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MUSTAFA

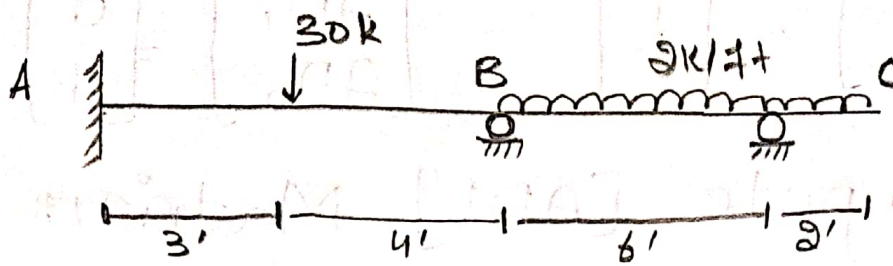
KHAN

ITJ: 7753

SEC: A"

SUBJECT: STRUCTURE II

# QUESTION # 1

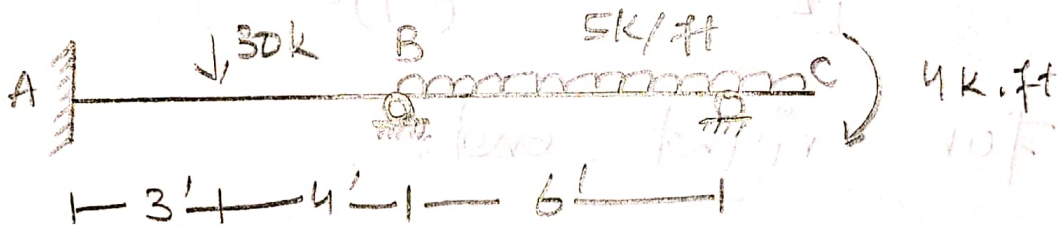


SOLUTION:

Determining Kinematic Indeterminacy

(Link  $K.I = 5^\circ$ )

so we have to reduce the extended portion.

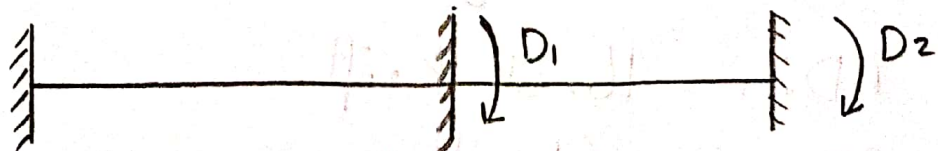


$$\Rightarrow \frac{\partial(\vartheta)}{1} = 4 \text{ k.ft}$$

Now

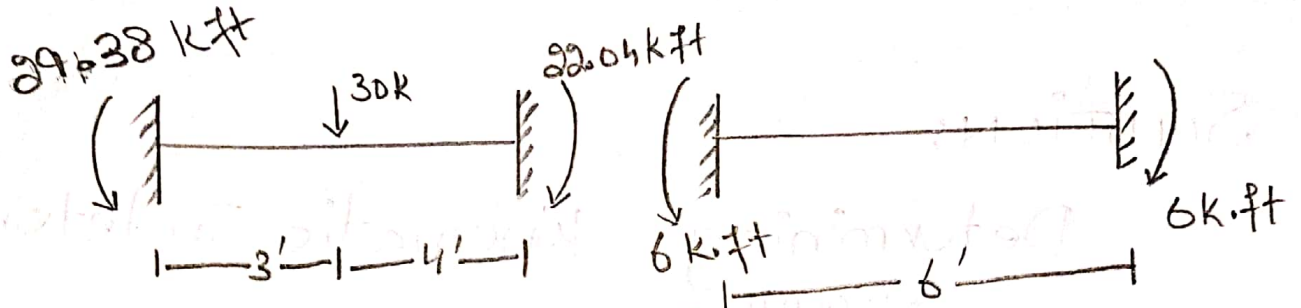
$$K.I = 2^\circ$$

★ Determine unknow joint displacement



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

\* Compute [ADL] Matrix:



⇒ For point load (not at mid)

⇒ For left end

$$\frac{Pab^2}{L^2} = \frac{(30)(3)^2(4)^2}{(7)^2} = 29.38 \text{ k-ft}$$

⇒ For right end:

$$\frac{Pa^2b}{L^2} = \frac{(30)(3)^2(4)}{(7)^2} = 22.04 \text{ k-ft}$$

⇒ For UDL:

$$\frac{WL^2}{12} = \frac{(2)(6)^2}{12} = 6 \text{ k-ft}$$

$$ADL_1 = 16.04 \text{ k-ft}$$

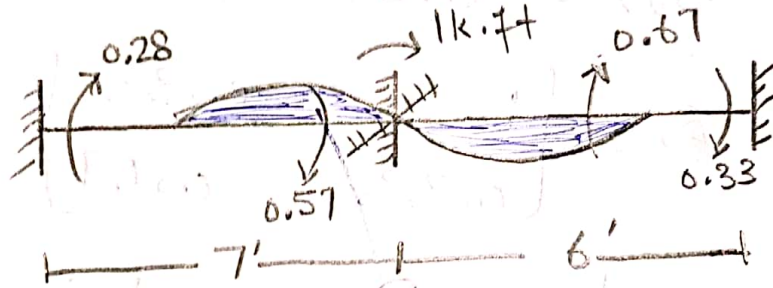
$$ADL_2 = 6 \text{ k-ft}$$

\* compute [S] matrix:

$$S = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}$$

$q = D_1$

a)  $D_1 = 1k$  ,  $D_2 = 0$



$$\frac{4EI}{7} = 0.57$$

$$\frac{2EI}{6} = 0.33$$

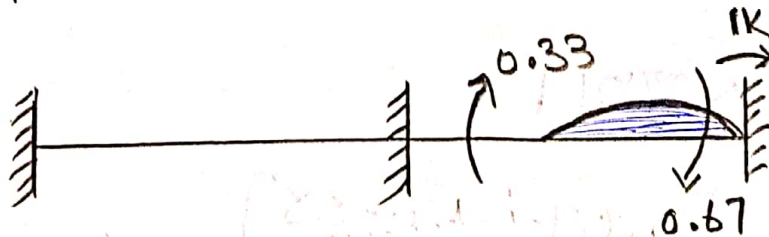
$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{7} = 0.28$$

$$S_{11} = 0.57 + 0.67 = 1.24 EA$$

$$S_{21} = 0.33 EA$$

b)  $D_1 = 0$  ,  $D_2 = 1k$





$$\frac{4EI}{6} = 0.67$$

$$\frac{2EI}{6} = 0.33$$

$$S_{12} = 0.33$$

$$S_{22} = 0.67$$

$$S = \begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}$$

\* Compute D matrix,

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}^{-1} \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$= \frac{1}{\begin{bmatrix} 1.24 & 0.33 \\ 0.33 & 0.67 \end{bmatrix}} \times \text{Adj } A \times \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} - \begin{bmatrix} ADL_1 \\ ADL_2 \end{bmatrix}$$

$$|S| = (1.24 \times 0.67) - (0.33 \times 0.33)$$

$$= 0.8368 - 0.1089$$

$$|S| = 0.7279$$

$$\text{Adj } A = \begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix}$$

Now

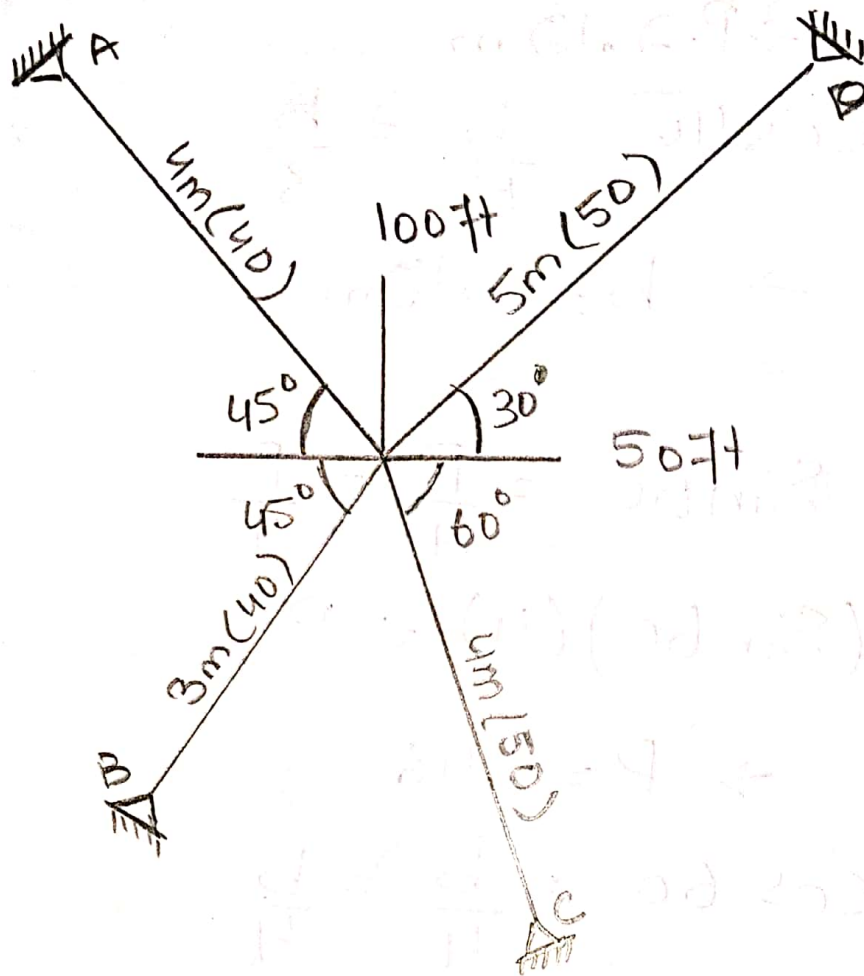
$$\begin{bmatrix} AD_1 - ADL_1 \\ AD_2 - ADL_2 \end{bmatrix} = \begin{bmatrix} 0 - 16.04 \\ 4 - 6 \end{bmatrix}$$

$$= \begin{bmatrix} -16.04 \\ -2 \end{bmatrix} E$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \frac{\begin{bmatrix} 0.67 & -0.33 \\ -0.33 & 1.24 \end{bmatrix} \times \begin{bmatrix} -16.04 \\ -2 \end{bmatrix}}{0.7219}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} -13.83 \\ 3.85 \end{bmatrix}$$

# QUESTION # 2:



SOLUTION:

For A:

$$\sin 45^\circ = \frac{P}{H} = \frac{P}{4}$$

$$\rightarrow P = 2.828 \text{ m}$$

$$\cos 45^\circ = \frac{b}{H} = \frac{b}{4}$$

$$\rightarrow b = 2.828 \text{ m}$$

For B:

$$\sin 45 = \frac{P}{H} = \frac{P}{3}$$

$$\rightarrow P = 2.12 \text{ m}$$

$$\cos 45 = \frac{b}{H} = \frac{b}{3}$$

$$\rightarrow b = 2.12 \text{ m}$$

For C:

$$\sin 60 = \frac{P}{H} = \frac{P}{4}$$

$$(\sin 60)(4) = P$$

$$\rightarrow P = 3.46$$

$$\cos 60 = \frac{b}{H} = \frac{b}{4}$$

$$\cos 60 \times 4 = b$$

$$\rightarrow b = 2$$

For D:

$$\sin 30 = \frac{P}{5}$$

$$\rightarrow P = 2.5 \text{ m}$$

$$\cos 30 = \frac{b}{5}$$

$$b = 4.33 \text{ m}$$



Now

$$EA(A) = 2000 \times 40 = 80000t$$

$$EA(B) = 2000 \times 40 = 80000t$$

$$EA(C) = 2000 \times 50 = 100000t$$

$$EA(D) = 2000 \times 50 = 100000t$$

★ KI

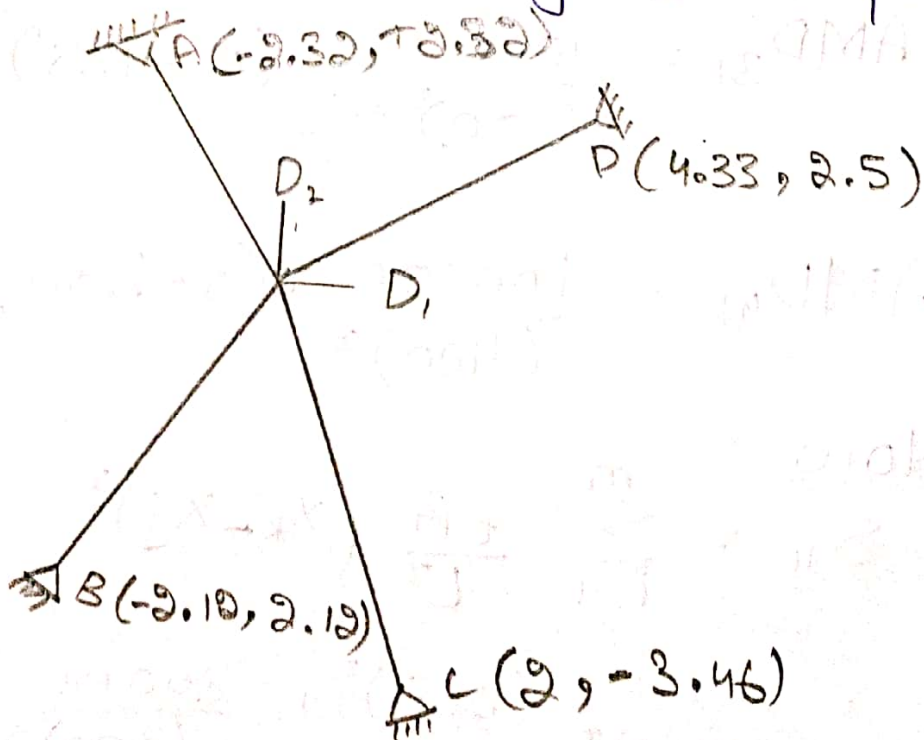
$$KI = 2j - r$$

$$= 2(5) - 8$$

$$KI = 2^{\circ}$$

★

select unknown joint displacement



$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix} \quad \begin{bmatrix} AD_1 \\ AD_2 \end{bmatrix} = \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\star \quad [AMD]_{4 \times 2} \quad [S]_{2 \times 2}$$

$$i) \quad D_1 = 1k, \quad D_2 = 0$$

$$AMD = \frac{EA}{L^2} (x_k - x_j)$$

$$AMD_{11} = \frac{80000}{(400)^2} \times (0 + 282) = 141$$

$$AMD_{21} = \frac{80000}{(300)^2} (0 + 212) = 188.44$$

$$AMD_{31} = \frac{100000}{(500)^2} \times (0 - 433) = -173.2$$

$$AMD_{41} = \frac{100000}{(400)^2} \times (0 - 200) = -125$$

Now

$$S_{11} = \sum_{i=1}^3 \frac{EA}{L^3} (x_k - x_j)^2$$

$$= \frac{80000}{(400)^3} (282)^2 + \frac{80000}{(300)^3} \times (212)^2$$

$$+ \frac{100000}{(500)^3} (433)^2$$

$$+ \frac{100000}{(500)^3} (-433)^2 + \frac{100000}{(400)^3} (-200)^2$$

$$S_{11} = 99.405 + 133.107 + 149.991 + 62.5$$

$$\underline{S_{11} = 445.063}$$

$$\Rightarrow S_{12} = S_{21} = \sum_{i=2}^m \frac{EA}{L^3} x(x_k - x_j)(y_k - y_j)$$

$$= \frac{80000}{(400)^3} (282)(-282) + \frac{80000}{(300)^3} (212)(212)$$

$$+ \frac{100000}{(500)^3} (-433)(-250) + \frac{100000}{(400)^3} (-200)(+346)$$

$$\underline{S_{12} = S_{21} = 19.237}$$

ii)  $D_1 = 0$        $D_2 = 1k$

$$AMD = \frac{EA}{L^2} (y_k - y_j)$$

$$AMD_{12} = \frac{80000}{(400)^2} (-282) = -141$$

$$AMD_{22} = \frac{80000}{(300)^2} (212) = 188.44$$

$$AMD_{32} = \frac{100000}{(500)^2} (-250) = -100$$

$$AMD_{y2} = \frac{100000 (346)}{(400)^2} = 216.25$$

$$\text{Now } S_{22} = \sum_{i=1}^m \frac{EA}{L^3} (Y_k - Y_j)^2$$

$$= \frac{80000}{400^3} (-282)^2 + \frac{80000}{300^3} (212)^2$$

$$+ \frac{100000}{500^3} (-250)^2 + \frac{100000}{400^3} (346)^2$$

$$S_{22} = 469.628$$

$$\star [D] = [S]^{-1} \times [AD]$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 445.003 \\ 12.237 \end{bmatrix}$$

$$\begin{bmatrix} 12.237 \\ 469.628 \end{bmatrix}^{-1} \times \begin{bmatrix} 50 \\ -100 \end{bmatrix}$$

$$\begin{bmatrix} D_1 \\ D_2 \end{bmatrix} = \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$

$$\star [AM]$$

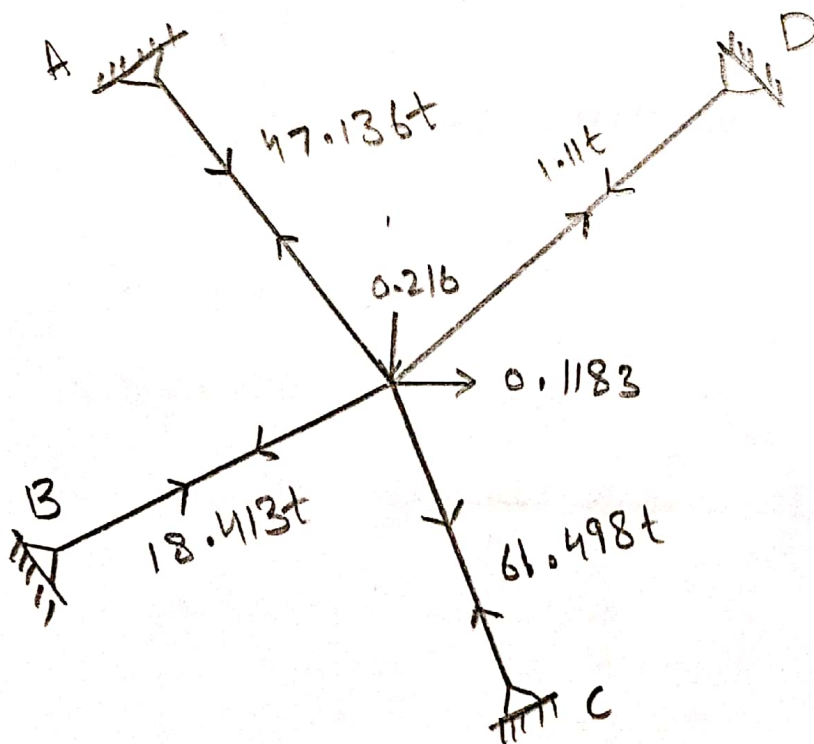
$$\begin{bmatrix} AM_1 \\ AM_2 \\ AM_3 \\ AM_4 \end{bmatrix} = \begin{bmatrix} 141 & -141 \\ 188.44 & 188.44 \\ -173.2 & -100 \\ -125 & 216.25 \end{bmatrix} \times \begin{bmatrix} 0.1183 \\ -0.216 \end{bmatrix}$$



$$= \begin{bmatrix} 141 \times 0.1183 + (-141) \times (-0.216) \\ 188.44 \times 0.1183 + (188.44) \times (-0.216) \\ -173.2 \times 0.1183 + (-100) \times (-0.216) \\ -125 \times 0.1183 + 216.25 \times (-0.216) \end{bmatrix}$$

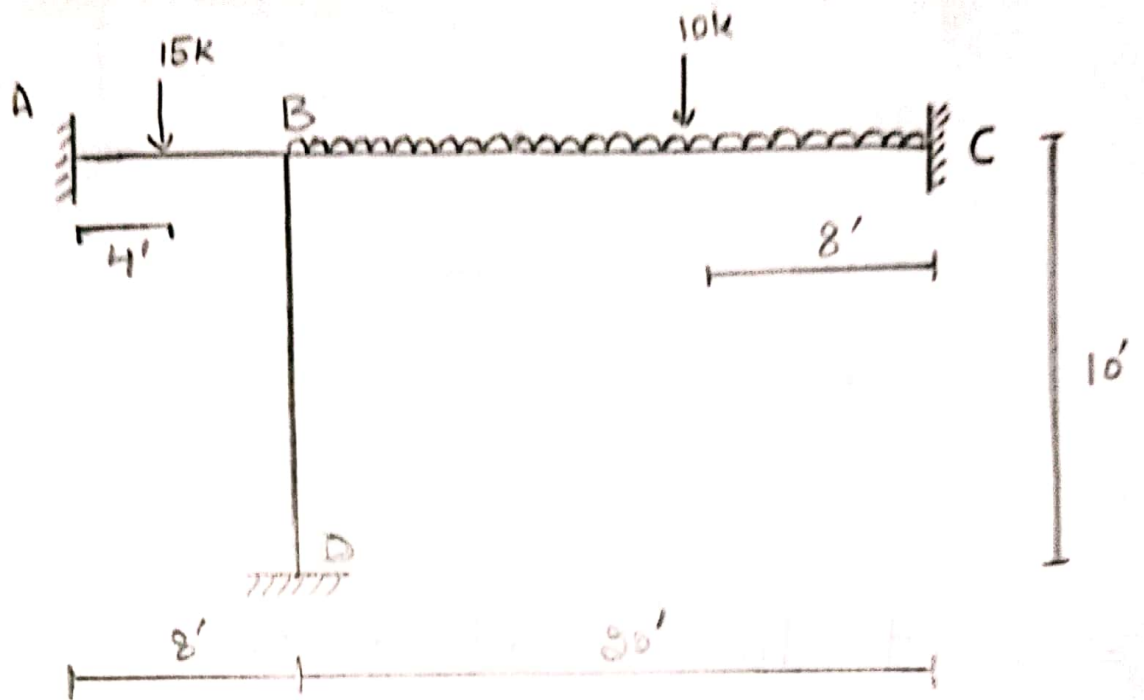
$$\begin{bmatrix} AMD_1 \\ AMD_2 \\ AMD_3 \\ AMD_4 \end{bmatrix} = \begin{bmatrix} 16.68 + 30.46 \\ 22.29 - 40.70 \\ -20.49 + 21.6 \\ -14.79 + 46.71 \end{bmatrix}$$

$$\begin{bmatrix} AMD_1 \\ AMD_2 \\ AMD_3 \\ AMD_4 \end{bmatrix} = \begin{bmatrix} 47.136t \\ -18.413t \\ 1.11t \\ -61.498t \end{bmatrix}$$





# QUESTION #3.

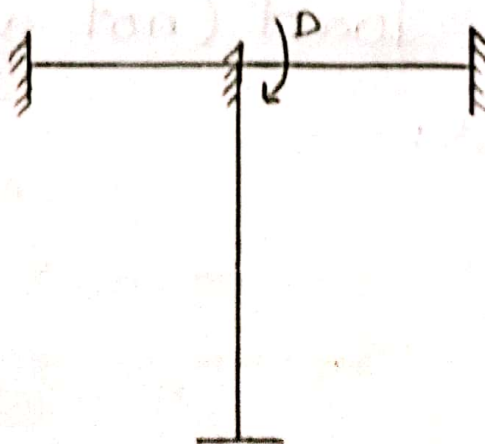


SOLUTION:

\* Determine kinematic indeterminacy

$$K.I = 1$$

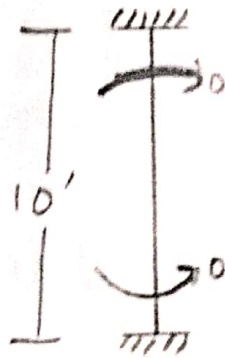
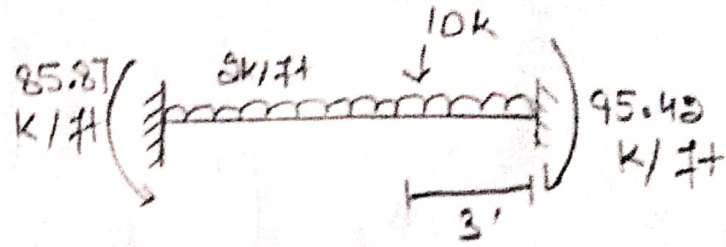
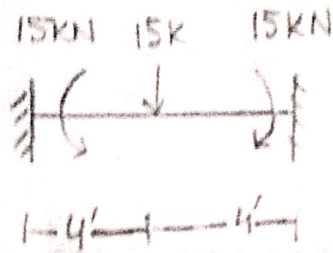
\* Determine unknown joint displacement



$$[D] = ?$$

$$[AD] = [0]$$

\* Compute [ADL] matrix.



⇒ point load at centre:

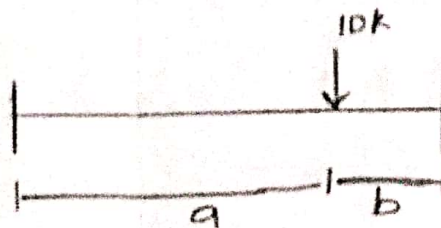
$$\frac{PL}{8} = \frac{(15)(8)}{8} = 15 \text{ kip}\cdot\text{ft}$$

⇒ Uniform distributed load:

$$\frac{WL^2}{12} = \frac{(3)(20)^2}{12} = 66.67 \text{ k}\cdot\text{ft}$$

⇒ Point load (not at mid):

Suppose:



For left end:

$$\frac{Pa^2b^2}{L^2} = \frac{(10)(12)(8)^2}{(20)^2} = 19.2 \text{ k}\cdot\text{ft}$$

For right end:

$$\frac{Pa^2b}{L^2} = \frac{(10)(12)^2(8)}{(20)^2} = 28.8 \text{ k}\cdot\text{ft}$$

So total moment at left end:

$$19.2 + 66.67 = 85.87 \text{ k}\cdot\text{ft}$$

similarly at right end:

$$28.8 + 66.67 = 95.47 \text{ k}\cdot\text{ft}$$

So

$$[ADL] = -85.87 + 15 = -70.87 \text{ k}\cdot\text{ft}$$

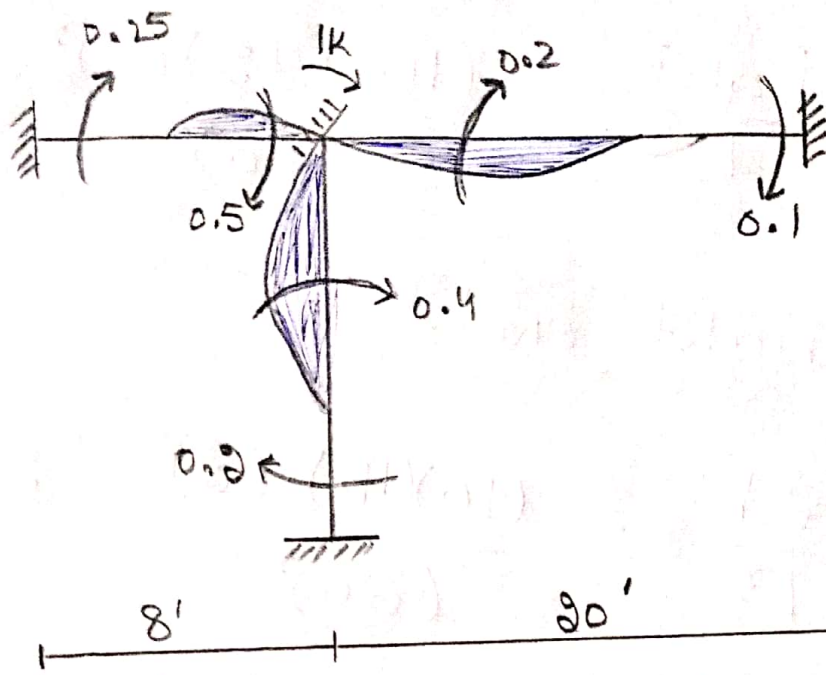
\* Determine  $[S]$  matrix:

$$[S] = [S_{11}]$$

Now

$$D = 1 \text{ k}$$





$$\Rightarrow \frac{4EI}{8} = 0.5$$

$$\frac{2EI}{8} = 0.25$$

$$\Rightarrow \frac{4EI}{20} = 0.2$$

$$\frac{2EI}{20} = 0.1$$

$$\Rightarrow \frac{4EI}{10} = 0.4$$

$$\frac{2EI}{10} = 0.2$$

$$[S] = (0.5 + 0.4 + 0.2) EI$$

$$= 1.1 EI$$

$$[S] = 1.1 EI$$

$$[D] = [S]^{-1} \times [AD] - [ADL]$$

$$[D] = \frac{1}{1.1} \times [0] - [-70.87] = \frac{70.87}{1.1}$$

$$[D] = [64.42] \text{ k/EI} \quad \text{ANSWER.}$$