

Final Term Summer 2020

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Subject: probability & Statistics. : Duration is 04 hours.

Instructor: Anwar Sharrim : Total marks = 50 ..

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Department of CED.

Q No# 01 ?

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Sol:-

Temperature	Chips per min	$xy$	$x^2$	$y^2$
53	20	1060	2809	400
62	32	1984	3844	1024
57	45	2565	3249	2025
71	60	4260	5041	3600
78	80	6240	6084	6400
id 22	100	2200	484	10000
86	120	10320	7396	14400
87	140	12180	7569	19600
96	160	15360	9216	25600
91	180	16380	8281	32400
94	200	18800	8836	40000
94	210	19740	8836	44100
<del>891</del>		<del>111089</del>	<del>60092</del>	<del>199509</del>
$\sum x$ 891	$\sum y$ = 1347	$\sum xy$ = 111089	$\sum x^2$ = 7645	

$\bar{x} = \frac{\sum x}{n}$

$x = \frac{891}{12}$

$\bar{y} = \frac{12}{12}$

$\bar{x} = 74.25$

$\bar{y} = \frac{1347}{12}$

$y = \frac{1347}{12}$

$\bar{y} = 112.25$

$n = 12$

$\sum x$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{12(111089) - (891)(1347)}{12(67645) - (891)^2}$$

$$b = 7.44$$

$$a = \bar{y} - b\bar{x}$$

$$a = 112.25 - 7.44(74.25)$$

$$a = 112.25 - 552.42$$

$$a = -440.17$$

$$\bar{y} = a + bx$$

$$y = -440.17 + 7.44x$$

Regression line equation.

(B) Coefficient correlation  $\gamma$  on  $x$ :

$$\gamma = \frac{n \sum xy - \sum x \sum y}{\sqrt{(n \sum x^2 - (\sum x)^2)(n \sum y^2 - (\sum y)^2)}}$$

$$\gamma = \frac{12(111089) - (891)(1347)}{\sqrt{12(67645)^2 - (891)^2 \cdot 12(109524)(1347)}}$$

$$\gamma = \frac{112895}{125082.25} = 0.90$$

Hence the estimated regression coefficient ~~the~~  $b = 7.44$  which indicated that the value of  $y$  increases by 7.44

unit increases in  $x$

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Q. No. 02? (part 2)

Solution:

~~$4+4+5=13$~~

(I)  $n(S) = \binom{13}{3} = 286$

4 - R
4 - W
5 - G
13 ball

Let A = Denote all ball of different colour.

$$n(A) = \binom{4}{1} \binom{4}{1} \binom{5}{1} = 4 \times 4 \times 5 = 80$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{80}{286} = 0.28$$

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$2 \times 2 \times 2 = 8$ even $\times$ even $\times$ even = even	$3 \times 2 \times 2 = 12$ odd $\times$ even $\times$ even = even	$3 \times 3 \times 2 = 18$ odd $\times$ odd $\times$ even = even
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Interpretation

$\Rightarrow \Rightarrow$  there are 28% chances that all ball are of different colours.

II let B = Denote all ball of same colours

Red white green

~~$n(B) = \binom{4}{3} \text{ or } \binom{4}{3} \text{ or } \binom{5}{3}$~~

$$n(B) = \binom{4}{3} \text{ or } \binom{4}{3} \text{ or } \binom{5}{3}$$

$$= \binom{4}{3} + \binom{4}{3} + \binom{5}{3} = 4 + 4 + 10 = 18$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{18}{286} = 0.063$$

Interpretation: there are 6.3% chances that all ball of same colours.

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Part B Qno#02?

Solution:

(I)

2	-	B
10	-	G
12		egg

$$n(S) = \binom{12}{4} = 495$$

let  $A$  = denote the event that exactly one egg is bad

$$n(A) = \binom{2}{1} \binom{10}{3} = 2 \times 120 = 240$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{240}{495} = 0.48$$

Interpretation: there are 48% chances that exactly one egg is bad

(II) let  $B =$  be the event that exactly  
One bad egg is Selected.

$$n(B) = \binom{2}{1} \binom{10}{3} + \binom{2}{2} \binom{10}{2}$$
$$= 2 \times 120 + 1 \times 45 = 240 + 45 = 285$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{285}{495} = 0.58$$

Interpretation: there are 58% chances  
that at least one bad egg is  
Selected.

QNO3?

Sol:-

	A	B	C
	12	47	15
	15	12	23
	6	76	52
	73	48	4
	7	4	24
ii)	22	22	22
	199	37	74
	36	48	52
	84	13	13
	29	3	4

$$\text{Range} = X_{\text{maximum}} - X_{\text{minimum}}$$

$$\text{Range of A} = X_m - x_0$$

$$= 199 - 6$$

$$\boxed{= 193} \text{ of A column range}$$



Range of B =  $\Sigma M - 10$

$= 76 - 3$

$= 73$  Range of column B

Range of C =  $\Sigma M - 10$

$= 74 - 4 = 70$

$= 70$  Range of column C

	Batsman A		Batsman B		Batsman C	
	$x$	$x^2$	$y$	$y^2$	$z$	$z^2$
	12	144	47	2209	15	225
	15	225	12	144	23	529
	6	36	76	5776	52	2704
	73	5329	48	2304	4	16
	7	49	4	16	24	576
	22	484	22	484	22	484
	199	39601	37	1369	74	5476
	36	1296	48	2304	52	<del>1072704</del> 2704
	84	7056	13	169	13	169
	29	841	3	9	4	16
	$\Sigma X =$	$\Sigma X^2 =$	$\Sigma y =$	$\Sigma Y^2 =$	$\Sigma Z =$	$\Sigma Z^2 =$
	483	<del>6755</del> 55061	310	14384	283	12599

Batsman A

$$\bar{x} = \frac{\sum x}{n}$$

$$\therefore n = 10$$

$$= \frac{483}{10}$$

$$\bar{x} = 48.3$$

$$S_x = \sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$

~~$$55061$$~~

$$\sqrt{\frac{55061}{10} - \left(\frac{483}{10}\right)^2}$$

$$S_x = 56.33$$

$$C.V = \frac{56.33 \times 100}{\bar{x}} = \frac{56.33}{48.3}$$

$$C.V = 1.16 \times 100$$

$$C.V = 116.62$$

Batsman B

$$\bar{y} = \frac{\sum y}{n} = \frac{310}{10}$$

$$\bar{y} = 31$$

$$s_y = \sqrt{\frac{\sum y^2}{n} - \left(\frac{\sum y}{n}\right)^2}$$

$$s_y = \sqrt{\frac{14384}{10} - \left(\frac{310}{10}\right)^2}$$

$$s_y = 21.84$$

$$C.V = 21.84 \times 100 = \frac{21.84}{28.3} \times 100$$

$$= 70.45\%$$

Batsman C

$$\bar{x} = \frac{\sum x}{n} = \frac{283}{10} = 28.3$$

$$s_x = \sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$

$$= \sqrt{\frac{12599}{10} - \left(\frac{283}{10}\right)^2}$$

$$= 21.42$$

$$C.V = \frac{21.42}{28.3} = 0.751 \times 100$$

$$C.V = 75\%$$

Batsman B is more consistent as  
it value of coefficient of variation  
is smallest.

Compare A with B

B is consistent.

Comp B with C:

B is 5% consistent

Compare A with C

C is more consistent

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