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Section # 13

Subject # Structural Analysis.

Q#01

①

⇒ Finding reactions

$$\left( \begin{array}{l} + \\ \downarrow \end{array} \right) \sum M_A = 0$$

$$= -4(10)(5) + C_y(8) = 0$$

$$C_y = 25 \text{ kip}$$

$$\sum F_y = 0 \uparrow^+$$

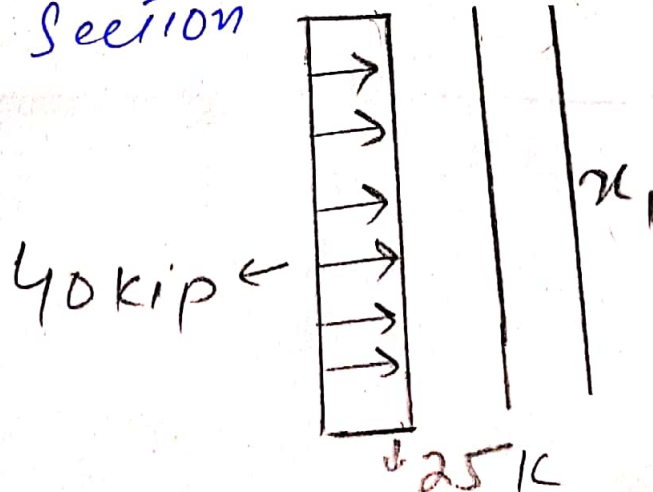
$$= 25 + A_y = 0$$

$$A_y = -25 \text{ kips}$$

$$\sum F_x = 0 \longrightarrow \textcircled{A}$$

$$= 40 - A_x = 0 \Rightarrow A_x = 40 \text{ k}$$

Taking section



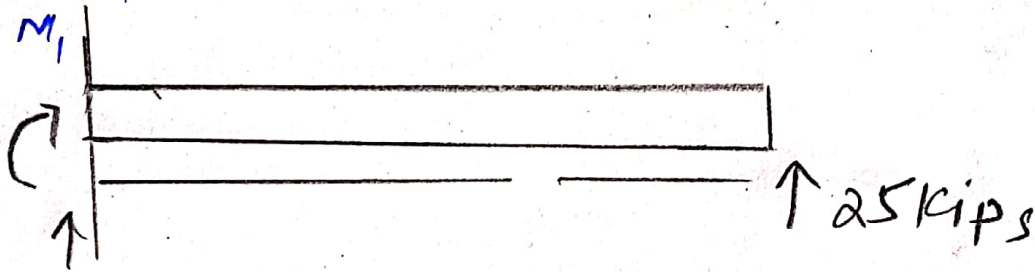
(2)

Real Moment

$$\sum M_1 = 0$$

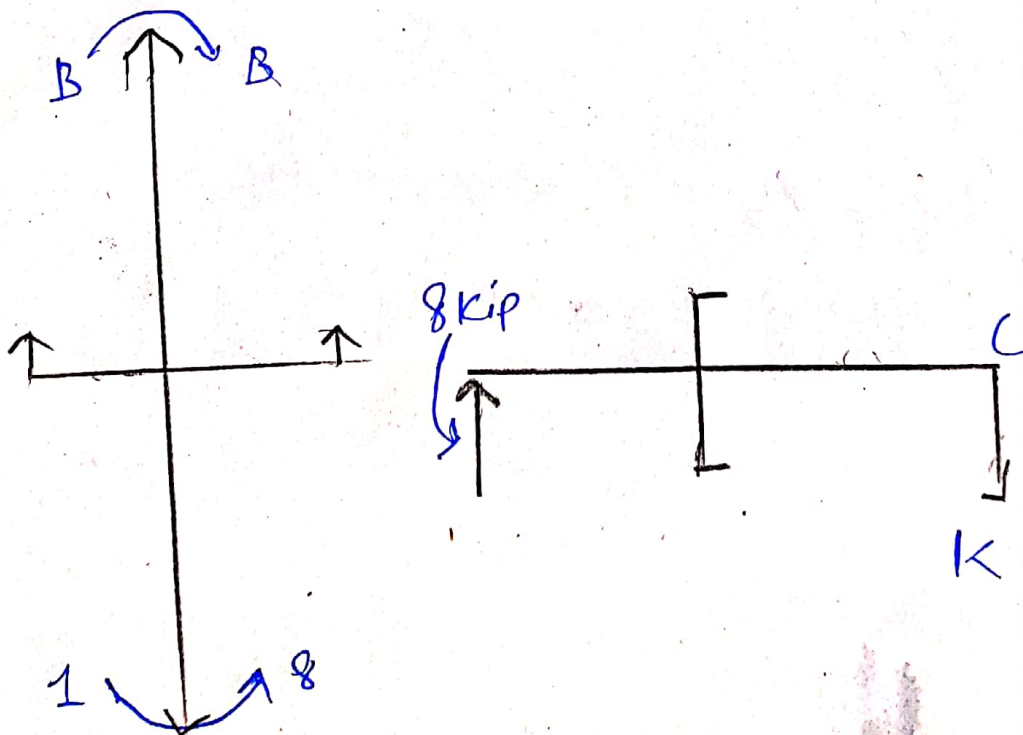
$$-40(x_1) + 4x_1\left(\frac{x_1}{2}\right) + C_{x_1} = 0$$

$$M_1 = 40x_1 - 2x_1^2$$



$$-25(x_2) + M_2 = 0$$

$$M_2 = 25x_2 \text{ Kips}$$



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Member	BA	CB
Origin	B	C
Limit	0-10	0-8
M	$2x^2$	0
M	8	$x$

By Virtual Work Method

$$1 \cdot \Delta I = \int_0^{10} \frac{2x^2(8) dx}{EI} + \int_0^8 \frac{(0)(x)}{EI}$$

$$11 = \frac{16x^3}{3} \Big|_0^{10} + 0$$

$$11 = \frac{16 \times 1000}{3} / EI$$

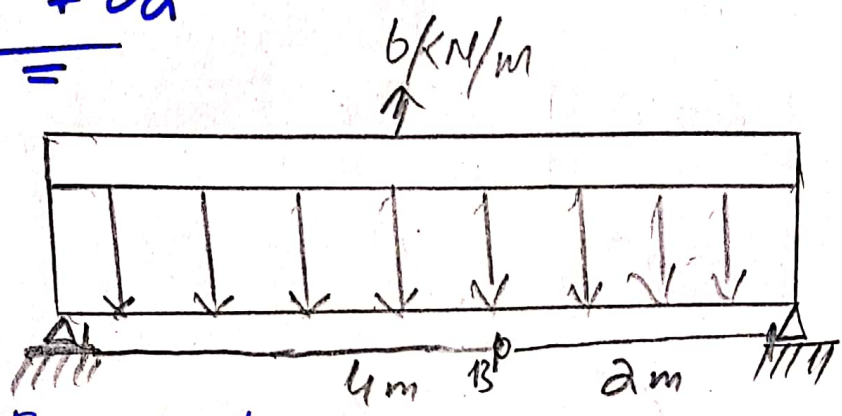
$$11 = \frac{63333.33}{EI} = \frac{53333.33}{29 \times 10^3 \times 600}$$



(4)

$$I \cdot \Delta I = 3.06 \times 10^{-4} \text{ In}$$

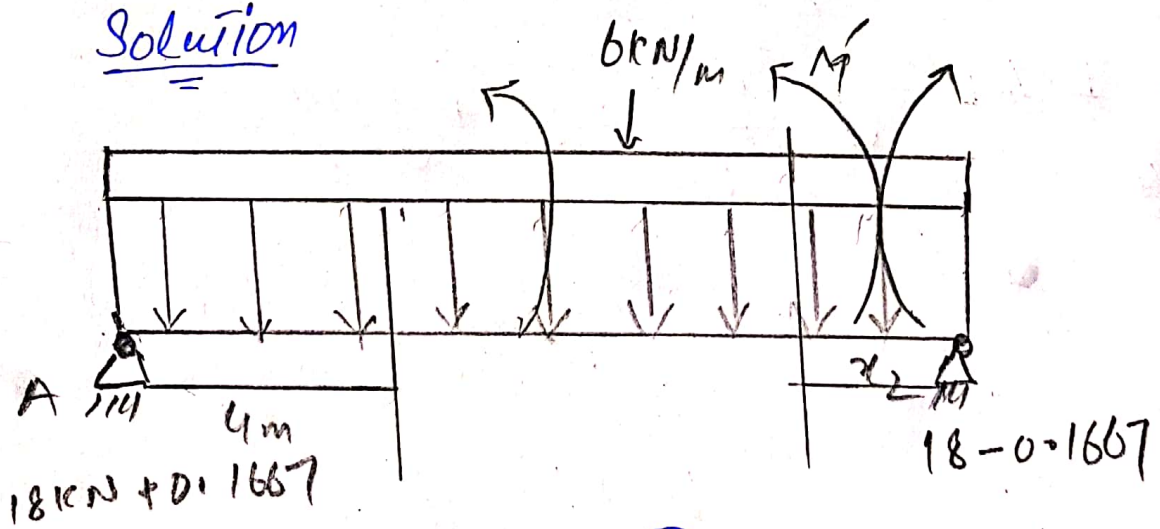
Q #02



Required

Slope and displacement at Point "B"

Solution



$$R_1 + R_2 = 0 \rightarrow \textcircled{1}$$

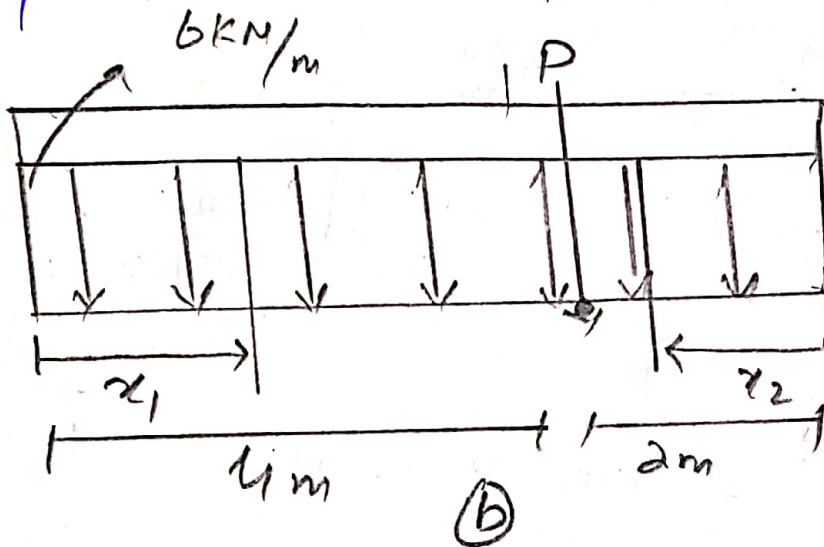
$$\sum M_A = 0 \quad (+)$$

$$\Rightarrow 1 + R_2(6) = 0$$

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$$R_1 + (-0.1667) = 0$$

$$R_1 = 0.16667 \text{ kN}$$



$$= R_1 + R_2 = 1$$

$$= \sum M_A = 0$$

$$= -(-1)(4) + R_2(6) = 0$$

$$R_1 = 0.6667 \text{ kN}$$

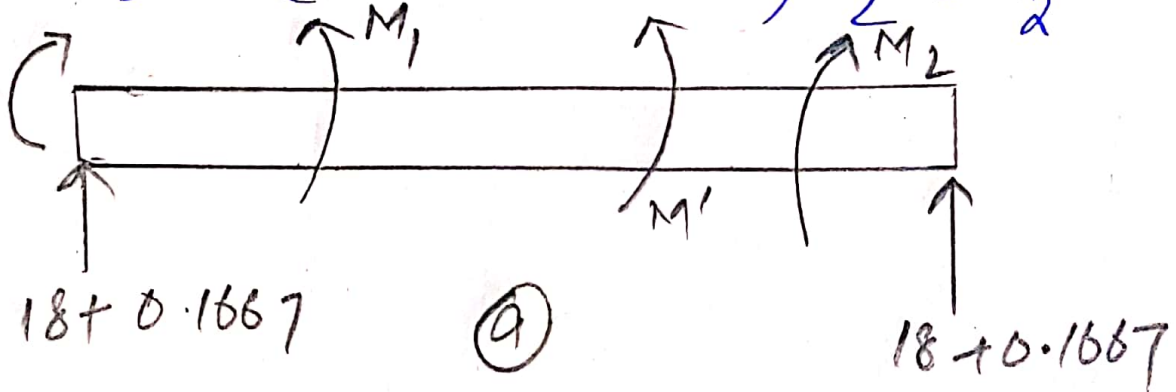
$$R_2 = 1 - 0.6667 \text{ kN}$$

$$R_2 = 0.333 \text{ kN}$$

(b)

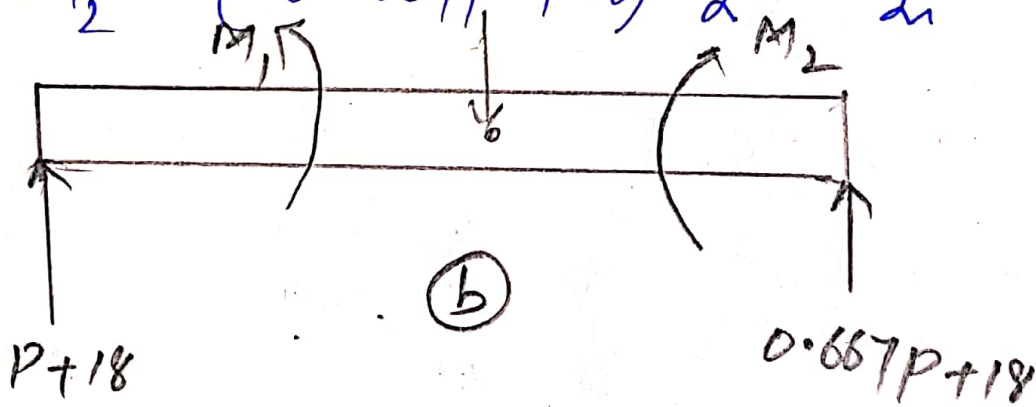
$$M_1 = (18 + 0.1667M')x_1 - 2x_1^2$$

$$M_2 = (18 - 0.1667M')x_2 - 2x_2^2$$



$$M_1 = (0.333P + 18)x_1 - 2x_1^2$$

$$M_2 = (0.667P + 18)x_2 - 2x_2^2$$



THE displacement functions shown in the figure "a" above

$$\frac{\partial M_1}{\partial M_2} = 0.1667x_1 \quad \& \quad \frac{\partial M_2}{\partial M'} = 0.1667x_2$$

set \$M' = 0\$ then

$$M_1 = (18 + 0.1667(0))x_1 - 2x_1^2$$

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$$M_1 = (18x_1 - 2x_1^2)$$

$$M_2 = (18x_2 - 2x_2^2)$$

$$Q_B = \int_0^2 M \left( \frac{\partial M}{\partial M_1} \right) \frac{dx}{EI} = \int_0^4 \frac{(18x_1 - 2x_1^2)(0.1667x_1) dx_1}{EI} \\ + \int_0^2 \frac{(18x_2 - 2x_2^2)(0.1667x_2) dx_2}{EI}$$

$$Q_B = \frac{42.65}{EI} + \frac{6.66}{EI}$$

$$Q_B = \frac{49.31}{EI}$$

$$Q_B = \frac{49.31}{(200 \times 10^6 \text{ Kpa})(0.0006)}$$

$$Q_B = 0.4411 \text{ radians}$$



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⇒ For the displacement functions are shown in figure "b"

$$\frac{\partial M_1}{\partial P} = 0.333x_1 \quad \text{and} \quad \frac{\partial M_2}{\partial P} = 0.6667x_2$$

also set  $P=0$  then  $M_1 = (18x_1 - 2x_1^2) \text{ KN}\cdot\text{m}$

Thus

$$\Delta_B = \int_0^L M \left( \frac{\partial M}{\partial P} \right) \frac{dx}{EI}$$

$$\Delta_B = \int_0^4 \frac{(30x_2 - 2x_2^2)(0.6667x_2) dx}{EI}$$

$$\Delta_B = \frac{218.5}{EI} \Rightarrow \frac{218.5}{(200 \times 10^6)(0.000006)}$$

$$\Delta_B = 0.018 \text{ m or } 18 \text{ mm}$$

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Q #03

Solution

⇒ we know that

$$y = \frac{w}{L^2} x^2 = \frac{10}{(15)^2}$$

$$y = \frac{10}{225} x^2$$

$$y = 0.444 x^2$$

⇒ we know that

$$T_0 = F_4 = \frac{w_0 L^2}{2h} = \frac{400(15)^2}{2(10)}$$

$$T_0 = 4500 \text{ lb dividing by 1000}$$

$$T_0 = 4.5 \text{ K}$$

⇒ As we know that

$$T_B = T_{\text{max}} = \sqrt{F_4^2 + (w_0 L)^2}$$

$$= \sqrt{(4500)^2 + (400)^2 + (15)^2}$$

(10)

$$\sqrt{20250000 + (400 \times 15)^2}$$

$$T_{\max} = 7500 \text{ lb}$$

∴ Dividing by 1000

$$T_B = T_{\max} = 7.5 \text{ k}$$

⇒ As we know that

$$T_B = T_{\max} = w_0 L \sqrt{1 + \left(\frac{L}{2h}\right)^2}$$

$$T_B = T_{\max} = 400(15) \sqrt{1 + \left(\frac{15}{20}\right)^2}$$

$$T_B = T_{\max} = 6000(1.25)$$

$$T_B = T_{\max} = 7500 \text{ lb}$$

Dividing by 1000

$$T_B = T_{\max} = 7.5 \text{ k Ans}$$



Q#4

Member AB;

$$\curvearrowright + \sum M_A = 0$$

$$\Rightarrow B_x(5) + B_y(8) - 240(4) = 0$$

Member BC:-

$$\curvearrowright + \sum M_C = 0$$

$$-B_x(5) + B_y(8) + 240(4) = 0$$

Solving

$$B_x = 192 \text{ kN}, \quad B_y = 0$$

Segment BD :-

$$\curvearrowright + \sum M_D = 0$$

$$= 192(2) - 150(2.5) - M_D = 0$$

$$M_D = 9 \text{ kN}\cdot\text{m} \text{ Ans}$$



