

Name:

M. Zeshan Shahid

ID#

7876

Section:

"A"

Semester:

"6th"

Subject:

PRCD-I

Mid Exams

Q No 1

Data :

$$\begin{aligned} \text{Dead load} &= 1.05 \text{ kips/ft} \\ \text{live load} &= 2.47 \text{ kips/ft} \\ \text{span} &= 18' \end{aligned}$$

$$f'_c = 4000 \text{ psi}$$

$$f'_y = 60,000 \text{ psi}$$

$$f_c = 4 \text{ ksi}$$

$$f_y = 60 \text{ ksi}$$

$$\text{Width} = 10''$$

$$\text{Height} = 20''$$

Solve :

step - 1

$$\Rightarrow \text{Effective depth} = h - 3$$

$$d = 20 - 3$$

$$d = 17''$$

$$\Rightarrow \text{Effective Cover} \\ d' = 2.5''$$

∴ Kilo = 1000

→ Reinforcement Ratio ^{Step-2}

$$\rho_{max} = 0.85(\beta)(f'_c/f_y)\left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y}\right)$$

$$\rho_{max} = 0.85(0.85)(4/60)\left(\frac{0.003}{0.003 + 0.005}\right)$$

$$\rho_{max} = 0.7225(4/60)\left(\frac{0.003}{0.008}\right)$$

$$\rho_{max} = 0.018$$

→ Step-2

Area of steel required

Formula
as we know that

$$\rho_{max} = \frac{A_{st}}{b \times d}$$

Cross multiplication

$$A_{st} = \rho_{max}(b \times d)$$

$$A_{st} = 0.018(10 \times 17)$$

$$A_{st} = 3.06 \text{ in}^2$$

Step-3

As by the Design Moment

$$M_u = \phi \times A_{st} (f_y) (d - a/2)$$

$$a = \frac{A_{st} \times f_y}{0.85(f'_c)(b)}$$

$$= \frac{3.06 \times 60}{0.85 \times 4 \times 10} = 5.4''$$

$$a = 5.4''$$

$$M_{u2} = 0.90 (3.06)(60) (17 - 5.4/2)$$

$$M_{u2} = 2362.9 \text{ kip-inch}$$

Moment due to given Load

$$\text{Beam weight} = \frac{10}{12} \left(\frac{20}{12} \right) (150)$$

$$= 208.33 \text{ lb/ft}$$

Total Factor Load

$$\text{Total factor load} = 1.2 (1050 + 208.33) + (1.6 (2470))$$

$$= 5461.9$$

$$\text{Total factor load} = 5.462$$

$$\text{Ultimate Factor Moment} = \frac{wL^2}{8}$$

$$M_u = \frac{5.46 (18)^2}{8}$$

$$M_u = 221.13 (12)$$

$$M_u = 2653.56$$

So

Page-4

M. Zeshan Shahid
ID# 7876

As,

$$M_u < M_u$$

$$2362.92 < 2653.56$$

Step-4

$$M_u = 2653.56 - 2362.92$$

$$M_u = 290.64 \text{ kip-inch}$$

Step-5

as per formula Steel Area in compression zone

$$M_u = \phi (A_{st}') (\gamma_y) (d - d')$$

$$A_{st}' = \frac{M_u}{\phi (\gamma_y) (d - d')}$$

$$= \frac{290.64}{0.90 (60) (17 - 2.5)}$$

$$A_{st}' = 0.37 \text{ in}^2$$

Step-6

$$A_{st} = A_{st} + A_{st}'$$

$$= 3.06 + 0.37$$

$$A_{st} = 3.43 \text{ in}^2$$

Step-7

We Use #8 bars

$$\text{Area} = 0.785 \text{ in}^2$$

$$\begin{aligned} \text{No of bars} &= \frac{A_{st}}{\text{Area of 1 bar}} \\ &= \frac{3.43}{0.785} \\ &= 4.36 \approx 5 \text{ bars} \end{aligned}$$

So 5 #8 bars

Compression steel:

Use #6 bar

$$\text{dia } (6/8) = 0.75''$$

$$\begin{aligned} \text{No of bars} &= \frac{A_{st}}{\text{Area of bar}} && \text{Area } 0.44 \text{ in}^2 \\ &= \frac{0.37}{0.44} = \\ &= 0.84 \approx 1 \text{ bar} \end{aligned}$$

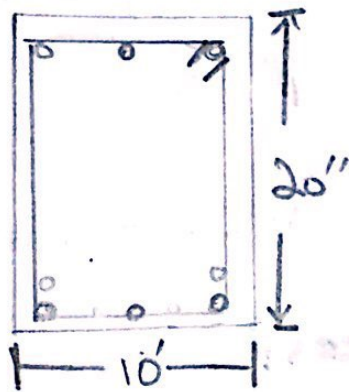
1 #6 bar in Compression zone

R.T.O

Step - 8**Minimum Width**

$$b_{min} = 2(1.5) + 2(3/8) + 5(8/8) + 4(8/8)$$

$$= 12.75" > 10"$$



⇒ Effective depth

$$d = 20 - 1.5 - 3/8 - 8/8 - 1/2(8/8)$$

$$d = 16.62"$$

Effective cover

$$d' = 1.5 + 3/8 + 1/2(6/8)$$

$$= 2.25"$$

Step - 9

Design Moment is given

$$M_d = \phi \times [A_{st}' \times \gamma \times (d - d') + (A_{st} - A_{st}') (\gamma) (d - \frac{\gamma}{2})]$$

$$a = \frac{(A_{st} - A_{st}') \times \gamma}{0.85 \times \gamma_c \times b}$$

Page - 7

M. Zeshan Shahid
ID#7876

$$= \frac{5(0.785) - 1 \times 0.44(60)}{0.85(4)(10)}$$

$$a = 6.15''$$

$$M_d = 0.90 \left[(1 \times 0.44)(60)(16.62 - 2.25) + \left[5 \times 0.785 - 1(0.44)(60) \times 16.62 - \frac{6.15}{2} \right] \right]$$
$$= 0.9 \left[379.368 + 3.925 - 357.588 \right]$$

$$\text{As } M_d = 2890.46$$

$$M/d = 2890.46 > 2653.56$$

So design is okay!

Q: 2 (a)

Ans (a)

Bond stress:

Bond stress is stress at the surface of reinforcing bar which prevent movement in between bar and surrounding concrete

OR

The force of adhesion per unit area of contact between concrete two bonded surface area such as concrete and steel reinforcing bar is called Bond stress.

Development Length:

The minimum length of steel rod that is inserted inside concrete column to ensure sufficient adhesion force between concrete and steel

OR

Development length creates a surface safe bond between bar surface and concrete. It also ensures during ultimate load condition the reinforcement bar should not slip through the concrete. It transfers stress from beam to column.

Q: 2 (b)

Ans: 2 (b)

Doubly reinforced beam

It has less depth and width as compared to single reinforced beam and resists more load and moment.

It is used in heavy structure for heavy load.

⇒ Doubly reinforced beams are provided in order to increase the moment carrying capacity of the section.

⇒ To ensure safety against reversal of stresses in the structure due to wind force, seismic force and temperature stresses.

⇒ Minimum compression reinforcement is provided to hold the shear reinforcement strips in position and for increasing the ductility of beam.

Q: 2 (c)

Ans: (c)

Difference

T-Beam	Rectangular Beam
<p>1 The beam whose cross section area in T-shape is called T Beam. It is connected or spliced the slab with center of the slab.</p>	<p>1 A rectangular beam is one which is used a compressive in top fibre and tension in bottom fibre of that beam. It is in Rectangular shape.</p>
<p>2: A T beam is more economical than rectangular beam.</p>	<p>2 A rectangular beam is cheaper expensive than T beam.</p>
<p>3: The resistance of T-beam is higher for positive moment because the flange section would be in compression but the negative moment it yield since strength an equivalent beam.</p>	<p>3: The rectangular section only depends on the location of reinforcement to yield the flexural capacity.</p>

Q No: 2 (d)

Ans: 2 (d)

Strength reduction Factor:

The ratio of elastic strength to

yield strength is called strength reduction

Factor

It is used to reduce the calculated strength of structure member to account

uncertainties arises from material used,

inaccurate of design calculated and

increases the pricing of steel and

any other factor

It is denoted by ϕ

Effect on Flexural strength

When designing a section to resist

the moment which is caused by load.

then the strength reduction factor shows the

strength in terms of percentage.

It represent the uncertainty in per determining

the member's behavior to the types of stresses

which is subjected.

For Example:- The design process of beam

we commonly take $\phi = 0.85$ for the ~~factor~~ torsion

It show that 85% of the strength is consider here
and the rest of 15% for accidental purposes.

QNO: 2 (e) Designing Method

There are three methods of structural design i.e working stress, limit state and ultimate load method of structural design.

These design methods are used reinforced concrete as well as steel structure design.

2) Ultimate strength Design Method

In the strength design method the increased load and reduced strength of the material considered but the both based scientific relationate.

eg it is quit possible then during the life span of structure dead and live loads is creage.

Stress Design Method (ASD)

In working stress or Allowable stress

design method the material strength is knowingly

taken less than actual e.g. half of the

actual to provide a factor of safety

equal to 2.0.

Best for use:

Ultimate strength design method is best

for use in designing different structural members because

⇒ It is economically good, its result is more economical.

⇒ Easy to use and understanding

⇒ Also easy to change the load and strength.

Q No: 3

Ans: 3

Given Data

$$\text{web width} = 14''$$

$$\text{slab thickness} = 6''$$

$$\text{Total depth} = 28''$$

$$\text{Effective depth} = 28'' - 3''$$

$$= 25''$$

$$\text{C/C distance} = 10'$$

$$\text{Span} = 32'$$

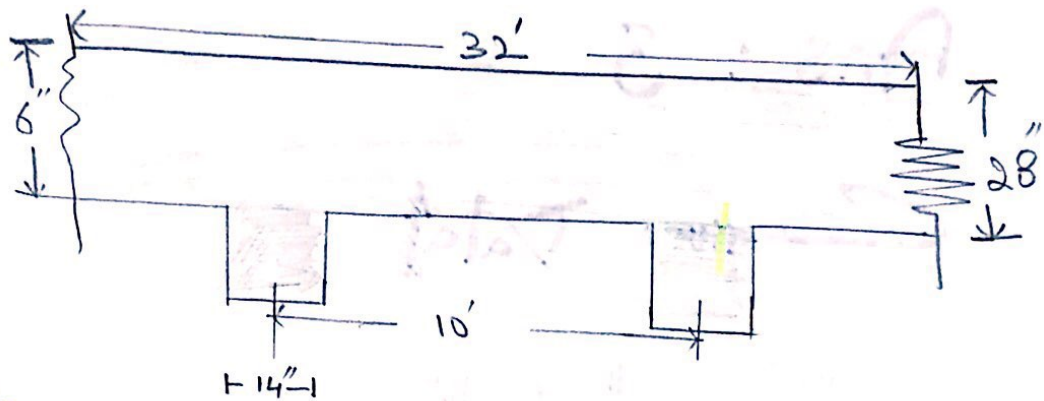
$$\text{D.L} = 50 \text{ lb/ft}^2$$

$$\text{S.S} = 225 \text{ lb/ft}^2$$

$$f_y = 60,000 \text{ psi}$$

$$f'_c = 4000 \text{ ksi}$$

Solve:



Step - 1

We know

$$M_u = \frac{W_u \times L^2}{8}$$

⇒ Beam self weight per feet

$$wt = b(t) \gamma_c$$
$$= 14/12 (28/12) (150)$$

$$wt = 408.3 \text{ Lb/ft}$$

Total Force Load:

$$= 1.2(50 + 408.3) + 1.6(225)$$
$$= 549.996 + 360$$
$$= 909.99$$
$$= 0.909 \text{ KSI}$$

1000 = kilo

⇒ **Moment:**

As we know that

$$m = \frac{Wl^2}{8}$$

$$= \frac{0.909(32)^2 \times 12}{8}$$

$$= 1396.23$$

⇒ **Effective Breadth:**

$$\textcircled{1} \quad 16(h_f) + bw = 16(6) + 4 \\ = 110''$$

$$\textcircled{2} \quad \text{Span} \Rightarrow \frac{\text{span}}{4} \\ = \frac{32}{4} \times 12 \\ = 96''$$

$$\textcircled{3} \quad \text{C/C distance} = 12(10) \\ = 120''$$

So now $b_e = 96$

Step - 3

M. Zeshan Shahid
ID# 7876

Page - 19

Rectangular or T-Beam

Trail - 1 so let we get $a = hf = 6''$

So Now as formulated

$$A_{st} = \frac{M_u}{\phi \times f_y (d - a/2)}$$

$$= \frac{1396.23}{0.90 \times 60 (25 - 6/2)}$$

$$= \frac{1396.23}{1188}$$

$$A_{st} = 1.175 \text{ in}^2$$

Now T-2

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b}$$

$$= \frac{1.17 (60)}{0.85 \times f'_c \times b} = \frac{1.17 \times 60}{0.85 \times 4 \times 96}$$

$$= 0.2'' < 6''$$

So T-beam design

P.T.O

$$A_{st} = \frac{1396.23}{0.90 \times 60 (25 - 0.2/2)}$$

$$= \frac{1396.23}{1344.6}$$

$$= 1.03 \text{ in}^2$$

~~Trial 3~~

$$a = \frac{1.03 (60)}{0.85 (4) (96)}$$

$$= 0.18$$

$$A_{st} = \frac{1396.23}{0.90 (60) (25 - 0.18/2)}$$

$$= \frac{1396.23}{1345.14}$$

$$A_{st} = 1.03 \text{ in}^2$$

Step - 4

Now P_{max} and S_{min}

$$P_{(max)} = 0.85 \times 0.85 (4/60) \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$P_{(max)} = 0.85 (0.85) (4/60) (0.375)$$

$$P_{(max)} = 0.018$$

Now

Page - 21

M. Zeshan Shahid
ID 7876

$$\Rightarrow P_{min} = \frac{200}{W}$$
$$= \frac{200}{60,000}$$

$$P_{min} = 0.003$$

$$\Rightarrow \rho = \frac{A_{st}}{b \times d}$$
$$= \frac{1.03}{14 \times 25}$$

$$\rho = 0.0029$$

So that

$$P_{min} < \rho < P_{max}$$
$$0.003 < 0.002 < 0.018$$

As we already know that

ρ is less than P_{min}

So

$$\rho = \frac{A_{st}}{b \times d}$$

$$\Rightarrow A_{st} = P_{min} \times b \times d$$

$$= 0.003 \times 14 \times 25$$

$$A_{st} = 1.05 \text{ in}^2$$

Step-5

No. & Selection of Bar

Let we use #8 bar then

$$\text{dia} = (8/8) = 1''$$

$$\text{Area} = 0.785 \text{ in}^2$$

now

$$\text{No of bars} = \frac{1.05}{0.785}$$

$$= 1.3 \rightarrow 2$$

want to get 2 #8 bars

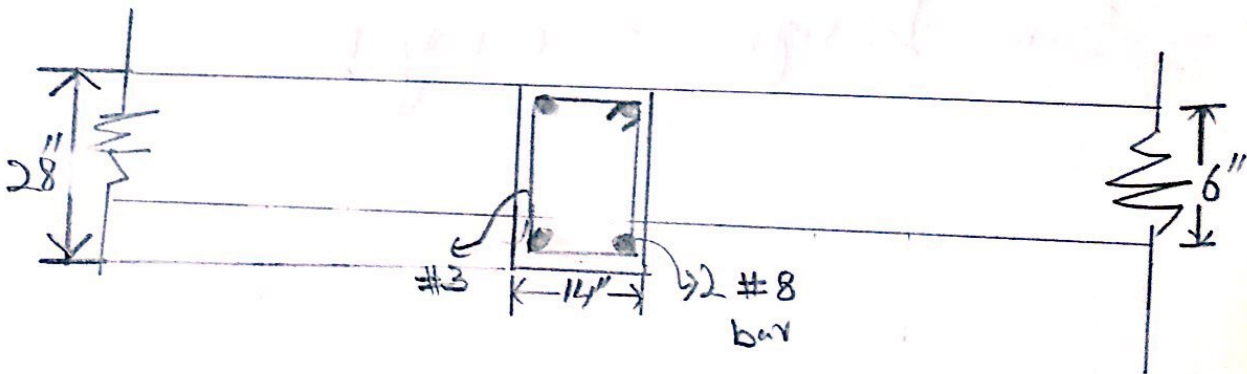
step-6

Minimum Width

$$b_{\text{min}} = 2(1.5) + 2(3/8) + 2(8/8) + 1(8/8)$$

$$= 6.75 < 14''$$

It's good in one layer



Step - 7

Design Moment

$$M_d = \phi \times \gamma_y \times A_{st} (d - a/2)$$

$$\text{Area of steel} = \text{Area of 1 bar} \times \text{No of bars}$$

$$= 0.785 \times 2$$

$$= 1.57 \text{ in}^2$$

Now

$$d = \frac{1.57 \times 60}{0.85 \times 4 \times 96}$$

$$= 0.2''$$

So

$$M_d = 0.90 \times 60 \times 1.57 \times (25 - 0.2/2)$$

$$M_d = 2111.02 \text{ kip-inch}$$

$$\text{As } 2111.02 > 1396.23$$

So Design is Okay!