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Subject Structural Analysis I

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Batch 2013

Semester 4th

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Q1
No

Given data:

uniform load = 4 k/ft

$$E = 29 \times 10^3 \text{ ksi}$$

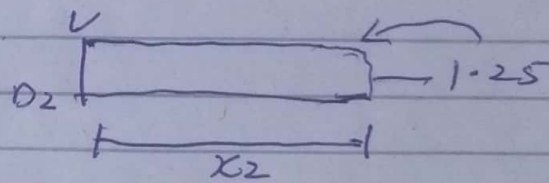
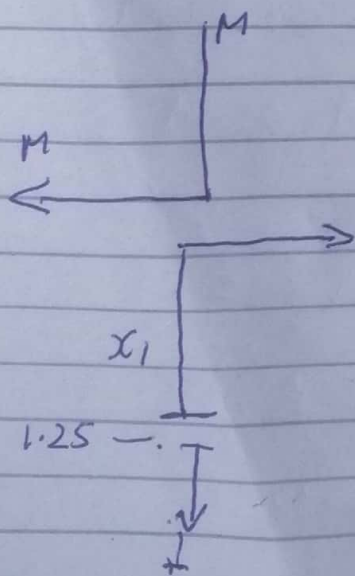
$$I = 600 \text{ in}^4$$

Req:

Vertical Displacement

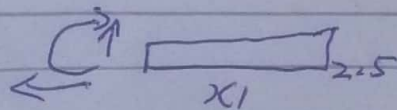
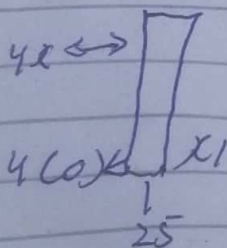
Sol:

Now Vertical Moment



$$M_2 = 1.25x$$

real Moment



$$M_2 = 25 - x_2$$

(3)

$$M^y = \frac{40x_1 - \frac{1}{2}x_1(x_2)}{40x_1 - 2x_1^2}$$

Now by virtual work equation

$$\Delta OC = \int_0^L \frac{mM dx}{E}$$

$$\Delta L = \int_0^{10} (1x) \left[\frac{40x_2 - 2x^2}{E} \right] dx + \int_0^8$$

$$\frac{0.25 \sqrt{2} (25x_2)}{EI} dx$$

$$D = \frac{1}{EI} \left[\frac{42x^3}{3} - \frac{2x^3}{4} \right]_0^{10} + \left[\frac{31.25x^2}{2} \right]_0^8$$

$$\frac{1}{EI} \left[\frac{4x^2}{3} - \frac{2x^3}{4} \right]_0^{10} + \left[31.25x^2 \right]_0^8$$

$$\frac{1}{EI} \left[\left[\frac{4x^2}{3} \right]_0^{10} - \left[\frac{2x^3}{4} \right]_0^{10} \right]$$

$$\frac{1}{EI} \left[\int_0^{10} \frac{4x^2}{3} - \int_0^{10} \frac{2x^3}{4} \right]$$

$$\frac{1}{EI} \left[\frac{4}{3} (10)^3 - (0)^3 - \frac{2}{4} \int_0^{10} (10)^3 \right]$$

$$\frac{1}{EI} [1333.34 - 500]$$

$$= \frac{833.34}{EI}$$

(4)

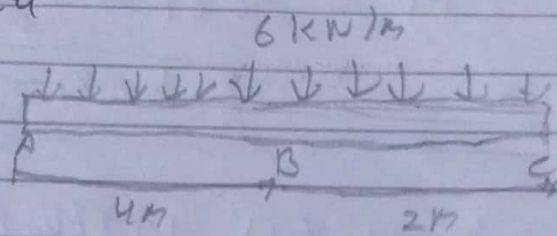
Q. 4

No

Sol: Given data

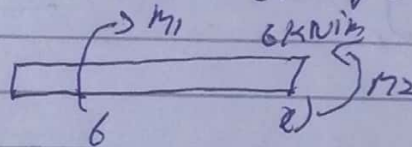
$$E = 200 \text{ GPa}$$

$$I = 60 \times 10^6 \text{ mm}^4$$



Req: \therefore

Slope and displacement:



$$M' - M_2 = \frac{1}{2} (x_2) (6 + x_1)$$

$$M' = M - \frac{6x_2 + x_1^2}{2}$$

$$M = -M' - 3x^2 + \frac{x_2^2}{2}$$

taking partial derivative with respect to M

$$\frac{\partial M_2}{\partial P} = -x$$

$$\Delta B = \int_0^2 \frac{M(2M)}{2P} \frac{du}{E}$$

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$$= \int_0^b \frac{-3x^2(-x) dx}{EI} + \int_0^4 \frac{-3x^2(-x) dx}{EI}$$

$$\Delta B = \frac{-3x^3}{4EI} \Big|_0^b + \frac{-3x^4}{4EI} \Big|_0^4$$

Put the value of EI and I

$$= \frac{-3x^3}{2(200 \times 60 \times 10^6)} \Big|_0^6 + \frac{-3x^4}{4000(60 \times 10^6)} \Big|_0^4$$

$$= \frac{-216 \text{ KN ft}^3}{4.8 \text{ N} \times 10^6} + \frac{-614.4 \text{ KN ft}^3}{4.8 \text{ N} \times 10^6}$$

$$= -4.5 \times 10^{-9} + (-1.28 \times 10^{-8})$$

$$\boxed{\Delta B = 5.76 \times 10^{-10} \text{ inch}} \quad \text{Displacement}$$

Slope:

$$M + \frac{1}{2} x (6x_1) = 0$$

$$M = -\frac{1}{2} x (6x_2) = 3x^2$$

$$\text{So, } \frac{2M_1}{2M_1} = 0$$

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$$M_1 - M_2 = \frac{1}{2} (x_2)(6 + x_2)$$

$$M = -M' + 6x_2 + x_2^2$$

$$M = -M' + 3x^2 + \frac{x^2}{2}$$

$$\frac{2M_2}{2M_1} = -1$$

$$= \int_0^8 \frac{-3x^2(4x)}{EI} + \int_0^{10} (-2 + 6x^2 + \frac{x^2}{2}) dx$$

$$= 0 + \left(\frac{-x + 6x^3}{3} + \frac{x^3}{6} \right) \Big|_0^{10} \left(\frac{1}{EI} \right)$$

$$= \frac{1}{200 \times (60 \times 10^6)} \left(-x + \frac{6x^3}{3} + \frac{x^3}{6} \right) \Big|_0^{10}$$

$$\Rightarrow \boxed{\theta = 4.125 \times 10^{-7} \text{ inch}}$$

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Q3

Given data :-

$$W = \text{uniform load} = 400 \text{ lb/ft}$$

$$h = 10 \text{ ft}$$

$$L = 15 \text{ ft}$$

Required :-

equation of curve and

force in cable = ?

Solution :-

We know that

$$y = \frac{h}{L^2} x^2$$

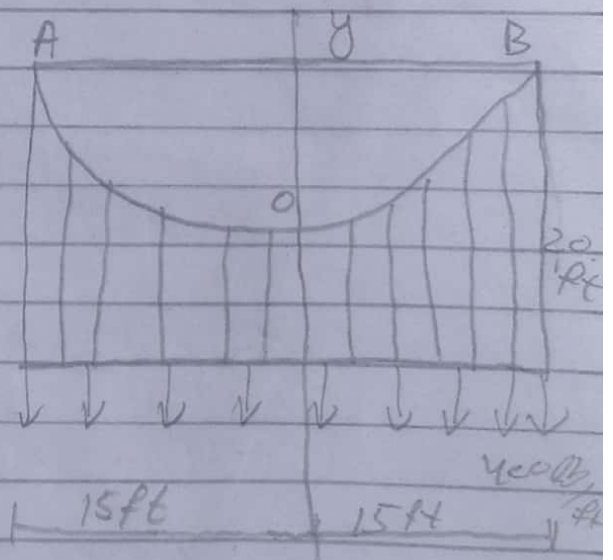
Putting the values

$$y = \frac{10}{(15)^2} x^2 = 0.044 x^2$$

$$T_0 = FH = \frac{w_0 L^2}{2h}$$

$$= \frac{400 \times (15)^2}{2 \times 10}$$

$$T_0 = 4500 \text{ lb} = 4.5 \text{ K}$$



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$$T_B = T_{Max} = \sqrt{(FH)^2 + (LbL)^2}$$
$$= \sqrt{(4500)^2 + (400 \times 15)^2}$$

$$T_{Max} = 7500 \text{ lb} = 7.5 \text{ k}$$

NOW T_{Max} Ry and other equation

$$T_B = T_{Max} = wL \sqrt{1 + \left(\frac{L}{2h}\right)^2}$$
$$= 400 \times 15 \sqrt{1 + \left(\frac{15}{2 \times 10}\right)^2}$$

~~8.9.1~~ $T_{Max} = 7500 \text{ lb} = 7.5 \text{ k}$

Q. No 4

Given data

uniform load = 30 kN/m

Req. :-

Internal Moment at D = ?

Solution :-

Dividing into two members.

AB and BC

AB

$$\sum \text{EMA} = 0 \quad B_x(5) + B_y(8) - 240(4) = 0 \quad \text{--- (a)}$$

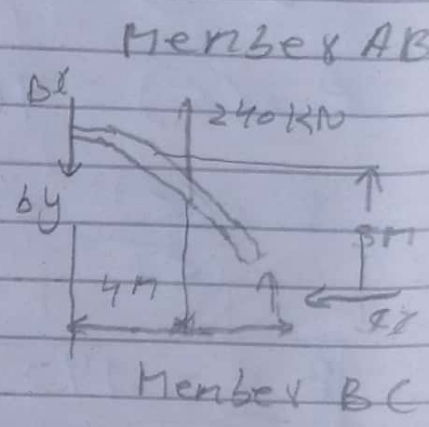
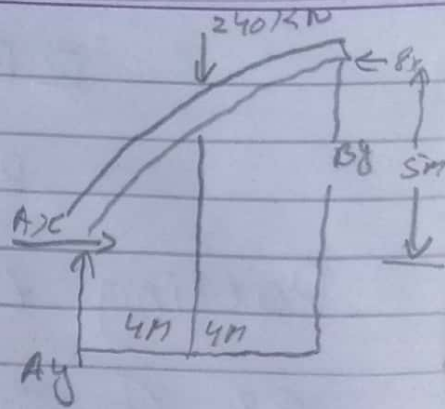
BC

$$\sum \text{EM}_B = 0 \quad -B_x(5) + B_y(8) + 240(4) = 0 \quad \text{--- (b)}$$

Adding eq (a) and (b)

$$\begin{aligned} & B_x(5) + B_y(8) - 240(4) = 0 \\ - & B_x(5) + B_y(8) + 240(4) = 0 \end{aligned}$$

$$0 + 2 B_y(8) + 0 = 0$$



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$$\sum B_y (8) = 0$$

$$\Rightarrow B_y = 0 \text{ kN}$$

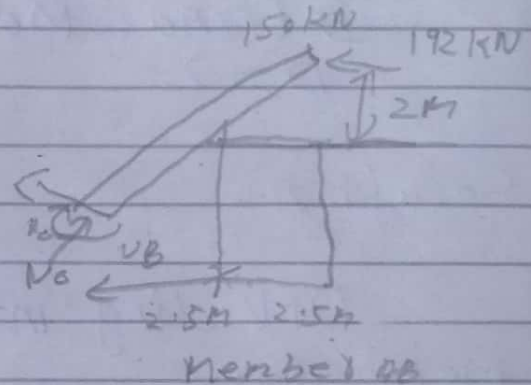
Putting the value of B_y in

$$\text{eq (b)} \Rightarrow -B_x (5) + 0(8) + 960 = 0$$

$$B_x (5) = 960$$

$$\frac{B_x (5)}{(5)} = \frac{960}{5}$$

$$\boxed{B_x = 192 \text{ kN}}$$



Now at segment DB

$$\sum \text{EMD} = 0$$

$$192(2) - 150(2.5) - \text{MD} = 0$$

$$384 - 375 - \text{MD} = 0$$

$$9 - \text{MD} = 0$$

$$\Rightarrow \text{MD} = 9 \text{ kN}\cdot\text{m}$$