

BILAL

ID = 16020

Discrete Structure

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8:00AM to 11:00AM

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1

(Q14) Let  $p$  be the statement "DATAENDFLAG is off,"  $q$  the statement "ERROR equal 0" and  $r$  the statement "Sum is less than 1000." Express the following sentence in symbolic notation:

(a) DATAENDFLAG is off, ERROR equal 0, and SUM is less than 1,000.

$p =$  DATAENDFLAG is off.

$q =$  ERROR equal 0.

$r =$  "Sum is less than 1,000."

$p \wedge q \wedge r$

(b) DATAENDFLAG is off but ERROR is not equal to 0

$p =$  "DATAENDFLAG is off."

$q =$  "ERROR equal 0."

$r =$  "Sum is less than 1,000."

$p \wedge \neg q$

(c) DATAENDFLAG is off, however ERROR is not 0, or SUM is greater than or equal to 1000.

$p =$  "DATAENDFLAG is off."

$q =$  "ERROR is equal to 0."

$r =$  "Sum is less than 1000."

$p \wedge (\neg q \vee r)$

(d) DATAENDFLAG is on and ERROR equal 0 but Sum is greater than or equal to 1000.

$p =$  "DATAENDFLAG is off."

$q =$  "ERROR is equal 0"

$r =$  "Sum is less than 1000."

$\neg p \wedge q \wedge \neg r$

Either DATAENDFLAG is on or it is the case that both ERROR is equal 0 and Sum is less than 1000.

$\Rightarrow$   $P$  " DATAENDFLAG is off,  
 $Q$  " ERROR equal 0,  
 $Y$  " Sum is less than 1000.

$$\sim PV(Q \vee Y)$$

(a)(b) = Show that  $P \vee Q \rightarrow Y \equiv (P \rightarrow Y) \wedge (Q \rightarrow Y)$ .

$\therefore$  So from column (5) and (8) values are same  
 So hence Proved that  $P \vee Q \rightarrow Y \equiv (P \rightarrow Y) \wedge (Q \rightarrow Y)$   
 L.H.S = R.H.S

P	Q	Y	$P \vee Q$	$P \vee Q \rightarrow Y$	$P \rightarrow Y$	$Q \rightarrow Y$	$(P \rightarrow Y) \wedge (Q \rightarrow Y)$
T	T	T	T	T	T	T	T
T	T	F	T	F	F	F	F
T	F	T	T	T	T	T	T
T	F	F	T	F	F	T	F
F	T	T	T	T	T	T	T
F	T	F	T	F	T	F	F
F	F	T	F	T	T	T	T
F	F	F	F	T	T	T	T

Q3 In the back of an old cupboard you discover a note signed by a pirate famous for his bizarre sense of humor and love of logical puzzles. In the notes he wrote that he had hidden a treasure somewhere on the property. He listed five sentences (a.e. below) and challenged the reader to use them to figure out the location of the treasure.

A) If this house is next to the lake, then the treasure is not in the kitchen.

B) If the tree in the front yard is an elm then the treasure is in the kitchen.

C) The house is next to the lake.

D) The tree in the front yard is an elm and the ~~front~~ treasure is buried under the ~~flag pole~~ flag pole.

E) If the tree in the backyard is an oak then the treasure is in ~~garage~~ where is the treasure hidden.

ANS/ = P = This house is next to a lake.

Q = The treasure is in the kitchen

R = The tree ~~is in the~~ is in the front is an elm

S = The treasure is buried under the flag pole

T = The tree is in the back yard is an oak.

U = The treasure is in garage.

We will arrange these sentences as given below

- a)  $P \rightarrow \sim a$
- b)  $\sim \rightarrow a$
- c) P
- d)  $\sim \vee \sim$
- e)  $t \rightarrow u$

We will assume that the previous four premises are true and drive a conclusion using rules of inference.

Step	Reason
$P \rightarrow \sim a$	Premise
$\sim \rightarrow a$	Premise
P	Premise
$\sim \rightarrow$	Premise
$t \rightarrow u$	Premise
$\sim a$	modus Ponens of (1) and (3)
$\sim \sim$	modus tollens of (2) and (6)
S	Elimination of (1) and (7)

(Q2(A) Write the Converse, Inverse and Contrapositive of the following IF Howard can swim across the lake, then Howard can swim to the island.

A) CONTRAPOSITIVE: If Howard cannot swim the island, then Howard cannot swim across the lake.

\* INVERSE: If Howard can swim across the lake, then Howard can't swim to the island.

CONVERSE:- If Howard can swim to the island then Howard swim across the lake.

B) If today is Easter, then tomorrow is Monday.

CONTRAPOSITIVE:- If tomorrow is not Monday then today is not Easter.

INVERSE:- If today is not Easter then tomorrow is not Monday.

CONVERSE:- If tomorrow is Monday then today is Easter.

(Q2B) Use truth table to determine whether the Argument Form are Valid - Indicate which column represent the Premises and which represent the conclusion.

a. P  
P → Q  
¬ Q ∨ R  
R

The first row is the only row in which all premises are true and the conclusion is also true there is not other row where Premises are all true, So this argument is valid.

P	Q	R	$\neg Q$	Premise P	Premise $P \rightarrow Q$	Premise $\neg Q \vee R$	Conclusion $\gamma$
T	T	T	F	T	T	T	T
F	F	T	T	T	T	F	F
T	F	T	T	T	F	T	T
T	F	F	T	T	F	T	F
F	T	T	F	F	T	T	T
F	T	F	F	F	T	F	F
F	F	T	T	F	T	T	T
F	F	F	T	F	T	T	F

B)  $P \wedge Q \rightarrow \neg R$

$P \vee \neg Q$

$\neg Q \rightarrow \neg Q$

$\neg R$

In third row all premise are true but conclusion is false so this argument is invalid.

Conclusion

	P	Q	R	$\neg Q$	$\neg R$	$P \wedge Q$	$P \wedge \neg R$	Premise $P \vee \neg Q$	Premise $\neg Q \rightarrow$	Conclusion $\uparrow$ Y
	T	T	T	F	F	T	F	T	T	F
	T	T	F	F	T	T	T	T	T	T
	T	F	T	T	F	F	T	T	T	F
	T	F	F	T	T	F	T	T	T	T
	F	T	T	F	F	F	T	F	T	F
	F	T	F	F	T	F	T	F	T	T
	F	F	T	T	F	F	T	T	F	F
	F	F	F	T	T	F	T	T	F	T