

FINAL TERM EXAMINATION

NAME SABQ-UL-HASSAN

ID 7932

SECTION B

DEPARTMENT BE (C)

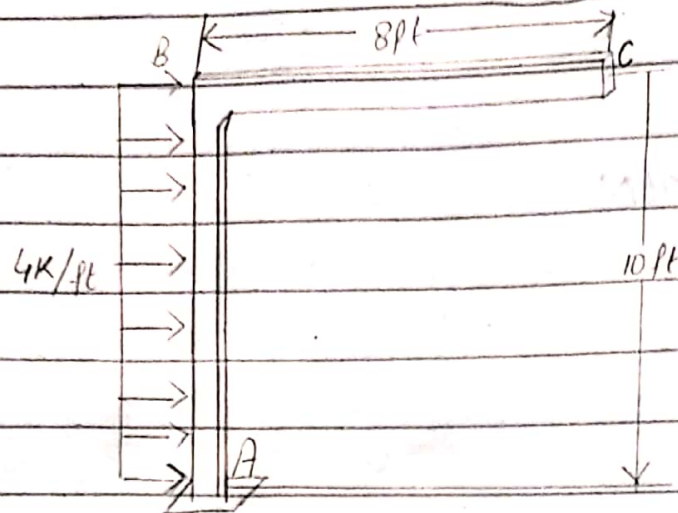
SUBJECT STRUCTURAL ANALYSIS - I

DATE 26-JUNE-2020

TEACHER SIR AMJAD ISLAM

QUESTION No 01

DETERMINE the vertical displacement at C
Use method of Virtual Work?



TO FIND :-

Virtual work = $\Delta c = ?$

GIVEN THAT :-

$$E = 29(10^3) \text{ Ksi}$$

$$I = 300 \text{ in}^4$$

SOLUTION

As we know that

For REACTION :-

$$\sum M_A = 0$$

$$-4(10)(5) + c_y(8) = 0$$

$$c_y = 25 \text{ Kips}$$

$$\sum \bar{F}_y = 0 \quad \uparrow +$$

$$25 + A_y = 0$$

$$A_y = -25 \text{ Kip}$$

$$\sum F_x = 0 \quad \rightarrow +$$

$$40 - A_x = 0$$

$$A_x = +40 \text{ Kips}$$

REAL MOMENTS

$$\sum M_1 = 0$$

$$-40x_1 + 4x_1 \left(\frac{x_1}{2} \right) + M_1 = 0$$

$$M_1 = 40x_1 - 2x_1^2$$

$$-25x_2 + M_2 = 0$$

$$M_2 = 25x_2$$

VIRTUAL MOMENTS

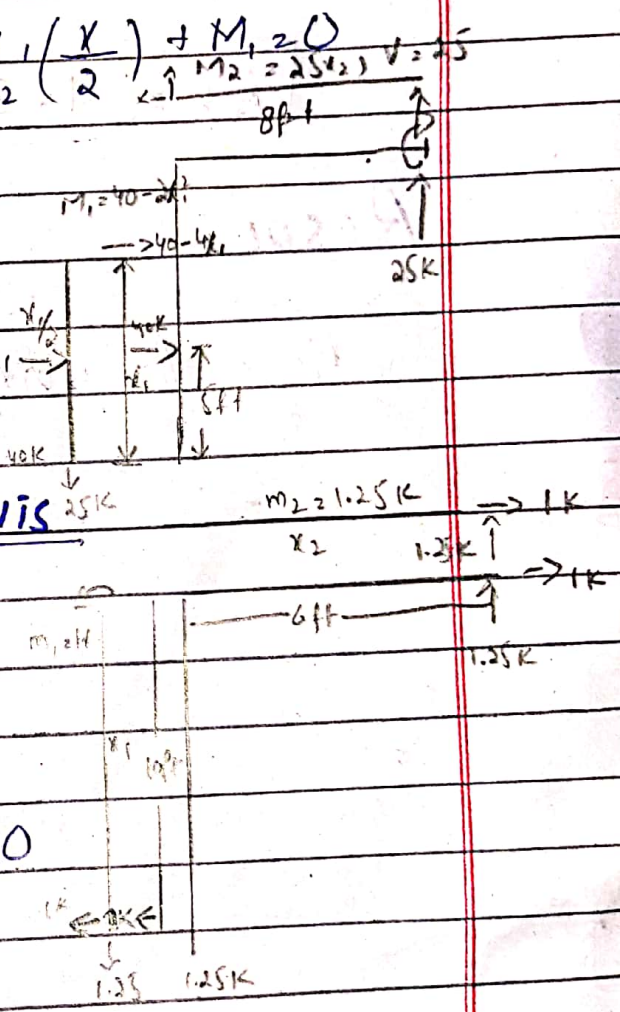
$$\sum m_1 = 0$$

$$-1(x_1) + m_1 = 0$$

$$m_1 = 1x_1$$

$$-m_2 + 1.25x_2 = 0$$

$$m_2 = 1.25x_2$$



FROM VIRTUAL WORK EQUATION :-

$$1 \text{ K} \cdot \Delta_{ch} = \int_0^L m M dx / EI$$

$$1 \text{ K} \cdot \Delta_{ch} = \int_0^{18} \frac{(40x_1 - 2x_1^2)(1x_1) dx}{EI}$$

$$\Delta_{ch} = \frac{8333.3}{EI} + \frac{5333.3}{EI}$$

$$\Delta_{ch} = \frac{13666.7}{EI} \text{ K}^2 \text{ ft}^3$$

$$= \frac{13666.7 \text{ K}^2 \cdot \text{ft} (12^3 \text{ in}^3 / 1 \text{ ft}^3)}{(29 \times 10^3 \text{ K/in}^2) (600)}$$

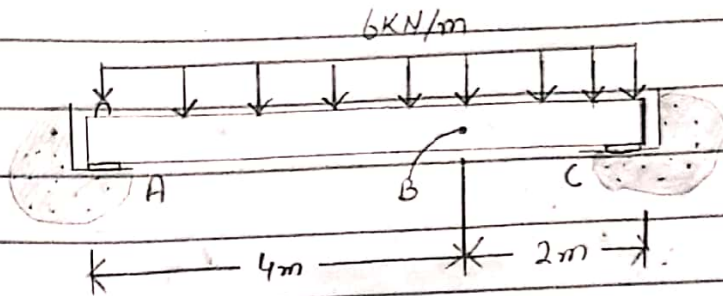
$$\Delta_{ch} = 1.357 \text{ in}$$

RESULT

Hence the Virtual work = $\Delta_{ch} = 1.357 \text{ in}$

QUESTION No 02

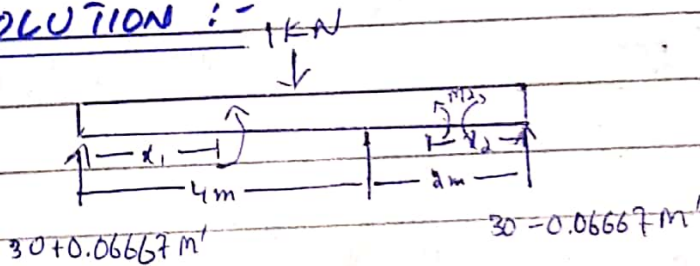
Determine the slope and
Use Castigliano's Theorem.



To FIND :-

We have to find the slope
and displacement

SOLUTION :-



$$M_1 = (30 + 0.06667 M') x_1 - 2x_1^2$$

$$M_2 = (30 + 0.06667 M') x_2 - 2x_2^2$$

Now

$$\frac{\partial M_1}{\partial M'} = 0.06667 x_1 \text{ and}$$

$$\text{And } \frac{\partial M_2}{\partial M'} = 0.06667 x_2$$

$$\text{Set } M' = 0$$

$$\text{Now } M_1 = (30x_1 - 2x_1^2) \text{ K.ft}$$

And

$$M_2 = (30x_2 - 2x_2^2) \text{ K.ft}$$

Thus

$$\begin{aligned} Q_B &= \int_0^L m \left(\frac{\delta M}{\delta M'} \right) \frac{dx}{EI} \\ &= \int_0^{4m} \frac{(30x_1 - 2x_1^2)(0.06667x_1)}{EI} dx \rightarrow \\ &\quad + \int_0^{2m} \frac{(30x_2 - 2x_2^2)(0.06667x_2)}{EI} dx_2 \\ &= \frac{1}{EI} \left[\int_0^{4m} (2.001x_1^2 - 0.1334x_1^3) dx_1 + \int_0^{2m} (2.001x_2^2 - 0.1334x_2^3) dx_2 \right] \end{aligned}$$

$$= \frac{1}{EI} \left[\frac{2.001x_1^3}{3} \Big|_0^4 - \frac{0.1334x_1^4}{4} \Big|_0^4 + \frac{2.001x_2^3}{3} \Big|_0^2 - \frac{0.1334x_2^4}{4} \Big|_0^2 \right]$$

$$= \frac{1}{EI} \left[\frac{0.667x_1^3}{10} \Big|_0^4 - \frac{0.3335x_1^4}{10} + \frac{0.667x_2^3}{10} \Big|_0^2 - \frac{0.03335x_2^4}{10} \Big|_0^2 \right]$$

$$Q_B \Rightarrow \frac{1}{EI} [42.688 - 8.5376 + (5.336 - 0.5336)]$$

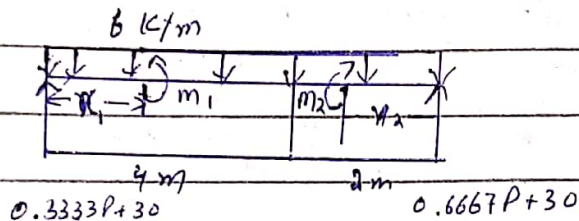
$$Q_B = \frac{38.9504}{EI}$$

$$Q_B = \frac{38.9504}{(200 \times 10^9)(60 \times 10^6 \text{ in } m^4)}$$

$$Q_B = \frac{38.9504}{(200 \times 10^9)(6 \times 10^{-5})}$$

$$Q_B = 0.03245 \times 10^{-4} \text{ radian}$$

Now DISPLACEMENT



$$\text{Now } M_1 = (0.33P+30)x_1 - 2x_1^2$$

$$M_2 = (0.6667P+30)x_2 - 2x_2^2$$

$$\text{Now } \frac{\delta M_1}{\delta P} = 0.3333x_1$$

$$\text{And } \frac{\delta M_2}{\delta P} = 0.6667x_2$$

$$\text{Set } P=0$$

$$M_1 = (30x_1 - 2x_1^2) \text{ and } M_2 = (30x_2 - 2x_2^2)$$

$$\Delta B = \int_0^4 m \left(\frac{\delta M}{\delta P} \right) \frac{dx}{EI}$$

$$\Rightarrow \Delta B = \frac{1}{EI} \left[\int_0^4 (30x_1 - 2x_1^2) 0.3333x_1 dx_1 + \int_0^2 (30x_2 - 2x_2^2) 0.6667 dx_2 \right]$$

$$\Rightarrow \Delta B = \frac{1}{EI} \left[\int_0^4 (9.999x^2 - 0.6666x^3) dx + \int_0^2 (20.001x^2 - 1.3334x^3) dx \right]$$

$$\Delta B = \frac{1}{EI} \left[\frac{9.999x^3}{3} \Big|_0^4 - \frac{0.6666x^4}{4} \Big|_0^4 + \frac{20.001x^3}{3} \Big|_0^2 - \frac{1.3334x^4}{4} \Big|_0^2 \right]$$

$$\Delta B = \frac{1}{EI} \left[(213.33 - 42.6624) + (53.336 - 5.336) \right]$$

$$\Delta B = \frac{218.6676}{(200 \times 10^9)(6 \times 10^{-5})}$$

$$\Delta B = 0.1822 \times 10^{-4} \text{ ft}$$

$$\Delta B = 2.186 \times 10^{-4}$$

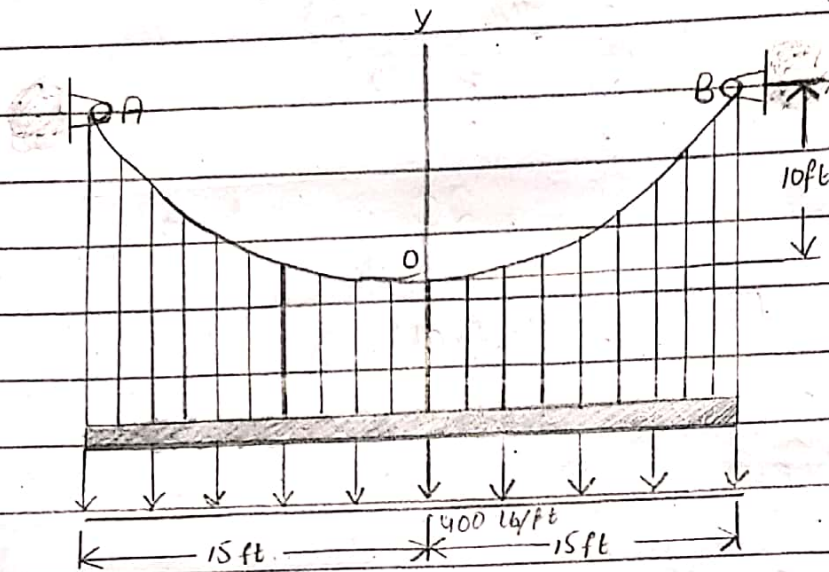
Hence

$$\phi_B = 0.03245 \times 10^{-4}$$

$$\Delta B = 2.186 \times 10^{-4}$$

QUESTION No 03

The cable is subjected to the uniform ~~curve~~ curve and the force in the cable at O, B.



To Find :-

We have to find the equation of the curve and the force in the cable at O and B.

SOLUTION :-

As we know that

$$y = \frac{h x^2}{L^2}$$

$$= \frac{10 x^2}{(15)^2}$$

$$y = 0.0444 x^2$$

AND

$$\begin{aligned}T_0 = F_H &= \frac{W_0 L^2}{2h} \\&= \frac{400 (15)^2}{2(10)} \\&= \frac{400 \times 225}{2(10)} \\&= \frac{90000}{20} \\&= 4500 \text{ lb}\end{aligned}$$

$$F_H = 4.500 \text{ K.lb}$$

Now As we know that

$$T_H = T_{\max} = \sqrt{(F_H)^2 + (W_0 L)^2}$$

$$= \sqrt{(4500)^2 + [(400)(15)]^2}$$

$$T_{\max} = \sqrt{(4500)^2 + (6000)^2}$$

$$T_{\max} = 7500 \text{ lb} = 7.500 \text{ K.lb}$$

Now,

$$T_B = T_{\max} = W_0 L \sqrt{1 + \left(\frac{L}{2h}\right)^2}$$

$$= 400(15) \sqrt{1 + \left(\frac{15}{2 \times 10}\right)^2}$$

$$= 6000 \sqrt{1 + \frac{225}{400}}$$

$$= 6000 \sqrt{\frac{400 + 225}{400}}$$

$$= 6000 \sqrt{\frac{625}{400}}$$

$$= 6000 \sqrt{1.5625}$$

$$= 6000 (1.25)$$

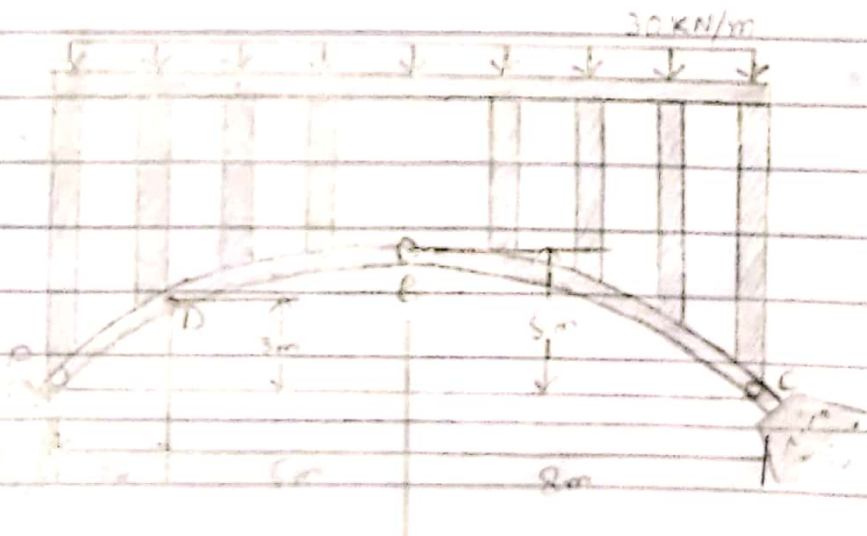
$$T_H = T_{max} = 7500 \text{ lb}$$

OR

$$T_H = T_{max} = 7500 \text{ lb} = 7.5 \text{ K lb}$$

QUESTION No 04

The Three hinged spandrel ...
... in the arch at point D?



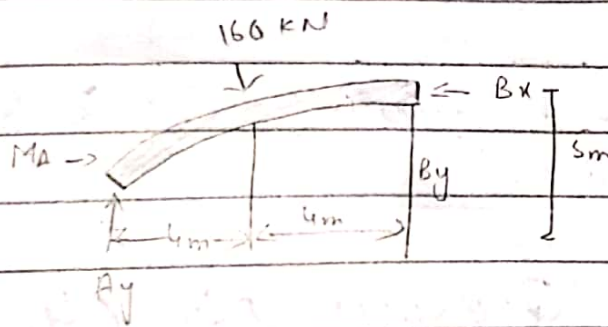
SOLUTION :-

MEMBER AB :-

$$\sum \text{MA} = 0$$

$$\Rightarrow B_x(5) + B_y(8) - 240(4) = 0$$

$$5B_x + 8B_y = 960$$



MEMBER BC :-

$$\sum \text{Mc} = 0$$

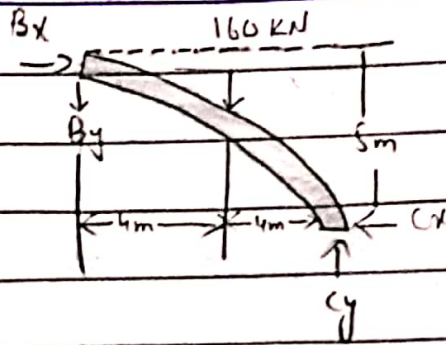
$$\Rightarrow B_x(5) + B_y(8) + (240)(4) = 0$$

As $B_y = 0$

$$\Rightarrow -5B_x + 0 + 960$$

$$\Rightarrow 5B_x = 960$$

$$\Rightarrow B_x = 192$$



MEMBER BD :-

$$\curvearrowright M_D = 0$$

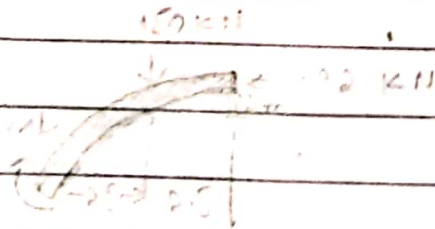
$$\Rightarrow (B_x)(2) - (150 \times 2.5) - M_D = 0$$

$$\Rightarrow (192 \times 2) - (375) - M_D = 0$$

$$\Rightarrow 384 - 375 - M_D = 0$$

$$\Rightarrow 9 - M_D = 0$$

$$\Rightarrow \boxed{M_D = 9 \text{ kN.m}}$$



RESULT

HENCE $M_D = 9 \text{ kN.m}$