



Name	Fawad Niaz
ID#	14568
Module	4 th
Subject	Electrical Network Analysis
Instructor	Dr.Shahreear Shafiq
Assingment	Sessional

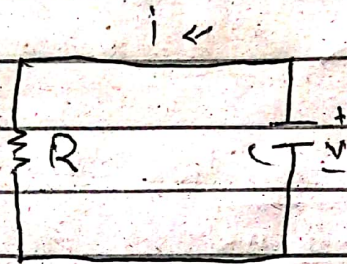
Q No 1:

For the circuit in Fig (c) if $v = 10e^{-4t}$ V $t > 0$ and $i = 0.2e^{-4t}$ A $t > 0$

(a) Find R & C (b) — (c) — (d)

50% of the initial energy.

Ans:



step 1:

(A)

$$T = RC = \frac{1}{4}$$

$$\Rightarrow i = C \frac{dv}{dt}$$

$$\Rightarrow -0.2e^{-4t} = C(10)(-4)e^{-4t}$$

$$\Rightarrow C = 5 \text{ mF}$$

$$R = \frac{1}{4C} = 50 \Omega$$

step 2

(B)

$$T = RC = \frac{1}{4} = 0.25 \text{ s}$$

step 3:

(C)

$$W_C(t) = \frac{1}{2} C v^2$$

$$\Rightarrow \frac{1}{2} (5 \times 10^{-3}) (100)$$

$$\Rightarrow 250 \text{ mJ}$$

step 4:

$$(17) \quad v_R = \frac{1}{2} \times \frac{1}{2} (V_0)^2$$

$$\Rightarrow \frac{1}{2} (V_0)^2 (1 - e^{-2t})$$

$$0.5 = 1 - e^{-8t} \Rightarrow e^{-8t} = \frac{1}{2}$$

OR

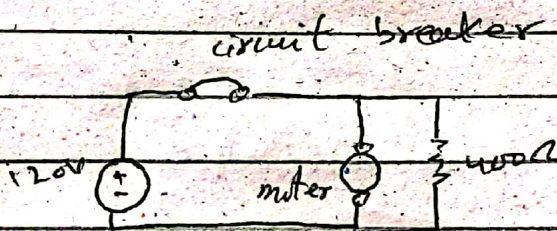
$$e^{8t_0} = 2$$

$$t_0 = \frac{1}{8} \ln(2)$$

$$\Rightarrow \boxed{186.6 \text{ ms}}$$

Q2: A 120V dc generator energize a motor whose coil

Ans:



step 1:

Let the inductor current for $t < 0$

$$i(0) = \frac{120}{100} = \frac{12}{10}$$

$$\Rightarrow \frac{6}{5} = 1.2 \text{ A}$$

For $t > 0$ we have an RL-circuit

$$\tau = \frac{L}{R} = \frac{50}{100 + 50}$$

$$\Rightarrow \frac{50}{500} = \frac{5}{50}$$

$$\Rightarrow \frac{1}{10} = 0.1$$

$$i(\infty) = 0$$

$$i(t) = i(\infty) + [i(0) - i(\infty)]e^{-t/\tau}$$

$$i(t) = 1.2e^{-10t}$$

At $t = 100\text{ms} = 0.1\text{s}$

$$i(0.1) = 1.2e^{-1} = 0.441\text{A}$$

which is the same as the current through the resistor.

step 02 :-

$$T = R_{\text{rms}} = 60\mu\text{s}$$

An integrator

$$T < 0.1, T = 6\mu\text{s}$$

$$T_{\text{max}} = 6\mu\text{s}$$

Q No 3 :-

The response of series RLC circuit

Ans

step 1:

series RLC circuit.

$$V_c(t) = 30 - 10e^{-2t} + 30e^{-10t}$$

$$V_c(t) = V_1 + A_1e^{\alpha_1 t} + A_2e^{\alpha_2 t} \quad [\alpha > 0]$$

$$40e^{-20t} - 60e^{-30t} \text{ mA}$$

$$\Rightarrow i(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t} \quad [\alpha > \omega_0]$$

comparing these eqn --- we get

$$V_s = 30$$

$$A_1 = -10 ; \quad A_2 = 30 ;$$

$$s_1 = -20 ; \quad s_2 = -1 \rightarrow \textcircled{a}$$

$$A'_1 = 40 ; \quad A'_2 = -60 ;$$

$$s'_1 = -20 ; \quad s'_2 = -10 \rightarrow \textcircled{b}$$

step 2 :

Now Eqn (a) & (b)

$$s_1 = -\alpha + \sqrt{\alpha^2 - \omega_0^2} \quad \text{AND} \quad s_2 = -\alpha - \sqrt{\alpha^2 - \omega_0^2}$$

$$s_1 + s_2 = -2\alpha \quad \{ \quad s_1 s_2 = \omega_0^2$$

$$\left[\text{where } \alpha = \frac{R}{2L} ; \quad \omega_0 = \frac{1}{\sqrt{LC}} \right]$$

$$\Rightarrow -30 = -2\alpha$$

$$\Rightarrow \alpha = 15 \quad \Rightarrow \quad \frac{R}{2L} = 15 \rightarrow \textcircled{c}$$

$$200 = \omega_0^2 \Rightarrow \frac{1}{LC} = 200 \rightarrow \textcircled{d}$$

step 03 :-

$$i(t) = C \frac{dv}{dt}(t) = C [200e^{-20t} - 300e^{-30t}]$$

$$(A_1 e^{s_1 t} + A_2 e^{s_2 t}) \times 10^{-3} \text{ A} = C [200e^{-20t} - 300e^{-30t}]$$

(OR)

$$[s_1 = s_1', \quad s_2 = s_2']$$

$$\Rightarrow 200C - A_1 = 40 \times 10^{-3}$$

$$\Rightarrow C = 200 \times 10^{-6} \text{ F} \Rightarrow C = 200 \mu\text{F}$$

using eqn (C) & (D)

$$L = \frac{1}{200C} = \frac{1}{200 \times 200 \times 10^{-6}} \Rightarrow L = 25 \text{ H}$$

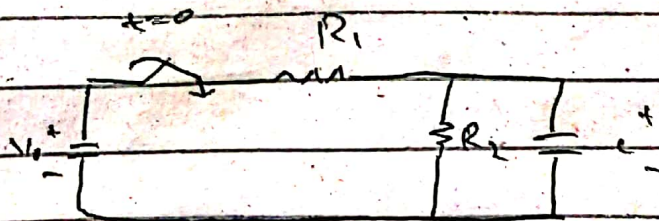
$$\& R = 30L = 30 \times 25 = 750 \Omega$$

$$\left. \begin{array}{l} C = 200 \mu\text{F} \\ L = 25 \text{ H} \\ R = 750 \Omega \end{array} \right\} \text{ Answers.}$$

Q No 4

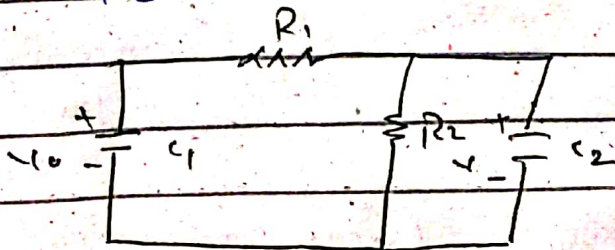
The circuit Fig. 3 is the electrical analog

ANS:



For $t=0$, $v_C(0) = 0$

For $t > 0$ the circuit is shown below



$$V_0 - \frac{V}{R_1} = \left(\frac{V}{R_2}\right) + C_2 \frac{dV}{dt}$$

$$V_0 = V \left(1 + \frac{R_1}{R_2}\right) + R_1 C_2 \frac{dV}{dt}$$

$$60 = \left(1 + \frac{5}{2.5}\right) + \left(5 \times 10^{-6} \times 5 \times 10^{-6}\right) \frac{dV}{dt}$$

$$60 = 3V + 25 \frac{dV}{dt}$$

$$V(t) = V_s + \left[A e^{-st/25} \right]$$

where

$$3V_s = 60 \text{ yields } V_s = 20$$

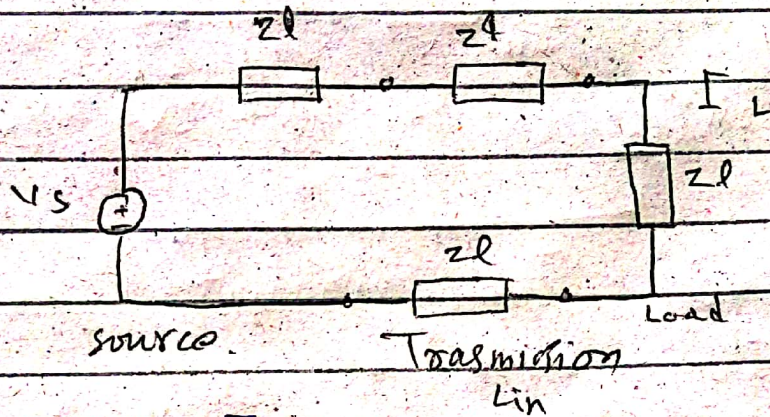
$$V(0) = 0 = 20 + A \text{ or } A = -20$$

$$V(t) = 20 \left(1 - e^{-st/25}\right) V.$$

Q No 5:

A power transmission system is modeled

Ans



$$Z = z_{at} + z_l + z_l$$

$$= (1 + 0.8 + 23 \cdot 2) + j(0.5 + 0.6 + 18.9)$$

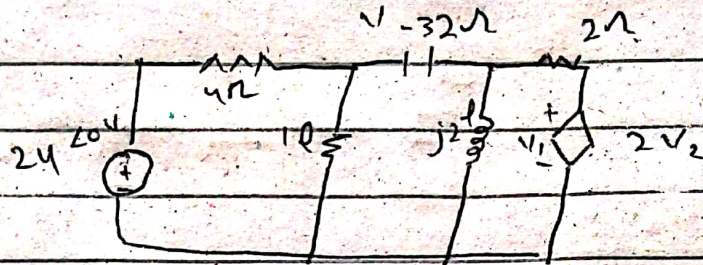
$$Z = 25 + j20$$

$$I_L = \frac{V_s}{Z} = \frac{115 \angle 0^\circ}{32 - j2} \angle -38.66^\circ$$

$$I_L = 3.592 \angle -38.66 \text{ A}$$

Q 6 :- For the circuit in Fig-5 find the current i

Ans :-



Consider the circuit as shown

At node 0

$$\frac{24 - V_0}{4} = \frac{V_0}{10} + \frac{V_0 - V_1}{-j}$$

$$24 = (5 + j4)V_0 - j4V_1 \rightarrow (1)$$

At node 1

$$\frac{V_0 - V_1}{-j} + 2V_0 = \frac{V_1}{j2}$$

$$V_1 = (2 - j4)V_0 \rightarrow (2)$$

substituting (2) into (1)

$$24 = (5 + j4 - j8 - 16)V_0$$

$$V_0 = \frac{-24}{11 + j4} \quad V_1 = \frac{(-24)(2 - j4)}{11 + j4}$$

voltage across the dependent source is

$$V_2 = V_1 + (2)(2V_0) = V_1 + 4V_0$$

$$V_2 = \frac{-24}{11 + 4j} (2 - j4) = \frac{(-24)(6 - j4)}{11 + 4j}$$

$$P = \frac{1}{2} V_2 I^* = \frac{1}{2} V_2 (2 \angle 0^\circ)$$

$$P = \frac{(-24)(6 - j4)}{11 + 4j} = \frac{24}{11 - j4}$$

$$= \left(\frac{576}{137} \right) (6 - j4)$$

$$P = 25.23 - j16.82 \text{ VA}$$

(Q 7) A balanced Y-load to a
60 Hz Three phase

ANS:

step of 2.

$$|V_{ab}| = \sqrt{3}V_p = 240 \Rightarrow V_p = \frac{240}{\sqrt{3}}$$

$$= 138.56$$

$$V_{an} = V_p \angle -30^\circ$$

$$P_f = 0.5 = \cos \theta \Rightarrow \theta = 60^\circ$$

$$P = S \cos \theta \Rightarrow S = \frac{P}{\cos \theta} = \frac{5}{0.5} = 10 \text{ KVA}$$

$$Q = S \sin \theta = 10 \sin 60 = 8.666$$

$$S_p = 5 + j8.66 \text{ KVA}$$

But.

$$S_p = \frac{V_p^2}{Z_p} \Rightarrow Z_p = \frac{V_p^2}{S_p} = \frac{138.56^2}{(5 + j8.66) \times 10^3}$$

$$= 0.96 - j1.66 \Omega$$

$$Z_p = 0.96 + j1.66 \Omega$$