

Page (1)

NAME : Jatazaz Ahmad

ID : 15050

COURSE : Discrete Structure

PROGRAM : BS (SE)

SEMESTER : 4th

Q1

(a) Explain the Concept of Bi Conditional Statement :

Ans: if we remove the if than part of a true Conditional Statement combine the hypothesis and conclusion, & track in a phrase "if and only if" we can create bi conditional statement. A bi conditional is true if and only if both the conditionals are true.

Bi-conditional are represented by the symbol $P \leftrightarrow Q$. For bi conditional statement, we use a double arrow \leftrightarrow . Since the truth works in both directions.

For examples:

Let P be the statement "shape is a triangle" and let Q be the statement "it has exactly three side".

"Shape is a triangle if and only if it has exactly three sides."

$$(P \rightarrow Q) \wedge (Q \rightarrow P)$$

The truth table for the Biconditional

		$P \leftrightarrow Q$
P	Q	$P \leftrightarrow Q$
T	T	T
T	F	F
F	T	F
F	F	T

"P is necessary and sufficient for Q"

"if P then Q and conversely."

Q1

(b) (i) Sam had Pizzo last night
 a Chris finished her homework.

(P \wedge Q)

P \Leftrightarrow Q		P \Leftrightarrow Q	
P	Q	P	Q
T	T	T	T
T	F	F	F
F	T	F	F
F	F	T	T

(ii) Chris and not finish her homework and Pat watched the news this morning ($\sim R \wedge Y$)

$\sim Y \Leftrightarrow P$

P	Y	$\sim Y$	$\sim Y \Leftrightarrow P$
T	T	F	F
T	F	T	T
F	T	F	T
F	F	T	F

civ Sam did not have Pizzo last night or Chris did not finish her homework

$$(\sim P \vee \sim Q)$$

$$\Leftrightarrow (Q \wedge \sim P)$$

P	Q	$\sim P$	$(Q \wedge \sim P)$	$\vee (\Leftrightarrow (Q \wedge \sim P))$
T	T	F	F	F
T	T	F	F	T
T	F	F	F	F
T	F	F	F	T
F	T	T	T	T
F	T	T	T	F
F	F	T	F	F
F	F	T	F	T

civ) $\vee (\Leftrightarrow (P \wedge Q))$

P	Q	\vee	$P \wedge Q$	$\vee (\Leftrightarrow (P \wedge Q))$
T	T	T	T	T
T	T	F	T	F
T	F	T	F	F
T	F	F	F	T
F	T	T	F	F
F	T	F	F	T
F	F	T	F	F
F	F	F	F	T

Question No 2

(i)

$P \sim Q \sim P$ = Bi Conditional
of truth table

P	Q	$P \sim Q$
T	T	T
T	F	F
F	T	F
F	F	T

(ii) $P \leftrightarrow Q \wedge \neg$

Solution:

P	Q	\neg	$Q \wedge \neg$	$P \leftrightarrow Q \wedge \neg$
T	T	T	T	T
T	T	F	F	F
T	F	T	F	F
T	F	F	F	F
F	T	T	T	F
F	T	F	F	T
F	F	T	F	T
F	F	F	F	T

(iii)

$$P \leftrightarrow (Q \vee \neg Q)$$

Solution

P	Q	\neg	$Q \vee \neg Q$	$P \leftrightarrow (Q \vee \neg Q)$
T	T	T	T	T
T	T	F	T	T
T	F	T	T	T
T	F	F	F	F
F	T	T	T	F
F	T	F	T	F
F	F	T	T	F
F	F	F	F	T

(iv)

$$\neg \leftrightarrow (P \vee Q)$$

Solution

P	Q	\neg	$P \vee Q$	$\neg \leftrightarrow (P \vee Q)$
T	T	T	T	T
T	T	F	T	F
T	F	T	T	T
T	F	F	T	F
F	T	T	T	T
F	T	F	F	T
F	F	T	T	T
F	F	F	F	T

Question 3

Arguments.

A logical argument is a claim that a set of premises support a conclusion.

Two types of argument, inductive and deductive argument.

Types of Arguments.

The inductive arguments uses a collection of specific examples as its premises and uses them to propose a general conclusion.

A deductive argument used collection of general statement at its premises and uses them to propose a specific situation as the conclusion.

~~we have developed the basic language of logic, we shall start to consider how logic can be used to determine whether or not a given argument is valid.~~ In order to do this

we shall first formally define exactly argument

"An argument is valid if whenever true statements are substituted in the statement variable the conclusion is

always true when a conclusion is reached using a valid argument. Before

we consider examples, we shall briefly examine how one can tell if a given argument from valid or invalid.

- (i) Identify the premises the conclusion
- (ii) to truth value premises & conclusion
- (iii) Look all the rows where the premises are all true, we call such critical row

Examples:-

$$P \rightarrow Q \quad Q \rightarrow \neg P$$

$$\therefore P \vee Q \rightarrow \neg P$$

Constructing a truth table we have

P	Q	$\neg P$	$P \rightarrow Q$	$Q \rightarrow \neg P$	$P \vee Q$	$P \vee Q \rightarrow \neg P$
T	T	F	T	F	T	F
T	F	F	F	T	T	F
F	T	T	T	T	T	T
F	F	T	T	T	F	T

Question #04

(a)

Unions:

The union of two sets A and B and the set of element which are in A in or in both A is denoted by $A \cup B$ and it is A Union B .

Example # 1

A	B	$A \cup B$
1	1	1
1	0	1
0	1	1
0	0	0

(b)

Intersection

The intersection of two sets A and B denoted by $A \cap B$ is the set of containing all elements of A that also belong to B (or frequently, all elements of B that also belong to A).

Example :-

C	D	$C \cap D$
1	1	1
1	1	1
1	0	0
1	0	0
0	1	0
0	1	0
0	0	0
0	0	0

Question 5

(a)

Venn diagram:

A Venn diagram is an illustration of relationships between and among sets, groups of objects that share something in common. Venn diagrams are used to depict set intersection (upside-down letter U).

This type of diagram is used in scientific and engineering presentations in computer application and in statistics.

Example: Points that belong to set x, y, z are gray.

Points x only set cyan

Color Point belonging only

Set y are magenta.

Point z belongs to yellow.

Point belonging to x and y

but not to z are blue

y & z but not to x are

red.

Page (14)

X and Z but not Y
∈ green. Points Contained
in all three Set are
black.

Practical example how venn
diagram can illustrate a
situation. Let universe
be the set of all
computer in the world. X
represent the set of all
notebook computer in the
world. Y represent the set
of all computer in the
world that are connected
to the internet.

Let Z represent the set
of all computer in
the world that have anti-
virus software installed.

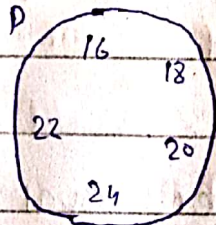
Q5

(b)

Solution: List out the element of P

$P = \{16, 18, 20, 22, 24\}$ "between" does not include 15 and 25

Draw a circle or oval, label it P, Put the element in P

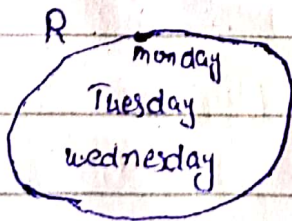


Example -

(c)

Solution $R = \text{Monday, Tuesday, Wednesday}$

Draw a circle or oval, label it R, Put the element in R

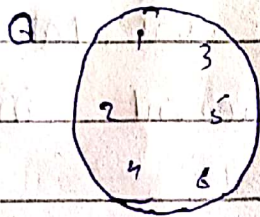


(C)

Solution:

Since an equation is given, we need to first solve for x

$$2x - 3 < 11 \Rightarrow 2x < 14 \Rightarrow x < 7$$



So $Q = \{1, 2, 3, 4, 5, 6\}$

Draw a circle or oval

Label it Q

Put the element in Q.

"The End"