= \frac{K(2Q)}{b^2 + a^2}$$

⇒ Therefore, the result of  $\vec{E}_1$  and  $\vec{E}_2$  is

$$\vec{E}_{1+2} = \vec{E}_1 + \vec{E}_2 = \vec{E}_{1x} + \vec{E}_{2x}$$

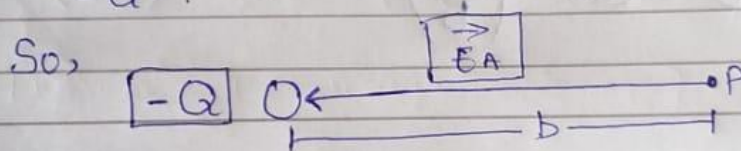
⇒ Component of  $y$ - will be canceled.

$$= \frac{K(2Q)}{b^2 + a^2} (\cos(\theta) + \cos(-\theta))$$

$$= \frac{K(2Q)}{b^2 + a^2} (2 \cos \theta)$$

$$= \vec{E}_{1+2} = \frac{4KQ \cos \theta}{b^2 + a^2} \rightarrow \text{eq (1)}$$

$\Rightarrow$  Therefore the electric field with point 'P' due to charge 'Q'. The charge is negative and electric field with point P will be directed towards charge "-Q".



$$\Rightarrow \vec{E}_A = \frac{-K(Q)}{b^2}$$

Therefore electric field at point 'P' will be

As,

$$\Rightarrow \vec{E}_{\text{net}} = \vec{E}_A + \vec{E}_1 + \vec{E}_2$$

$$= \frac{-K(Q)}{b^2} + \frac{4KQ \cos \theta}{b^2 + a^2}$$

$$= \frac{-KQ(a^2 + b^2) + 4KQb^2 \cos \theta}{b^2(a^2 + b^2)}$$

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$$= \frac{kQ}{b^2(a^2+b^2)} \left[ 4b^2 \cos\theta - (a^2+b^2) \right]$$

= Therefore,

$$k = 9 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$$

$$\vec{E}_{\text{net}} = 9 \times 10^9 Q \left[ 4b^2 \cos\theta - (a^2+b^2) \right]$$

So,

$$\theta = \tan^{-1} \left( \frac{a}{b} \right)$$

Now,

$$\vec{E}_{\text{net}} = \frac{9 \times 10^9 Q}{b^2(a^2+b^2)} \left[ 4b^2 \cos \left[ \tan^{-1} \left( \frac{a}{b} \right) \right] - (a^2+b^2) \right]$$

