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SECTION :

B

SEMESTE :

6<sup>th</sup>

SUBJECT :

HYDRAULIC ENGR

INSTRUCTOR :

SIR FAWAZ.

## QUESTION - 1

### SOLUTION:-

The pressure drop  $\Delta P$  is expected to depend upon the gate opening  $h$ , the overall depth  $d$ , the velocity  $v$ , density  $\rho$  and velocity  $u$

List the relevant variable

$\Delta P, h, d, v, \rho, u$

write down dimension

$\Delta P$	$ML^{-1}T^{-2}$
$h$	$L$
$d$	$L$
$v$	$LT^{-1}$
$\rho$	$ML^{-3}$
$u$	$ML^{-1}T^{-1}$

No of variables  $n = 6$

No of independent dimension group  $= n - m = 3$

Choose  $m(3)$  scaling variable

geometric (d): kinetic / time - dependent (V):

dynamic / mass - dependent (P)

Form dimension groups by non dimensioning the remaining variable:  $\Delta P$ ,  $h$  and  $u$

$$\pi = \Delta P d^a v^b \rho^c$$

$$M^0 L^0 T^0 = (M L^{-1} T^{-2}) (L)^a (L T^{-1})^b (M L^{-3})^c$$
$$= M^{3+c} L^{-1+a+b-3c} T^{-2-b}$$

$$M: 0 = 1+c \quad L = -1$$

$$T: 0 = -2-b \quad b = -2$$

$$L: 0 = -1+a+b-3c \quad a = 1+3c-b=0$$

$$\Rightarrow \pi_1 = \Delta P v^2 \rho^{-1} = \frac{\Delta P}{\rho v^2}$$

$$\pi_2 = \frac{h}{d} \text{ (by inspection, since } h \text{ is a length)}$$

$$\pi_2 = u d^a v^b \rho^c \text{ (probably obvious by now but here goes anyway.)}$$

(3)

$$M^0 L^0 T^0 = (M L^{-1} T^{-1}) (L)^a (L T^{-1})^b (M L^{-3})^c$$

$$M^{1+c} L^{-1+a+b-3c} T^{-1-b}$$

$$M: 0 = 1+c \Rightarrow c = -1$$

$$T: 0 = -1-b+0 \Rightarrow b = -1$$

$$L: 0 = -1+a+b-3c \Rightarrow a = 1+3c-b = -1.$$

$$\Pi_3 = \mu d^{-1} v^{-1} f^{-1} = \frac{\mu}{f v d}$$

Recognition of the Reynold number suggest that we replace  $\Pi_3$  by

$$\Pi_3 = (\Pi_3)^{-1} = \frac{\rho v d}{\mu}$$

Hence dimensional analysis yields

$$\Pi_1 = f(\Pi_2, \Pi_3)$$

ie

$$\frac{\Delta P}{\rho v L} = f\left(\frac{h}{d}, \frac{\rho v d}{\mu}\right)$$

10      4

a) Dynamic Similarities requires that all non-dimensional group be the same in model and prototype i.e

$$\pi_1 = \left[ \frac{\Delta P}{\rho V^2} \right] = \left[ \frac{\Delta P}{\rho V^2} \right]_m$$

$$\pi_2 = \frac{h}{d} = \left( \frac{h}{d} \right)_m$$

$$\pi_3 = \left( \frac{\rho V d}{\mu} \right)_p = \left( \frac{\rho V d}{\mu} \right)_m$$

from the last we have velocity ratio

$$\frac{V_p}{V_m} = \frac{(\mu/\rho)_p}{(\mu/\rho)_m} = \frac{d_m}{d_p} = \frac{0.002/800}{1.6 \times 10^{-6}} \times \frac{1}{5}$$
$$= 0.5$$

Hence.

$$V_m = \frac{V_p}{0.5} = \frac{3.0}{0.5} = 6.0 \text{ m/s.}$$

⑤

The ratio of Quantities flow in

$$\frac{Q_p}{Q_m} = \frac{(\text{Velocity} \times \text{area})_p}{(\text{Velocity} \times \text{area})_m} = \frac{v_p}{v_m} \left( \frac{d_p}{d_m} \right)^2$$

$$\Rightarrow 0.5 \times 5^2$$

$$\Rightarrow \boxed{12.5}$$

For pressure drop.

$$\pi_1 = \left( \frac{\Delta P}{\rho v^2} \right) = \left( \frac{\Delta P}{\rho v^2} \right) = \frac{(\Delta P)_p}{(\Delta P)_m}$$

$$\Rightarrow \frac{\rho_p (v_p)^2}{\rho_m (v_m)^2}$$

$$= \frac{800}{1000} \times 0.5^2$$

$$\Rightarrow 0.2$$

$$\Delta P_m = 0.2 \times 60$$

$$\Rightarrow 120 \text{ kPa.}$$

## QUESTION - 2

DATA:-

Max length depth = 78m

Specific gravity = 2.4

 $\rho_{av} = 788 \text{ T/m}^2$ 

Height of wave = 1.2m.

SOLUTION:-

$$1) \quad H - \text{Limiting} = \frac{\rho_{av}}{\rho_w (4 - \omega + 1)}$$

$$= \frac{788 \times 1000}{1000 (2.4 - 0 + 1)}$$

$$\Rightarrow 231.765$$

7

2) Top WIDTH: (a)

$$\begin{aligned} \text{Free board} &= 1.5 \times \text{wave} \\ &= 1.5 \times 1.2 \\ &= 1.8 \end{aligned}$$

$$\begin{aligned} \text{Height of dam} &= H_w + F.B \\ &= 78 + 1.8 \\ &= 79.8 \end{aligned}$$

Height of dam =

$$\begin{aligned} a &= 14\% \text{ H.D} \\ &= 0.14 \times 79.8 \\ &= 11.17 \text{m} \end{aligned}$$

Base width

$$\begin{aligned} b &= \frac{H_w}{44} \\ &= \frac{78}{0.7 \times 2.4} \\ &= 46.42 \text{m} \cong 47 \text{m} \end{aligned}$$



20

8

47

for no tension Criteria

$$b' = \frac{Hw}{\sqrt{g}} = \frac{78}{\sqrt{2.4}}$$

$$= 50.34$$

57 Depth of vertical portion on  $\frac{1}{2}$  side

$$h' = 2a \sqrt{g \cdot w}$$

$$= 2(11.17) \sqrt{2.4 - 0}$$

$$= 34.60$$

$$\approx 35 \text{ m}$$

upstream of Set

$$\frac{a}{16} = \frac{11.17}{16}$$

$$= 0.6$$

Depth below the water level to the end of

$$\text{inclined portion } \frac{1}{2} = 3.14 a \sqrt{g}$$

$$3.14 \times 11.17 \sqrt{2.4}$$

$$\Rightarrow 54.33$$

249

(9)

Total width of the base of the dam

$$b = b' + \frac{a}{16}$$

$$\Rightarrow 50.34 + \frac{11.17}{16}$$

$$\boxed{b = 51.03}$$

$$\tan \theta = \frac{b'}{h} = \frac{50.34}{78}$$

$$\tan \theta = 0.64$$

$$\theta = \tan^{-1}(0.64)$$

$$\theta = 44.80^\circ$$

Depth of vertical portion on D/s (from WL on V/s side)

$$\tan \theta = \frac{a}{d'} = \frac{11.17}{d'}$$

$$d = 17.30 \text{ m}$$

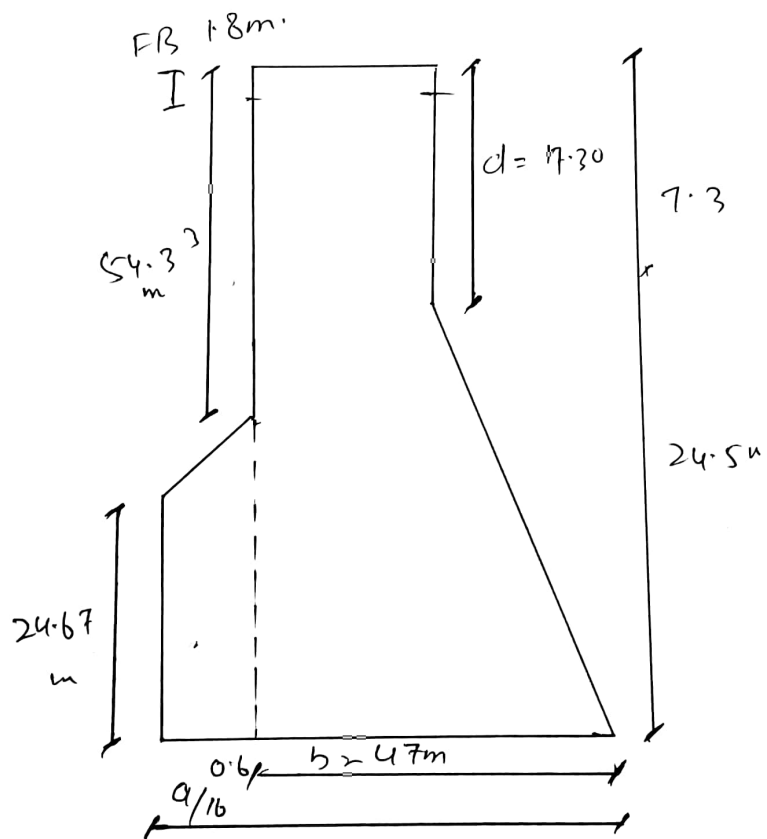
$$\therefore \tan \theta = \frac{11.17}{d'}$$

$$\therefore \left( \frac{839}{1300} \right) \times d' = 11.17$$

(10) 2 (5)

### Depth of vertical portion

$$\begin{aligned}d &= d' + f \cdot b \\ &= 17 + 30 \cdot 18 \\ &= 19.1\end{aligned}$$



(11)

### QUESTION- 3

Finding  $\pi$  group  
For drag on sphere using step by  
step method.

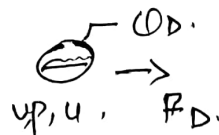
#### STATEMENT :

The drag  $F_D$  of sphere  
in a fluid flowing past the sphere is  
function of the velocity viscosity  $\mu$ , the  
mass density  $\rho$ , the velocity flow  $V$ ,  
and the diameter of sphere  $D$ . use  
steps to find  $\pi$  group.

#### SITUATION :-

Drag force (Sphere)

$$F_D = f(\rho, \mu, V, D)$$



(12)

GOAL:

Find  $\pi$  group (Steps).

IDEA:-

- ① Apply  $\pi$  Buckingham theorem
- ② Follow process

ACTION:-

$\pi$  - Buckingham

#  $\pi$ 's = # VARS - # primary dimen

$$= n - m$$

$$5 - 3 = 2.$$

STEP BY STEP TABLE:

~~FB~~ · ~~MDC~~

~~Buckingham~~  
~~#  $\pi$ 's~~

(13)

### STEP BY STEP METHOD.

F <sub>D</sub>	$\frac{ML}{T^2}$	F <sub>D</sub> /D	M/T <sup>2</sup>	$\frac{M}{T^2}$	$\frac{E}{PD^4}$	$\frac{F}{PD^2V^2}$
V	$\frac{L}{T}$	$\frac{V}{D}$	1/T	$\frac{1}{T}$	$\frac{V}{D}$	
P	$\frac{M}{L^3}$	PD <sup>3</sup>	PD <sup>3</sup>	M	—	
U	$\frac{M}{LT}$	UD	UD	M/T	$\frac{M}{PD^2T} = \frac{1}{T}$	$\frac{MD}{PD^2V}$
D	L	—	—	—	—	

$$\frac{F}{(PV^2) D^2} = f \left( \frac{U}{PD^2V} \right)$$

↓

$$Co \Rightarrow f(RC)$$

### QUESTION - 4

ANSWER:

#### PARTICLE DIAMETER:

The diameter of particle is directly proportional to the fall velocity because size of particle so greater the be moment. Thus there will be more gravitation force on particle of greater size so it will fall quickly due to its weight.

#### PARTICLE DENSITY:

Density of particle is directly proportional to the rate of fall velocity since particle with high density tends to settle down early comparing to low density particle.

### PARTICLE CONCENTRATION:-

Concentration  
 of particle size will considerably effect its fall velocity as the section having greater concentration will be settled down at the place. thus causing more fall velocity comparing with section of flow concentration.

### PARTICLE SHAPE:-

Particles having regular shape (having) tends to be affected more than irregular shape since regular shape particle have even surfaces which offer very little or no friction while particle with irregular shape offer more friction as the particle with smaller surface area are more likely to be effected due to their less resistance.