

ID

7962

Section

B

Dep

Be (civil)

Paper

Fluid mechanics

Part AEnergy head

It is the sum of all energy head at a point in a fluid.

Form of energy Head.

There are various forms of energy Head which are in following

- (1) Kinetic Head
- (2) Potential Head
- (3) Pressure Head.

Kinetic Head

It is the kinetic energy per unit weight of the fluid.

Mathematical Form

P2
Q1
PA

$$\frac{K.E}{w} = \frac{\frac{1}{2} m v^2}{m g}$$

$$\frac{K.E}{w} = \frac{1}{2} \frac{v^2}{g}$$

This is also known as velocity Head.

Unit

The unit is meter (m)

Potential Head

It is the potential energy per unit weight of the fluid.

Mathematical Form.

$$\frac{P.E}{w} = \frac{m g h}{m g} = h$$

Pressure Head

P3
P1
PA

The vertical height of the free surface above any point in a liquid at rest is Pressure Head.

Mathematical Form

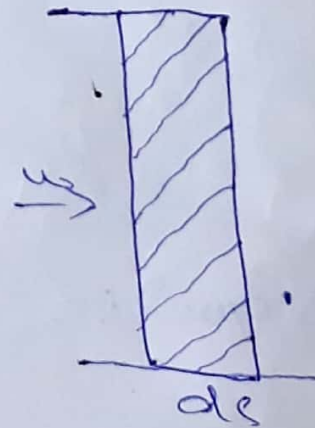
$$\text{Pressure Head} = \frac{P \cdot E}{\text{weight}} = \frac{P}{\gamma}$$

or

$$\frac{F \cdot ds}{w}$$

$$= \frac{P \cdot A \cdot ds}{w}$$

$$= \frac{P \cdot \cancel{A}}{w} = \frac{P}{\gamma} \text{ is pressure.}$$



Q1 part = B

Hydraulic grade line

The surface or profile of water flowing in an open channel or a pipe flowing partially full. In a pipe is under pressure the hydraulic grade line is that level water would rise to in a small vertical tube connected to the pipe also see energy grade line.

Hydraulic radius

The ratio of the cross-sectional area of a channel or pipe in which a fluid is flowing to the wetted perimeter of the conduit.

Energy Grade Line

5

A line that represents the elevation of energy head (in feet or meters) of water flowing in a pipe conduit or channel. The line is drawn above the hydraulic grade line a distance equal to the velocity head ($v^2/2g$) of the water flowing at each section or point along the pipe or channel.

Question = 2

Part = A

Given data

$$\text{velocity} = U = 2 \text{ m/s}$$

$$\text{pressure} = P = 300 \text{ kPa}$$

$$\text{datum} = Z = 5 \text{ m}$$

Sol

$$H = \text{pressure head} + \text{KE} + \text{PE}$$

$$H = \frac{P}{\rho} + \frac{U^2}{2g} + Z$$

$$H = \frac{300 \times 10^3}{9810} + \frac{2^2}{2 \times 9.81} + 5$$

$$H = 35.7849 \text{ m}$$

Q No 2 Part = B

(7)

Given data

$$\text{Diameter} = d_1 = 300 \text{ mm}$$

$$\text{Diameter} = d_2 = 200 \text{ mm}$$

$$\begin{aligned} \text{Pressure} &= p_1 = 300 \text{ kPa} = 300 \times 10^3 \text{ N/m}^2 \\ &= p_2 = 120 \text{ kPa} = 120 \times 10^3 \text{ N/m}^2 \end{aligned}$$

$$\text{Datum} = z = ?$$

$$Q = \frac{40}{1000} \text{ m}^3/\text{sec}$$

$$d_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$d_2 = 200 \text{ mm} = 0.2 \text{ m}$$

Required

z

$$z = ?$$

Sol

$$A_1 = \frac{\pi d_1^2}{4}$$

$$A_1 = \frac{3.14 \times (0.3)^2}{4}$$

⇒

$$A_1 = 0.0706 \text{ m}^2$$

$$A_2 = \frac{\pi d_2^2}{4}$$

$$A_2 = \frac{3.14 \times (0.2)^2}{4}$$

⇒

$$A_2 = 0.0314 \text{ m}^2$$

As

we know that

$$Q_1 = v_1 A_1$$

$$v_1 = \frac{Q_1}{A_1}$$

$$Q_1 = \frac{40}{1000}$$

$$v_1 = \frac{0.04}{0.0706}$$

$$= 0.566 \text{ m/s}$$

$$v_2 = \frac{Q}{A_2}$$

$$v_2 = \frac{0.04}{0.03144}$$

$$v_2 = 1.27$$

Now

$$\frac{P_1}{\gamma} + \frac{v_1^2}{2g} + z_1 = \frac{P_2}{\gamma} + \frac{v_2^2}{2g} + z_2$$

$$z_1 = 0$$

$$\gamma = 9810$$

$$\frac{300 \times 10^3}{9810} + \frac{0.566}{2(9.81)} + 0 = \frac{120 \times 10^3}{9810} + \frac{1.27}{2(9.81)} + z_2$$

$$30.60 + 0 = 12.314 + z_2$$

$$z_2 = +18.286 \text{ m}$$

Q No 3

10

Sol

Given data

length of Pipe = $l = 500\text{ m}$

dia = $d = 0.2\text{ m}$

Specific gravity of oil = 0.9

Flow rate = $Q = 0.06\text{ m}^3/\text{s}$

viscosity = $\mu = 6 \times 10^{-5}\text{ N}\cdot\text{s}/\text{m}^2$

Required

pressure loss = $\Delta P = ?$

As we know

$$f \left(0.0032 + \left(\frac{0.221}{R^{0.837}} \right) \right)$$

where $R = \text{Reynold's No.}$ and is given as.

$$R = \frac{U \times d}{\nu} \rightarrow \text{① and } \Rightarrow$$

$$\text{and } \cancel{Z} \quad v = \frac{\mu}{\rho} = \frac{6 \times 10^{-5}}{2000}$$

$$v = 6.67 \times 10^{-8} \text{ m}^2/\text{s}$$

$$\text{and } v = \frac{Q}{A}$$

For circular pipe

$$A = \frac{\pi}{4} d^2$$

$$\Rightarrow v = \frac{0.06}{0.031} = \frac{\pi}{4} (0.02)^2$$

$$A = 0.031 \text{ m}^2$$

$$\Rightarrow \boxed{v = 1.95 \text{ m/s}}$$

Now eq (1)

$$R = \frac{1.95 \times 0.2}{6.67 \times 10^{-5}} = 5.73 \times 10^6$$

Now

$$f = 0.0032 + \frac{0.221}{(5.73 \times 10^6)} = 0.237$$

$$\Rightarrow f = 8.79 \times 10^{-3}$$

$$F = 0.00879$$

Now from Bernoulli's equation

$$\text{Head loss} = h_L = \frac{FLv^2}{2gD} \rightarrow \text{(ii)}$$

Putting values in eq. (ii)

$$h_2 = \frac{(0.00879)(0.005)(1.95)^2}{2(9.81)(0.2)}$$

$$h_2 = 4.259 \text{ m}$$

Now to find pressure loss due to friction.

Pressure Head formula is used

$$h_2 = \frac{\Delta P}{\rho g}$$

$$\Rightarrow \Delta P = h_2 \times \rho g$$

Put value

$$\Delta P = 4.259 \times 900 \times 9.81$$

$$\Rightarrow \Delta P = 37602.7 \text{ Pa}$$

$$\Rightarrow \Delta P = 37.602 \text{ kPa}$$