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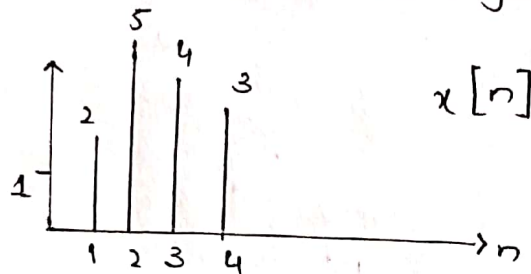
Subject Signal and System

Semester 10th

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Date 04/06/2020

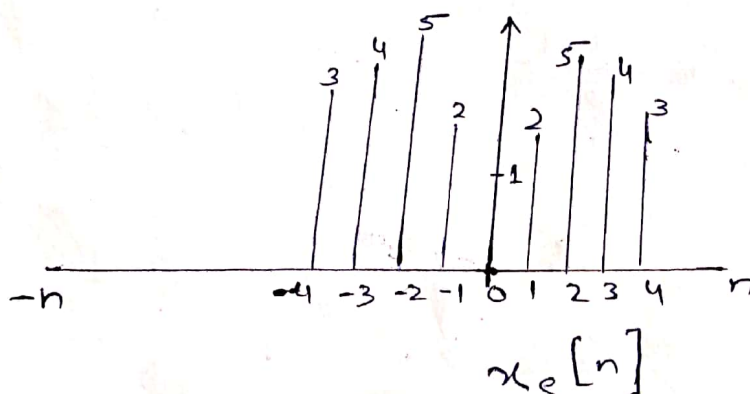
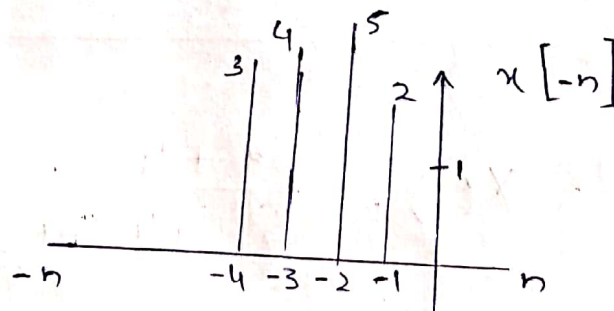
Q: 1 Evaluate the even and odd components for the given function.



Solution:- As we know that even components of a function can be written

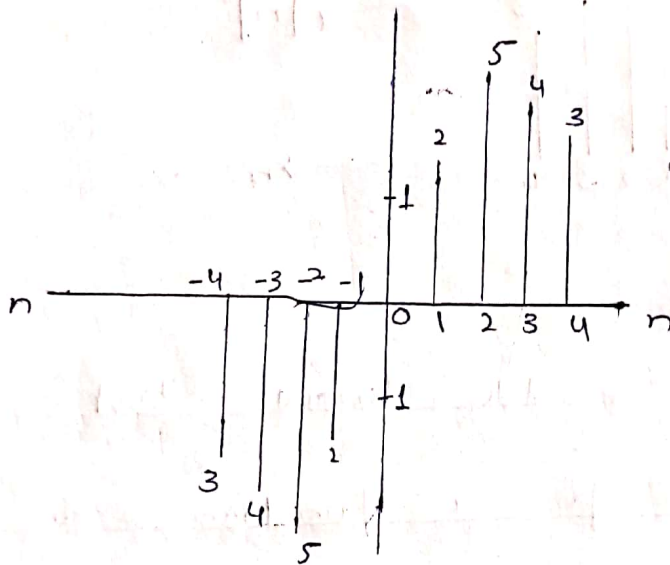
$$x_e[n] = \frac{x[n] + x[-n]}{2}$$

Reflect $x[n]$ to get $x[-n]$



odd components can be written as

$$x_o[n] = \frac{x[n] - x[-n]}{2}$$



Q:2 Calculate the inverse Laplace transform
of the given equation:

$$Y(s) = \frac{5s + 4}{s^2 + 4s - 12}$$

Solution: $\frac{S+4}{S^2+4S-12}$

$$\frac{S+4}{S^2+4S-12}$$

$$\frac{S+4}{S^2+6S-2S-12}$$

$$\frac{S+4}{S(S+6)-2(S+6)}$$

$$\frac{S+4}{(S-2)(S+6)}$$

$$\frac{S+4}{(S-2)(S+6)} = \frac{A}{S-2} + \frac{B}{S+6}$$

Multiply both side by $(s-2)(s+6)$

or taking L.S.M B.Sides

$$Y(s) = S+4 = A(s+6) + B(s-2) \rightarrow \textcircled{1}$$

Let $s = -6$ in eq ①

$$(-6+4) = A(-6+6) + B(-6-2)$$

$$-2 = A(0) + B(-8)$$

$$-2 = B(-8) \Rightarrow B = \frac{-2}{-8} = \frac{1}{4}$$

$$\boxed{B = \frac{1}{4}}$$

Now,

$s = 2$ in eq ①

$$s+4 = A(s+6) + B(s-2)$$

$$2+4 = A(2+6) + B(2-2)$$

$$6 = A(8) + B(0)$$

$$6 = A(8)$$

$$A = \frac{6}{8} \Rightarrow \frac{3}{4} = \frac{1}{2}$$

$$\begin{aligned} Y(s) &= \frac{1}{2} \frac{1}{s-2} + \frac{4}{s+6} \\ &= \frac{1}{2} L^{-1} \left(\frac{1}{s-2} \right) + 4 L^{-1} \left(\frac{1}{s+6} \right) \\ &= \frac{1}{2} e^{2t} + 4 e^{-6t} \end{aligned}$$

Q

3(A)

Discuss procedure of converting an analog signal into a digital one.

Ans

An analog-to-digital converter, or ADC as it is more commonly called, is a device that converts analog signal into digital. Analog information is transmitted by modulating a continuous transmission signal by amplifying a signal's strength or varying its frequency to add or take away data. Digital information describes any system based on discontinuous data or events. Computers which handle data in digital form, require analog to digital converter to turn signals from analog to digital before it can be read. One example is Modem which turn signals from digital to analog.

before transmitting those signals over communication lines such as telephone lines that carry only analog signals. The signals are turned back into digital form (demodulated) at the receiving end so that computer can process data in its digital format.

Q.3b

Suppose an analog signal has a highest frequency of 60 Hz. Outline the steps that will ensure that no aliasing occurs.

Ans

$$f = 60 \text{ Hz}$$

ensure that there is no aliasing occur.

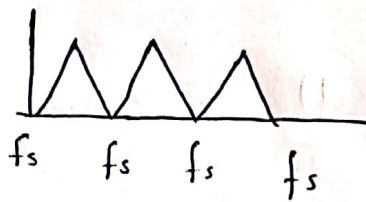
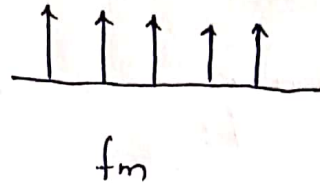
$$f = 60 \text{ Hz}$$

From Nyquist Criteria

$$f_s \geq 2 f_m$$

$$f_s \geq 2 \times 60$$

$$f_s = 120$$



if $f_s = 120 \text{ Hz}$ there will be no aliasing occurs as Nyquist criteria
 Prove that.

Q.4 Show that :-

$$x[n] * [h_1[n] * h_2[n]] = [x[n] * h_1[n]] * h_2[n]$$

Ans

$$x[n] * [h_1[n] * h_2[n]] = [x[n] * h_1[n]] * h_2[n]$$

Consider

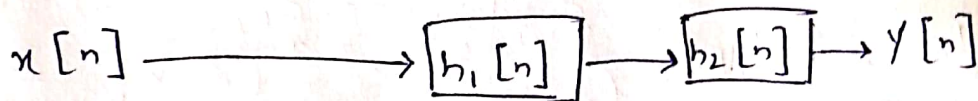
$$y[n] = [x[n] * h_1[n]] * h_2[n]$$

$$x[n] * h[n] = w_1[n]$$

Now

$$y[n] = [h[n] * h_1[n]] * h_2[n]$$

$$y[n] = w_1[n] * h_2[n]$$

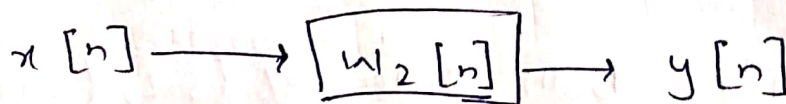


Now consider that

$$w_2[n] = h_1[n] * h_2[n]$$

$$y[n] = x[n] * [h_1[n] * h_2[n]]$$

$$y[n] = x[n] * w_2[n]$$



Both the block diagrams give us the same response we can write as:

$$x[n] * [h_1[n] * h_2[n]] = [x[n] * h_1[n]] * h_2[n]$$