

Name

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Subject

Structural Analysis I

Date

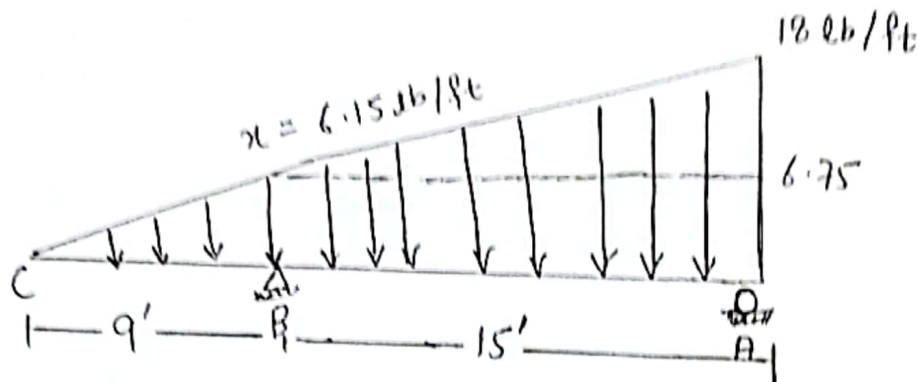
26-9-2020

Question no. 1 (i)

Draw the shear and bending moment equation and diagrams for the beam shown in fig 1. The value of the uniformly varying load is the last two digits of your registration number.

Answer no. 1

Solution:-



By using similar triangle Method

$$\frac{18}{(15+9)} = \frac{x}{9}$$

$$(18 \times 9) = 24x$$

$$162 = 24x$$

$$x = \frac{162}{24} = 6.75 \text{ lb/ft}$$

$$\sum R_A = 0 \quad (R_B \times 15) - \left(18 \times \frac{24}{2}\right) \left(\frac{24}{3}\right) = 0$$

$$15R_B = 1728$$

$$R_B = \frac{1728}{15} = \boxed{115.2 \text{ lb}}$$

$$\sum R_B = - (R_B \times 15) + (6.75 \times 15) \left(\frac{15}{2}\right) + \left(11.25 \times \frac{15}{2}\right) \left(\frac{2 \times 15}{3}\right)$$

$$- \left(6.75 \times \frac{9}{2}\right) \left(\frac{9}{3}\right) = 0$$

$$= -15R_B + 1512 =$$

$$R_A = \frac{1512}{15} = \boxed{100.8 \text{ lb}}$$

(Shear force calculator)

$$S.F@ C = \boxed{0}$$

$$S.F@ B = -(6.75 \times 9) \frac{11}{2} = \boxed{-30.375 \text{ lb}}$$

again S.F@ B = $-30.325 + 115.2$

$$= \boxed{84.825 \text{ lb}}$$

$$S.F@ A = -(18 \times 24) \frac{1}{2} + 115.2$$

$$= -216 + 115.2$$

$$= \boxed{-100.8 \text{ lb}}$$

again S.F@ B = $-100.8 + 100.8$

$$= \boxed{0}$$

(Bending Moment Calculation)

$$B.M@ C = 0$$

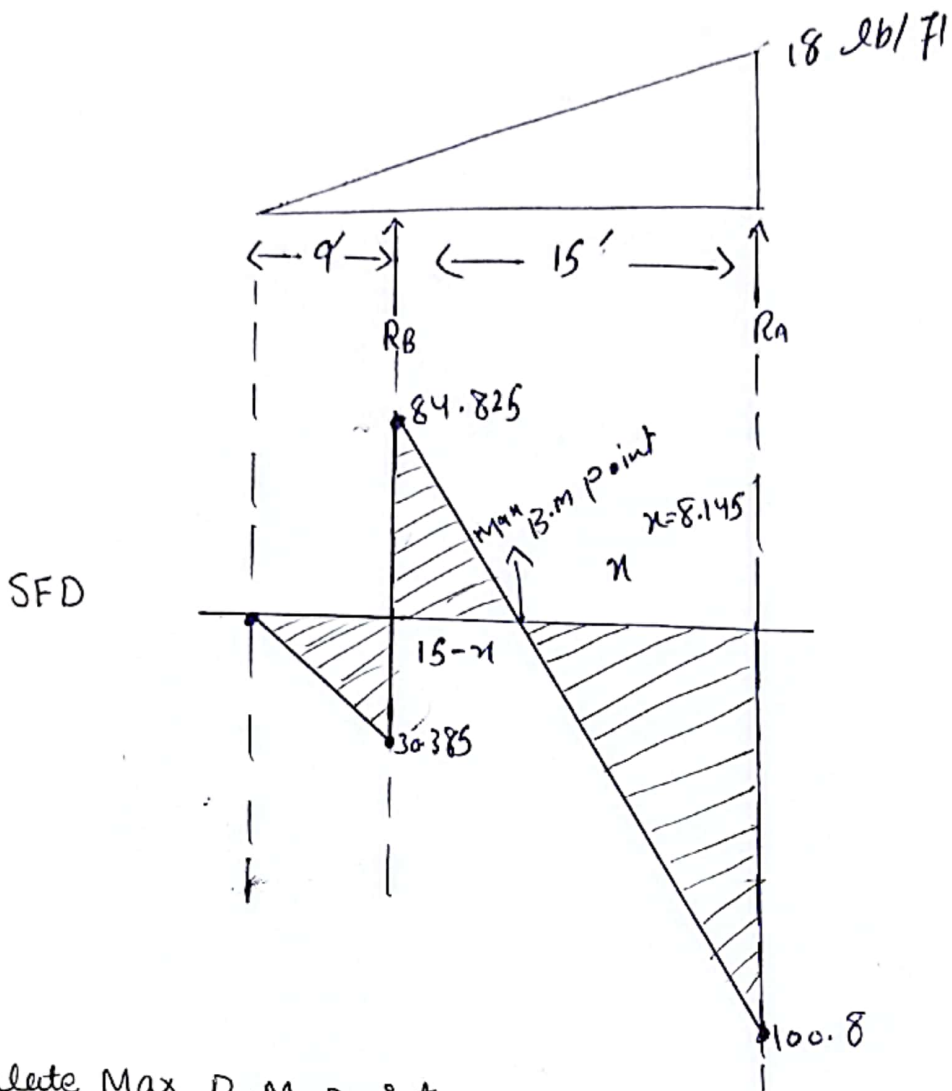
$$B.M@ B = (-6.75 \times 9) \frac{9}{3} = \boxed{-182.25 \text{ lb-ft}}$$

$$B.M@ A = (18 \times \frac{24}{2}) (\frac{24}{3}) + \cancel{115.2} \times 15$$

$$= -1728 + 1728$$

$$= \boxed{0 \text{ lb-ft}}$$

(3)



Calculate Max B.M point by Similar triangle m.

$$\frac{84.825}{15-x} = \frac{100.8}{x}$$

$$84.825x = 1512 - 100.8x$$

$$185.625x = 1512$$

$$x = 8.145$$

Similar Triangle m

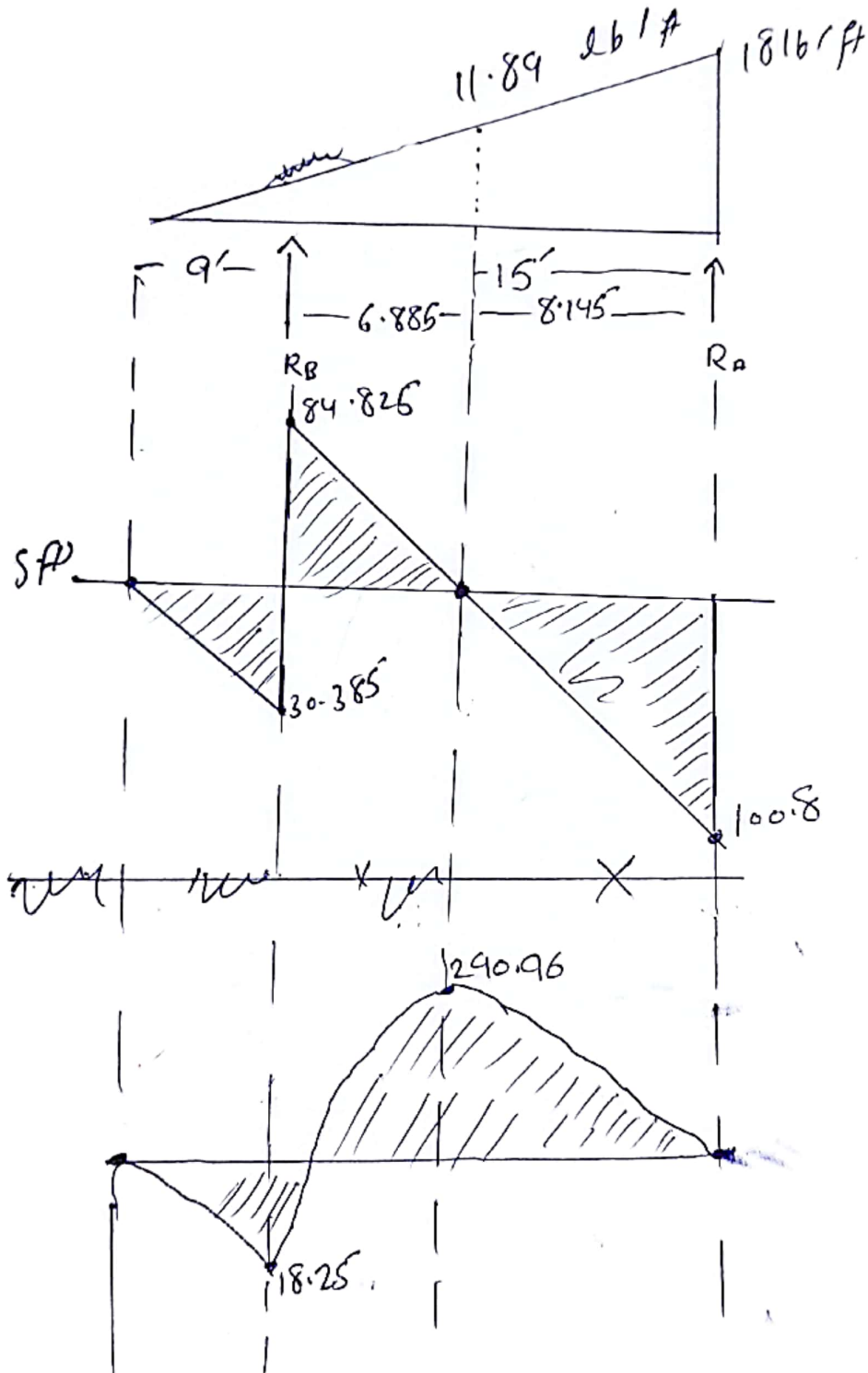
$$\frac{18}{25} = \frac{x}{15.855}$$

$$x = 11.89 \text{ lb/ft}$$

(4)

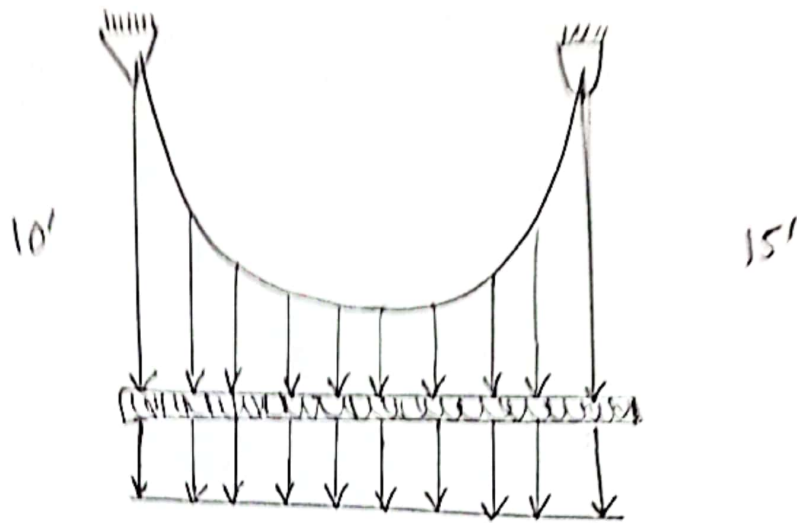
$$B.M @ D = - \left(11.89 \times \frac{15.855}{2} \right) \left(\frac{15.855}{3} \right) + (115.2 \times 6.855)$$

$$B.M @ D = \boxed{290.96 \text{ lb-ft}}$$



Question no. 2

Solution:-



- Cable supports uniform load 918 lb/ft
- Determine the tension in cable at,
- Support A = ?
- Support B = ?

Solution:-

$$y = \frac{w_0}{2F_H} x^2$$

by putting the value

$$15 = \frac{918}{2F_H} x^2 \quad \text{--- (i)}$$

$$10 = \frac{918}{2F_H} (25-x)^2 \quad \text{--- (ii)}$$

By solving both equations

$$F_H = \frac{918}{2(15)} x^2, \quad F_H = \frac{918}{2(10)} (25-x)^2$$

$$F_H = F_H$$

$$\frac{918}{2(15)} x^2 = \frac{918}{2(10)} (25-x)^2$$

$$\frac{918x^2}{30} = \frac{918(125+x^2-2 \times 25 \times x)}{20}$$

$$\frac{918}{30} x^2 = \frac{918}{20} (125+x^2-50x)$$

$$30 \cdot 6 x^2 = 45 \cdot 9 (125+x^2-50x)$$

$$x^2 = \frac{45 \cdot 9}{30 \cdot 6} (125+x^2-50x)$$

$$x^2 = 1.5 (125+x^2-50x)$$

$$x^2 = (187.5 + 1.5x^2 - 75x)$$

$$15x^2 - x^2 - 75x + 187.5 = 0$$

$$0.5x^2 - 75x + 187.5 = 0 \text{ --- (i)}$$

Multiply by 2 to get x^2 in regular

$$2(0.5x^2 - 75x + 187.5) = 0$$

$$x^2 - 150x + 375 = 0$$

By Applying quadratic equation, $x_{1/2} = 2.543$

$$\text{As } F_H = \frac{918}{30} x^2 = \frac{918}{30} (2.543)^2$$

$$F_H = 197.88 \text{ lb-ft}$$

$$F_H = \frac{918}{20} (25-x)^2$$

$$= \frac{918}{20} (25-2.543)^2$$

$$= 23148.14 \text{ lb-ft}$$

$$\tan \theta = \frac{918 \times 2.543}{197.88}$$

$$\tan \theta = 197.88$$

$$\theta = \tan^{-1}(197.88)$$

$$\theta = 89.71^\circ$$

Now

$$T_A \sin \theta = w_0 x$$

$$T_A = \frac{w_0 x}{\sin \theta} = \frac{918 \times 2.543}{\sin 89.71}$$

$$T_A = 2334.50 \text{ lb}$$

Now

$$w_0 x = (25 - 2.543)$$

$$x = 22.457$$

$$\tan \theta = \frac{918 \times 22.457}{23148}$$

$$\theta = 41.68^\circ$$

$$T_B = \frac{918 \times 22.457}{\sin 41.68^\circ}$$

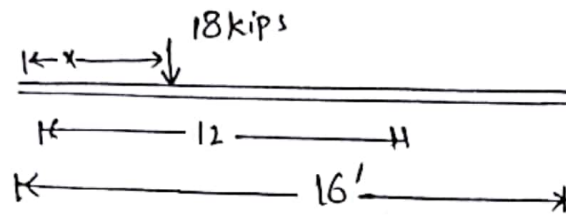
$$T_B = 31002.20 \text{ lb}$$

Question no. 3

Draw the shear force influence line for beam shown in fig. 3. Also influence line for reaction A.

Answer no. 3

Solution:-



For $x = 0$
 $R_A = ?$

$$\sum M_B = (18 \times 16) - R_A(16) = 0$$

$$= 288 - 16R_A = 0$$

$$R_A = \frac{288}{16} = 18$$

$$R_A = 18 \text{ kips}$$

For

$$x = 1 \text{ ft}$$

$$\sum M_B = (18 \times 15) - R_A(16) = 0$$

$$\Rightarrow 270 - 16R_A = 0$$

$$R_A = 16.875 \text{ kips}$$

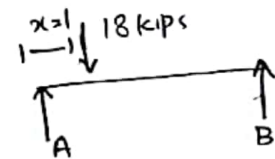
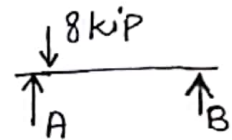
For

$$x = 5$$

$$R_A = ?$$

$$\sum M_B = (18 \times 11) - R_A(16) = 0$$

$$R_A = \frac{198}{16} = 12.375 \text{ kips}$$



put $x = 7$ $RA = ?$

$\hookrightarrow MB = (18 \times 9) - RA \times 16 = 0$

$RA = \frac{161.25}{16}$ kips

Put $x = 10$ $RA = ?$

$\hookrightarrow MB = (18 \times 6) - RA \times 16 = 0$

$RA = \frac{67.5}{16}$ kips

put $x = 12$ $RA = ?$

$\hookrightarrow MB = (18 \times 4) - RA \times 16 = 0$

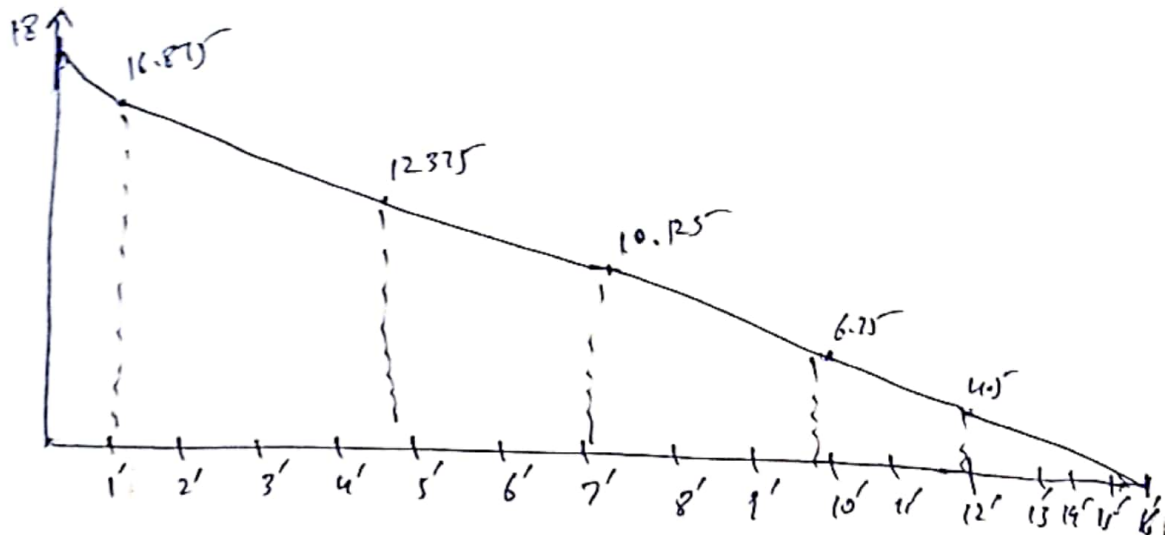
$RA = 4.5$ kips

put $x = 16$ $RA = ?$

$\hookrightarrow MB (18 \times 0) - RA \times 16$

$0 - RA$

$RA = 0$



(Influence line diagram)