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3rd Semester As CS  
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Digital Logic Design.

- Q1. Convert each of the following  
(a)  $45.45_{10} = (?)_2$

### Division Method

$$\begin{array}{r} 2 \quad 45 \\ 2 \quad 22 - 1 \\ 2 \quad 11 - 0 \\ 2 \quad 5 - 1 \\ 2 \quad 2 - 1 \\ 1 \quad 1 - 0 \end{array}$$

101101 Now for ~~fraction~~ fraction

### multiplication

$$\begin{array}{l} 0.25 \times 2 = 0.5 - 0 \\ 0.5 = 1 - 1 \end{array}$$

$(101101.01)_2$  Ans.



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b)  $(0000000 \cdot 1010)_2 = ( ? )_{10}$

**Solution:**

$$1 \times 2^7 + 0 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$$

$$+ 0 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} + 0 \times 2^{-4}$$

$$(128 + 0.625)_{10}$$

$$(128.625)_{10} \text{ Ans.}$$

c)  $(4D7F)_{16} = ( ? )_{10}$

**Solution:**

$$4 \times 16^3 + 13 \times 16^2 + 7 \times 16^1 + 15 \times 16^0$$

$$= (19839)_{10} \text{ Ans.}$$

d)  $(128)_{10} = ( ? )_{16}$

**Solution:**

$$\begin{array}{r|l} 16 & 128 \\ & 8 - 0 \end{array}$$

$$(128)_{10} = (80)_{16}$$

e)  $(3A6F)_{16} = ( ? )_2$

**Solution:**

3    A    6    F

0011    1010    0110    1111

$$(0011101001101111)_2 \text{ Ans.}$$

$$f \quad (110000111100101)_2 = (?)_{16}$$

**Solution:**

$$\begin{array}{cccc} \underline{1100} & \underline{0011} & \underline{1100} & \underline{10101} \\ C & 3 & E & F \end{array}$$

$$(C3EF)_{16} \text{ Ans.}$$

$$g \quad (6173)_8 = (?)_{16}$$

**Solution:**

$$6 \times 8^3 + 1 \times 8^2 + (7 \times 8^1) + 3 \times 8^0$$

$$= 3825$$

$$= (3825)_{10} \text{ Ans.}$$

$$h \quad (169)_{10} = (?)_8$$

**Solution:**

$$169/8 = 21.125 \rightarrow 0.125 \times 8 = 2$$

$$21/8 = 2.625 \rightarrow 0.625 \times 8 = 5$$

$$\frac{2}{8} = 0.25 \rightarrow 0.25 \times 8 = 2$$

$$(169)_{10} = (251)_8$$

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i)  $(2A7D)_{16} = (?)_8$

Solution:

Hexadecimal  $\rightarrow$  Binary

2 A 7 D

0010 1010 0111 1101

Group of 3 for Octa

010 101 001 111 101

2 7 1 7 5

$$(2A7D)_{16} = (27175)_8$$

j)  $(11111111)_2$

Solution:

$$(1 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0)$$

$$= 64 + 32 + 16 + 8 + 4 + 2 + 1$$

$$= 127$$

sign-bit 1

So

$$(11111111)_2 = (-127)_{10}$$

k)  $(-12)_{10} = (?)_2$

Solution:

$$(-12)_{10} = (00001100)_2$$

Ans.



L  $198 = (?)_{BCD}$

**Solution:**

1 9 8  
0001 1001 1000

$198 = (000110011000)_{BCD}$

M  $10000110000 = (?)_{10}$   
BCD

**Solution:**

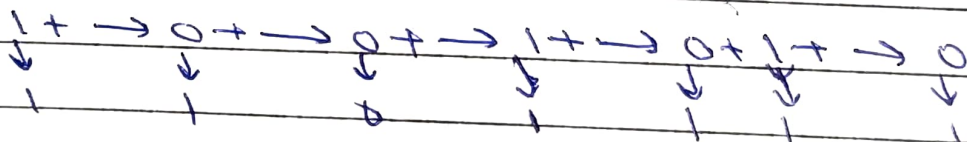
10000 110000  
8 7 0

So

$(10000110000)_2 = (870)_{10}$

N  $(1001010)_2 = (?)_{Gray}$

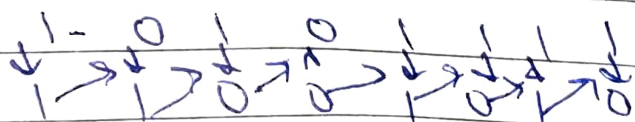
**Solution:**



$(110111)_{Gray}$  Ans.

O  $(1010111)_{Gray} = (?)_2$

**Solution:**



$(1001010)_2$  Ans.

Q P  $(01000001)_2 = (?)_{\text{ASCII}}$

**Solution:**

$$01000001 \rightarrow 65 \rightarrow 0$$

$$= (065)_{\text{ASCII}}$$

Q  $111000 = (?)_{\text{Even Parity}}$

**Solution:**

Must have even number of 1  
 $(11000) = (1111000)_{\text{Even Parity}}$

Q Calculate each of the following.

Q (a)  $01111111_2 - 00001111_2$

**Solution:**

$$\begin{array}{r} 00000111 \\ 11111000 \\ \hline 11111001 \end{array}$$

$$+ 1$$

$$\hline 11111001$$

$$\begin{array}{r} 01111111 \\ + 1111001 \\ \hline 01111000 \end{array}$$

$$+ 1111001$$

$$\hline 01111000$$

$(01111000)_{\text{ASCII}}$

(b)  $(01101010)_2 \times (11110001)_2$

**Solution:**

$$\begin{array}{r}
 11110001 \\
 00001110 \quad \text{1st comp} \\
 \hline
 00001111
 \end{array}$$

$$\begin{array}{r}
 01101010 \\
 \times 00001111 \\
 \hline
 01101010 \\
 01101010x \\
 01101010xx \\
 01101010xxx \\
 00000000xxx \\
 00000000xxxx \\
 00000000xxxxx \\
 00000000xxxxxx \\
 \hline
 0000101010110
 \end{array}$$

Ans.

c  $(10001000)_2 \div (00100010)_2$

**Solution:**

?

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d  $60_{16} - 3F_{16}$

Solution:

$3F = 00111111$

2's complement

$$\begin{array}{r}
 00111111 \\
 11000000 \\
 \hline
 + 1 \\
 \hline
 11000001
 \end{array}$$

2's complement

$11000001 \Rightarrow C1_{16}$

Now add  $60_{16} + C1_{16}$

$$\begin{array}{r}
 60 \\
 C1 \\
 \hline
 34
 \end{array}$$

e  $(00010110)_{80} + (00010101)_{80} = (?)$

$$\begin{array}{r}
 0001 \} 0110 \\
 0001 \} 0101 \\
 \hline
 0010 \} 1011 \\
 \hline
 3 \quad | \quad 1
 \end{array}$$

(31) Ans.



Q3 Apply CRC to the data bits 110100112 using the generator code 1010, to produce the transmitted CRC

$$D = 11010011$$

$$G = 1010$$

$$D = 110100110000$$

$$D = 110100110000$$

$$P \quad 1010$$

$$110100110000$$

$$\underline{1010}$$

$$1110$$

$$\underline{1010}$$

$$1000$$

$$\underline{1010}$$

$$1011$$

$$\underline{1010}$$

$$1000$$

$$1010$$

$$\underline{0100}$$

$$R \neq 0$$

$$110100110100$$

$$\underline{1010}$$

$$1110$$

$$\underline{1010}$$

$$1000$$

$$\underline{1010}$$

$$1011$$

$$\underline{1010}$$

$$1010$$

$$\underline{1010}$$

$$00$$

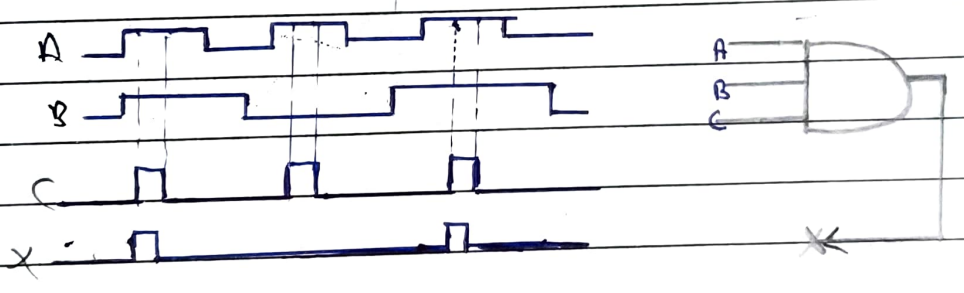
$$R = 0$$

\* Transmitted Code (110100110100)

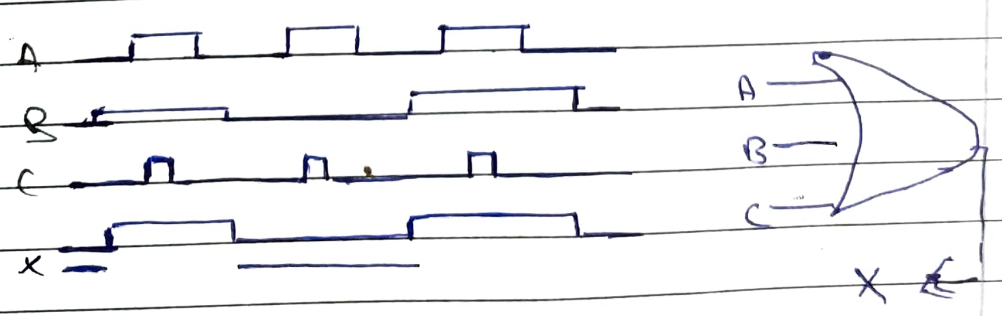
Q4 Assume that the code produced in problem Q-3 occur an error in the most significant bit during trans. Apply CRC to detect the error.

?

Q5 The input waveform in figure 1 is applied to 3-input AND gate. Show the output waveform is proper relation to input with timing diagram.



Q6 3-input OR gate



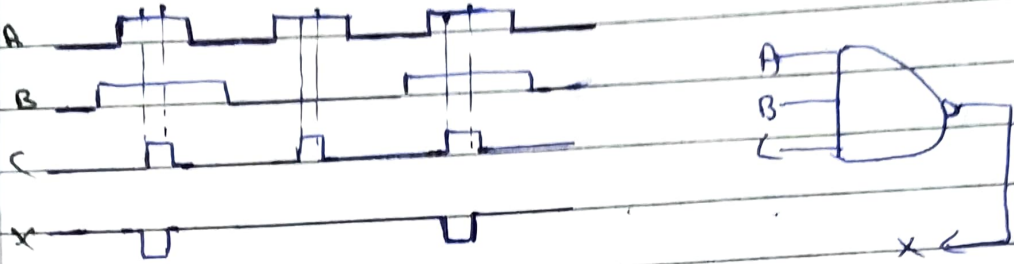
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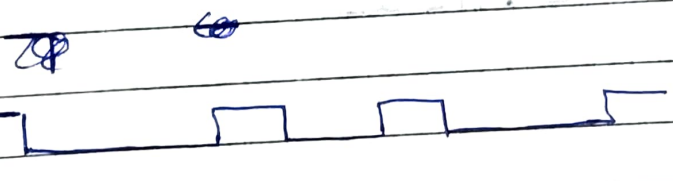
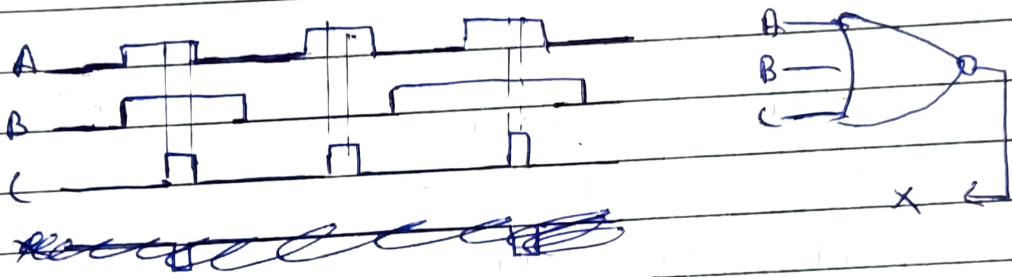
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Q7 3-input NAND gate

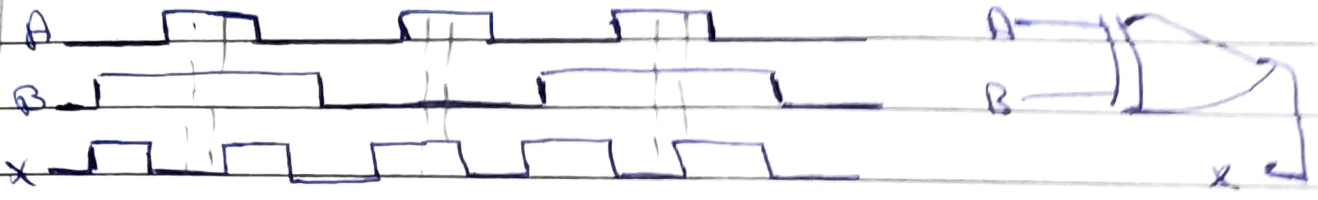


Q8 3-input NOR gate.



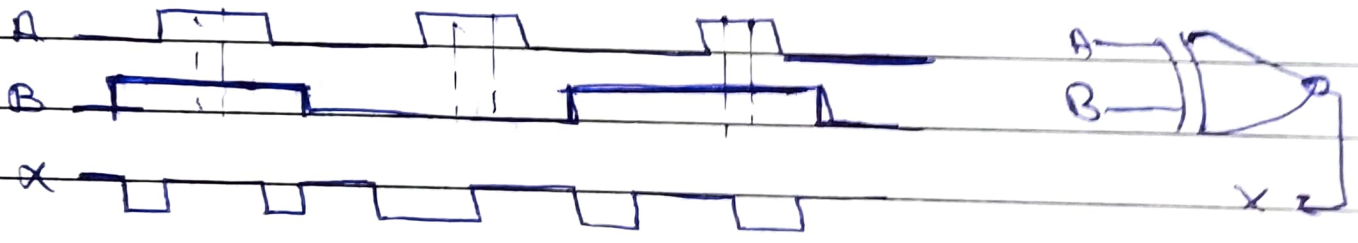


Q9 2 input XOR gate.



Q10

**XNOR GATE**



Q11

Using Boolean Algebra techniques, Simplify the following expressions as much as possible.

$$\begin{aligned}
 & A\bar{B} + A\bar{B}C + A\bar{B}CD + A\bar{B}CDE \\
 &= A\bar{B}(1+C) + A\bar{B}CD(1+E) \\
 &= A\bar{B}(1) + A\bar{B}CD(1) \\
 &= A\bar{B} + A\bar{B}CD \\
 &= A\bar{B}(1+CD) \\
 &= A\bar{B}(1) \\
 &= A\bar{B}
 \end{aligned}$$

Q 12 Convert the following expressions to standard SOP form  $(C+D)(\bar{A}+D)$

**Solution:**

$$C\bar{A} + CD + D\bar{A} + DD$$

$$= C\bar{A} + CD + D\bar{A} + D \quad \text{multiply missing}$$

$$= C\bar{A}(D+\bar{D}) + CD(A+\bar{A}) + D\bar{A}(C+\bar{C}) + D(A+\bar{A}) \text{ term.}$$

$$= C\bar{A}D + C\bar{A}\bar{D} + CDA + CD\bar{A} + D\bar{A}C + D\bar{A}\bar{C} + DA + D\bar{A}$$

$$= C\bar{A}D + C\bar{A}\bar{D} + CDA + CD\bar{A} + D\bar{A}C + D\bar{A}\bar{C} + DAC + D\bar{A}\bar{C}$$

$$= C\bar{A}D + C\bar{A}\bar{D} + CDA + CD\bar{A} + D\bar{A}C + D\bar{A}\bar{C} + DAC + D\bar{A}\bar{C}$$

$$= ACD + \bar{A}CD + \bar{A}C\bar{D} + \bar{A}\bar{C}\bar{D} + \bar{A}\bar{C}D$$

Q 13 Write the standard POS expression using the standard SOP expression obtained in Q.12

**Solution:**

$$ACD + \bar{A}CD + \bar{A}C\bar{D} + \bar{A}\bar{C}\bar{D} + \bar{A}\bar{C}D$$

$$(111) \quad (011) + (010) + (001) + (001)$$

$$(A+C+D)(\bar{A}+C+D)(\bar{A}+C+\bar{D})(\bar{A}+\bar{C}+D)$$

$$(A+\bar{C}+D)$$

Q14

Draw a single truth table for both POS and SOP expression obtained in Q12 and Q13:

A	C	D	X	POS/SOP
0	0	0	0	$A + C + D$
0	0	1	0	$\bar{A} + C + D$
1	0	1	0	$\bar{A} + C + \bar{D}$
1	1	0	0	$\bar{A} + \bar{C} + D$
0	1	0	0	$A + \bar{C} + D$
1	1	1	1	<del><math>A + C + D</math></del> $ACD$
0	1	1	1	$\bar{A}CD$
0	1	0	1	$\bar{A}C\bar{D}$
0	0	1	1	$\bar{A}\bar{C}D$
1	0	1	1	$A\bar{C}D$

POS:

$$(A + C + D)(\bar{A} + C + D)(\bar{A} + C + \bar{D})(\bar{A} + \bar{C} + D)(A + \bar{C} + D)$$

SOP:

$$(ACD) + (\bar{A}CD) + (\bar{A}C\bar{D}) + (\bar{A}\bar{C}D) + (A\bar{C}D)$$



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Q15 Use a karnaugh map to simplify expression to a minimum sop form

$$\bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}C + AB\bar{C}$$

Solution:

$$(000) + (010) + (101) + (110)$$

		AB			
		00	01	11	10
C	0	1		1	
	1		1		1

$$(\bar{A}\bar{B}C) + \bar{A}B\bar{C} (\bar{A}\bar{B}C + A\bar{B}C)$$

Q16 Obtain the minimum POS expression for the karnaugh map used in Q15

Ans:

		AB			
		00	01	11	10
C	0	1	0	1	0
	1	0	1	0	1

$$(A+B+\bar{C})(A+\bar{B}+C)(A+B+\bar{C})(A+B+C)$$

Q  
17

Write the output expression for circuit

NO ANSWER ?

Q  
18

Q 18

NO ANSWER ?

Q  
19

~~Q 19~~

9 don't know Answer.

Q  
20

Implement a logic circuit for the truth table.

**Solution.**

$$(\bar{A}\bar{B}C\bar{D}) + (\bar{A}\bar{B}CD) + (\bar{A}BC\bar{D}) + (\bar{A}BCD) + (A\bar{B}C\bar{D}) + (A\bar{B}CD) + (ABC\bar{D}) + (ABCD)$$

**Simplify form**

$$(\bar{A}\bar{B}C\bar{D}) + (\bar{A}BC\bar{D}) + (A\bar{B}CD)$$

Don't know about gates.