## Department of Electrical Engineering

Assignment
Date: 13/04/2020

## Course Details

Course Title: Linear Circuit Analysis
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Instructor: Sir Sohail Imran

Module: 2
30
Total Mark $\qquad$

## Student Details

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|  |  | Determine the power supplied by the leftmost element in the circuit of following figure | PLO1 |
| :---: | :---: | :---: | :---: |
|  | (c) | Following figure depicts the current-voltage characteristic of three different resistive elements. Determine the resistance of each, assuming the voltage and current are defined in accordance with the passive sign convention. | $\begin{array}{\|l\|} \hline \begin{array}{l} \text { Marks } \\ 3 \end{array} \\ \hline \text { PLO1 } \end{array}$ |
|  |  |  <br> (a)  <br> (b)  <br> (c) |  |
| Q2 | (a) | Refer to the circuits of following figures, and answer the following: <br> 1. How many distinct nodes are contained in the circuit? | Marks $4$ |


|  |  | 2. How many elements are contained in the circuit? <br> 3. How many branches does the circuit have? <br> 4. Determine if each of the following represents a path, a loop, both, or neither: <br> i. $\quad \mathrm{A}$ to B <br> ii. $\quad \mathrm{B}$ to D to C to E iii. C to <br> E to D to B to A to C <br> iv. $\quad \mathrm{C}$ to D to B to A to C to E | PLO2 |
| :---: | :---: | :---: | :---: |
|  | (b) | For the circuit of following figure (which is a model for the dc operation of a bipolar junction transistor biased in forward active region), $I_{B}$ is measured to be $100 \mu \mathrm{~A}$. Determine $I_{C}$ and $I_{E}$ | $\begin{array}{\|l\|} \hline \text { Marks } \\ 6 \\ \hline \text { PLO2 } \\ \hline \end{array}$ |
|  |  |  |  |
| Q3 | (a) | Although drawn so that it may not appear obvious at first glance, the circuit of following figure is in fact a single-node-pair circuit. <br> a. Determine the power absorbed by each resistor. <br> b. Determine the power supplied by each current source. <br> c. Show that the sum of the absorbed power calculated in (a) is equal to the sum of the supplied power calculated in (b). | Marks 5 <br> PLO1 |
|  | (b) |  | Marks <br> 5 |



## Ans 1(a):-

First we have to use Ohm's Law

$$
\begin{aligned}
& V=I R \\
& I=\frac{V}{R}
\end{aligned}
$$

First find Power :

$$
P=V I
$$

To find first circuit. So we have to take the current in opposite side means with negative sign

$$
\begin{aligned}
& V=I R \\
& I=\frac{V}{R} \\
& I=\frac{5 v}{10000 \Omega} \\
& I=0.0005 A \\
& I=0.5 m A
\end{aligned}
$$

Now for Power

$$
\begin{aligned}
& P=V I \\
& P=5 \times 0.5 \times 10^{-3} \\
& P=2.5 \times 10^{-3} \\
& P=0.25 \mathrm{~mW}
\end{aligned}
$$

Now for $2^{\mathrm{ND}}$ circuit:

$$
\begin{aligned}
& V=I R \\
& I=\frac{V}{R} \\
& I=\frac{-5 v}{10000 \Omega} \\
& I=-0.0005 A \\
& I=-0.5 m A
\end{aligned}
$$

For power

$$
\begin{aligned}
& P=V I \\
& P=5\left(-0.5 \times 10^{-3}\right) \\
& P=-2.5 \times 10^{-3} \\
& P=-0.0025 \mathrm{~W} \\
& P=-0.25 \mathrm{~mW}
\end{aligned}
$$

For $3^{\text {rd }}$ circuit:

$$
\begin{aligned}
& V=I R \\
& I=\frac{V}{R} \\
& I=\frac{-5 v}{10000 \Omega} \\
& I=-0.0005 A \\
& I=-0.5 \mathrm{~mA}
\end{aligned}
$$

Then Power

$$
\begin{aligned}
& P=V I \\
& P=5\left(-0.5 \times 10^{-3}\right) \\
& P=-2.5 \times 10^{-3} \\
& P=-0.25 \mathrm{~mW}
\end{aligned}
$$

Now Circuit $4^{\text {th }}$ :

$$
\begin{aligned}
& V=I R \\
& I=\frac{V}{R} \\
& I=\frac{5 v}{10000 \Omega} \\
& I=0.5 m A
\end{aligned}
$$

For Power

$$
\begin{aligned}
& P=V I \\
& P=5\left(0.5 \times 10^{-3}\right) \\
& P=2.5 \times 10^{-3} \\
& P=0.25 \mathrm{~mW}
\end{aligned}
$$

## Ans 1(b):

We know that

$$
\begin{aligned}
& P=V I \\
& P=2 v \times 2 A \\
& P=4 W
\end{aligned}
$$

In this circuit voltage and current are given
We will multiply two factors to find power

$$
2 v \times 2 A=4 w
$$

This $4 w$ is supplied. And we will take current with positive sign.

Ans 1(c):
For this we have to use Ohm's Law

$$
\begin{aligned}
& V=I R \\
& O R \quad R=\frac{V}{I}
\end{aligned}
$$

To find R take the value of I and V from the graph

## Solution (a)

## Given that

$$
\begin{aligned}
& I=0.01 m A \\
& V=1 V \\
& R=?
\end{aligned}
$$

## Calculation:

Using Ohm's Law
$V=I R$
$R=\frac{V}{I}$
$R=\frac{0.5 A}{5 V}$
$R=10 \mu S$
$R=\frac{1 v}{0.01 \times 10^{-3}}$
$R=100 \times 10^{3}$
$R=100 \mathrm{k} \Omega$

## Solution (b)

## Given that:

From graph we know that current is zero

$$
\begin{aligned}
& V=1 v \\
& I=0 \\
& R=?
\end{aligned}
$$

## Calculation:

We know that

$$
\begin{aligned}
V & =I R \\
R & =\frac{V}{I} \\
R & =\frac{1 v}{0} \\
R & =\infty
\end{aligned}
$$

## Solution (c)

## Given that:

From this graph we come to know that the current is infinite

$$
\begin{aligned}
& V=1 v \\
& I=\infty \\
& R=?
\end{aligned}
$$

## Calculation:

We know that

$$
\begin{aligned}
V & =I R \\
R & =\frac{V}{I} \\
R & =\frac{1}{\infty}
\end{aligned}
$$

$$
R=0 \quad \text { So, we have zero resistance }
$$

Ans 2(a):

1) Number of nodes $=4$
2) Number of elements $=5$
3) Number of branches $=5$
4) 

i. Neither
ii. Only path
iii. Path and loop
iv. neither

## Ans 2(b):

## We know that KCL tells us that

Total current entering a node $=$ total current leaving a node
So by this equation;

$$
\mathrm{I}_{B}+I_{C}=I_{E}
$$

Or

$$
\begin{aligned}
& \mathrm{I}_{E}=I_{B}+I_{C} \Rightarrow \mathrm{I}_{C}=150 . I_{B} \\
& \mathrm{I}_{C}=15 \mathrm{~mA}
\end{aligned}
$$

Now,

$$
\begin{aligned}
& \mathrm{I}_{E}=150 \times 10^{-3}+100 \times 10^{-6} \\
& \mathrm{I}_{E}=15.1 \mathrm{~mA}
\end{aligned}
$$

## Ans 3(a):

We know that

$$
\mathrm{V}=\mathrm{IR}
$$

So

$$
\mathrm{V}=2 \times 637 \times 10^{-3} \Rightarrow 1.274 \mathrm{~V}
$$

Now find current I of each

$$
\mathrm{V}=\mathrm{IR}
$$

$$
\mathrm{I}=\frac{V}{R}
$$

Let

$$
\begin{aligned}
& \mathrm{I}_{X}=\frac{1.274 v}{1000 \Omega} \\
& \mathrm{I}_{X}=0.001274 A \\
& \mathrm{I}_{X}=1.274 \mathrm{~mA}
\end{aligned}
$$

Now

$$
\begin{aligned}
& \mathrm{I}_{Y}=\frac{1.274 v}{2800 \Omega} \\
& \mathrm{I}_{Y}=0.000455 \mathrm{~A} \\
& \mathrm{I}_{Y}=0.455 \mathrm{~mA}
\end{aligned}
$$

Then

$$
\begin{aligned}
& \mathrm{I}_{Z}=\frac{1.274 v}{4700 \Omega} \\
& \mathrm{I}_{Z}=0.000271 \mathrm{~A} \\
& \mathrm{I}_{Z}=0.271 \mathrm{~mA}
\end{aligned}
$$

Now to find Power,
We know the equation

$$
\begin{aligned}
P & =V I \\
\Rightarrow \quad P(2.8 \mathrm{k}) & =(1.274 \mathrm{v})(0.455) \\
& =0.5797 \mathrm{~mW} \\
\Rightarrow \quad \mathrm{P}(4.7 \mathrm{k}) & =(1.274)(0.271) \\
& =0.3452 \mathrm{~mW} \\
\Rightarrow \quad \mathrm{P}(1 \mathrm{k})= & (1.274)(1.274) \\
& =1.6230 \mathrm{~mW}
\end{aligned}
$$

$$
\begin{aligned}
\Rightarrow \quad \mathrm{P}(5 \mathrm{~mA}) & =(1.274)(-5) \\
& =-6.37 \mathrm{~mW} \\
\Rightarrow \quad \mathrm{P}(3 \mathrm{~mA}) & =(1.274)(3)
\end{aligned}
$$

Ans 3(b):
In this circuit first we will calculate the source and equivalences:

$$
\begin{aligned}
i_{e q} & =4-2 i+3-9 \\
& =4-2 i-6 \\
\mathrm{i}_{e q} & =-2-2 i \\
R_{e q} & =(6+3 \| 5)\|6\| 6 \\
R_{e q} & =8.5 \| 3=2.217 \Omega
\end{aligned}
$$

Now find voltage V:

$$
\begin{aligned}
& V=i_{e q} \cdot \mathrm{R}_{e q} \\
& V=(-2-2 i)(2.217 \Omega)
\end{aligned}
$$

From diagram;

$$
\begin{gathered}
V=6 i \\
6 i=(-2-2 i)(2.217) \\
6 i=-4.434-4.434 i \\
6 i+4.434 i=-4.434 \\
10.434 i=-4.434 \\
\mathrm{i}=\frac{-4.434}{10.434} \\
\mathrm{i}=-0.424 \mathrm{~A} \\
v=-2.55 v \\
\text { So, } \\
\quad P=\frac{V^{2}}{R} \\
P_{15 \Omega}=\frac{(-2.55)^{2}}{15} \\
V_{15 \Omega}=\frac{6}{6.25} \\
V_{15 \Omega}=1.8 v
\end{gathered}
$$

Now Power,

$$
\begin{aligned}
P_{15 \Omega} & =\frac{V^{2}}{R} \\
& =\frac{(1.8)^{2}}{15 \Omega} \\
& =\frac{3.24}{15} \\
P_{15 \Omega} & =0.216 \mathrm{~W}
\end{aligned}
$$

Finished !

