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Section = 'A'

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Q.1

A Circular Curve has 300m radius and 60° deflection angle. What its degree by (a) arc definition of standard length 30m. Also calculate its length of Curve (ii) tangent length (iii) length of long chord (iv) mid-ordinate (v) apex distance.

Sol:

$$R = 300\text{m} \quad \Delta = 60^\circ$$

(a) Arc definition:-

$$s = \frac{300}{R} \times 30\text{m}$$

$$R = \frac{s}{D_a} \times \frac{180}{\pi}$$

$$\therefore 300 = \frac{30 \times 180}{D_a \pi} \quad \text{or } D_a = \boxed{5.730}$$

(b) Chord definition:-

$$R \sin \frac{D_c}{2} = \frac{s}{2}$$

$$300 \sin \frac{D_c}{2} = \frac{30}{2}$$

$$\boxed{D_c = 5.732}$$

(1) length of the Curve

$$L = R \Delta \frac{\pi}{180} = 300 \times 60 \times \frac{\pi}{180}$$

$$\boxed{314.16\text{m}}$$

(ii) Tangent length:

$$T = R \tan \frac{\Delta}{2} = 300 \tan \frac{60}{2} =$$

$$= \boxed{173.21 \text{ m}}$$

(iii) length of long chord:

$$L = 2R \sin \frac{\Delta}{2} = 2 \times 300 \times \sin \frac{60}{2}$$

$$= \boxed{300 \text{ m}}$$

(iv) Mid-ordinate:

$$M = R \left(1 - \cos \frac{\Delta}{2} \right) = 300 \left(1 - \cos \frac{60}{2} \right)$$

$$= \boxed{40.19 \text{ m}}$$

(v) Apex distance:

$$E \odot = R \left(\sec \frac{\Delta}{2} - 1 \right) = 300 \left(\sec \frac{60}{2} - 1 \right)$$

$$= \boxed{46.41 \text{ m}} \text{ Ans.}$$

Q.21

Two roads having a deviation angle of 45° at apex point V are to be joined by a 200m radius circular curve. If the chainage of apex point is 1839.2m and peg interval being 10m . Calculate necessary data to the set

the curve by

\Rightarrow offset from chords (using peg interval 20m if needed).

Solution:-

$$R = 200\text{m} \quad \Delta = 45^\circ$$

$$\therefore \text{length of tangent} = 200 \tan \frac{45}{2} = 82.84\text{m}$$

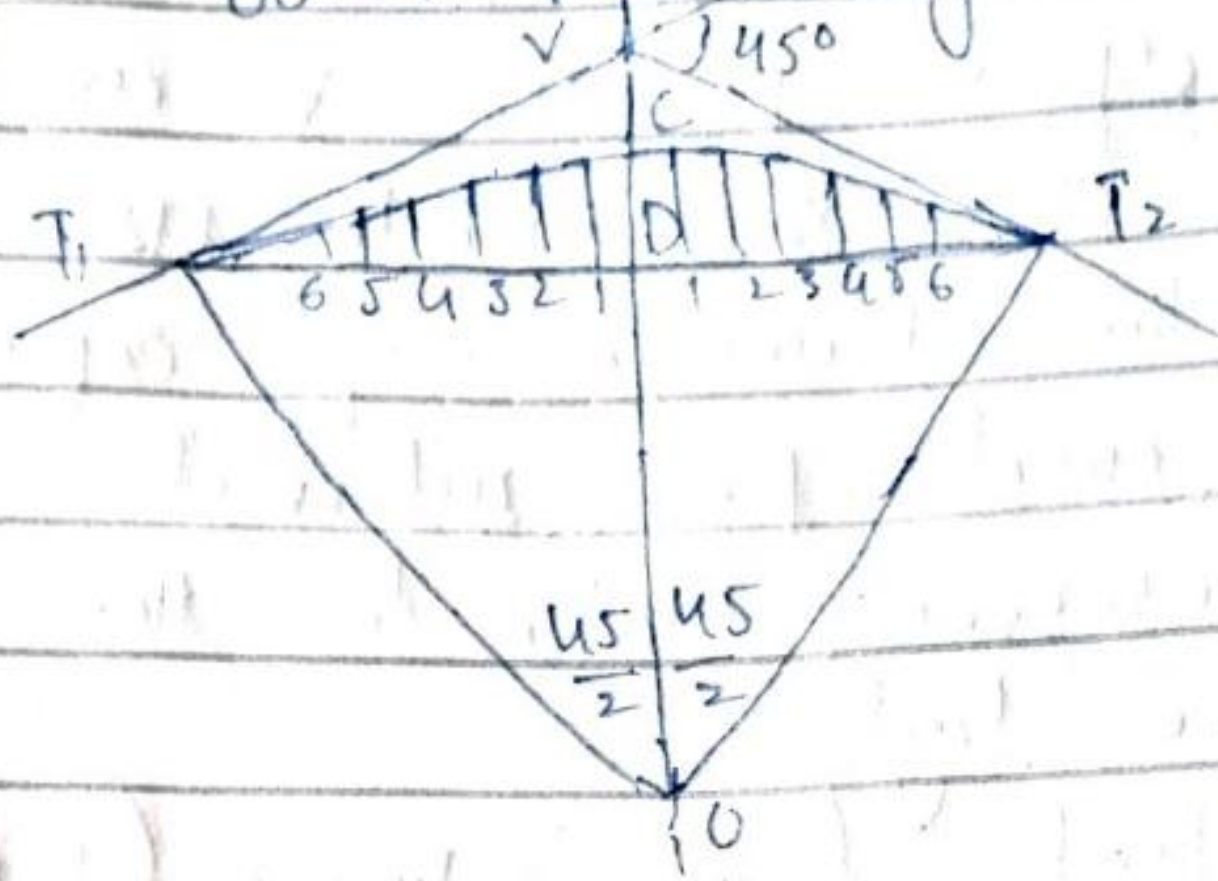
$$\therefore \text{Chainage of } T_1 = 1839.2 - 82.84 = 1756.36\text{m}$$

$$\text{length of Curve} = R \times 45 \times \frac{\pi}{180} = 157.08\text{m}$$

$$\begin{aligned} \text{Chainage of Forward tangent } T_2 \\ = 1756.36 + 157.08 = 1913.44\text{m} \end{aligned}$$

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(a) By object from long chord:-



$$\text{Distance of DT} = L/2 = R \sin \Delta/2 = 200 \sin 45/2 = 76.54$$

Measuring "x" from D,

$$y = \sqrt{R^2 - x^2} - \sqrt{R^2 - (L/2)^2}$$

$x = 0$

$$O_0 = 200 - \sqrt{200^2 - 76.54^2} = 200 - 184.78 = 15.22m$$

$$O_1 = \sqrt{200^2 - 10^2} - 184.78 = 14.97m$$

$$O_2 = \sqrt{200^2 - 20^2} - 184.78 = 14.22m$$

$$O_3 = \sqrt{200^2 - 30^2} - 184.78 = 12.96m$$

$$O_4 = \sqrt{200^2 - 40^2} - 184.78 = 11.18m$$

$$O_5 = \sqrt{200^2 - 50^2} - 184.78 = 8.87m$$

$$O_6 = \sqrt{200^2 - 60^2} - 184.78 = 6.01m$$

$$O_7 = \sqrt{200^2 - 70^2} - 184.78 = 2.57m$$

At T₁, O = 0.00-

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(b)

Method of Bisection-

$$\begin{aligned} \text{Central ordinate at } D &= R \left(1 - \cos \frac{\Delta}{2} \right) = \\ &= 200 \left(1 - \cos \frac{45}{2} \right) \\ &= 15.22 \end{aligned}$$

$$\begin{aligned} \text{Ordinate at } D_1 &= R \left(1 - \cos \frac{\Delta}{4} \right) = 200 \left(1 - \cos \frac{45}{4} \right) \\ &= 3.84 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Ordinate at } D_2 &= R \left(1 - \cos \frac{\Delta}{8} \right) = 200 \left(1 - \cos \frac{45}{8} \right) \\ &= 0.96 \text{ m} \end{aligned}$$

(c) Offset from tangent:

Radial offset:

$$O_x = \sqrt{R^2 + x^2} - R$$

$$\text{Chainage of } T_1 = 1756.36 \text{ m.}$$

∴ For 30m Chain it is at.

$$= 58 \text{ chains} + 16.36 \text{ m}$$

$$x_1 = 30 - 16.36 = 13.64$$

$$x_2 = 43.64 \text{ m}$$

$$x_3 = 73.64 \text{ m.}$$

∴ The last it at $x_4 = \text{tangent length} = 82.84 \text{ m}$

$$O_1 = \sqrt{200^2 + 13.64^2} - 200 = 0.96 \text{ m.}$$

$$O_2 = \sqrt{200^2 + 43.64^2} - 200 = 4.71 \text{ m}$$

$$O_3 = \sqrt{200^2 + 73.64^2} - 200 = 13.13 \text{ m}$$

$$O_4 = \sqrt{200^2 + 82.84^2} - 200 = 16.48 \text{ m.}$$

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offset from chord produced:

length of 1st sub-chord = 13.64m = C_1
length of normal chord = 30m = C_2

Since length of chain is 157.08m, $C_3 = C_4 = C_5$
= 30m.

Chainage of Forward tangent = 1913.44m
= 63 chain + 23.44m

length of last chord = 23.44m = $C_n = C_6$

$$i- O_1 = \frac{C_1^2}{2R} = \frac{13.64^2}{2 \times 200} = 0.47m$$

$$O_2 = \frac{C_2 (C_1 + C_2)}{2R} = \frac{30 (30 + 13.64)}{2 \times 200} = 3.27m$$

$$O_3 = \frac{C_2^2}{R} = \frac{30^2}{2 \times 200} = 4.5m = O_4 = O_5$$

$$O_6 = \frac{C_n (C_{n-1} + C_n)}{2R} = \frac{23.44 (23.44 + 30)}{2 \times 200}$$

$$= \underline{\underline{3.13m}}$$

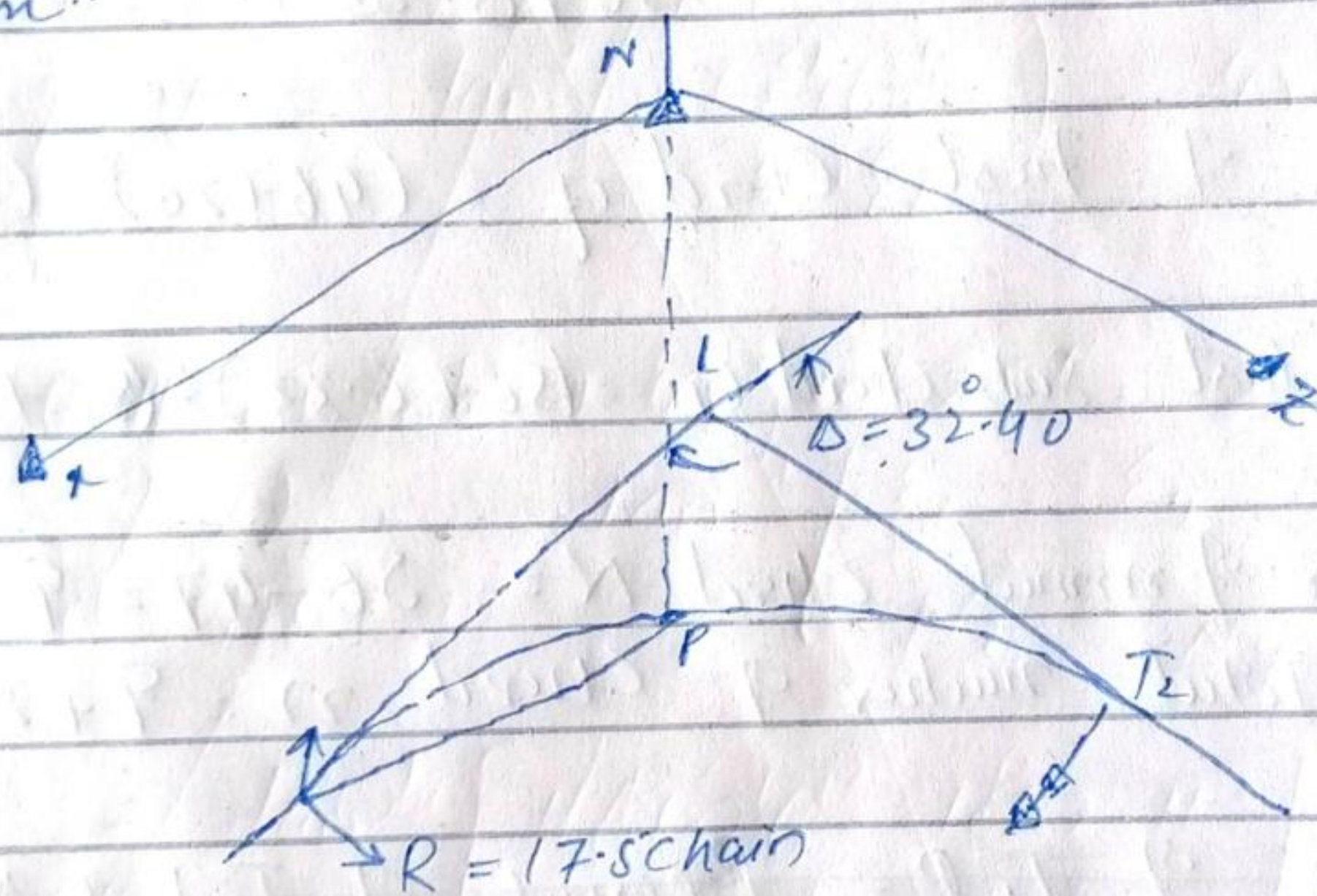
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Q₃

A Circular Curve of radius of 17.5 Chain deflecting right through $32^{\circ}.40'$ is to be set out between two straight having Chainage of the Intersection as (51+9.35)

Calculate the necessary data to set out the curve by the method the deflection angle of the sight of one chain 20m.

Solution:



$$R = 17.5 \times 20 = 350\text{m}$$

$$D = 32^{\circ}40' = 32.667^{\circ}$$

$$D/2 = 16^{\circ}20'$$

$$\text{Tangent Length } T = R \tan D/2$$

$$= 350 \times \tan 16^{\circ}20' = 102.57\text{m}$$

$$\text{Length of Curve } l = \frac{\pi R D}{180}$$

$$= \frac{\pi \times 350 \times 32.667}{180} = 198.55\text{m}$$

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$$\text{Change of } T_1 = \text{Change of P.I.} - T$$

$$= Q(S_1 + 9.35) - 102.57$$

$$= (51 \times 20 + 9.35) - 102.57$$

$$= 926.78 \text{ m} = 46 + 6.78$$

$$\text{Change of } T_2 = \text{Change of } T_1 + 1$$

$$= 926.78 + 199.55 = 1126.33 \text{ m}$$

$$= 56 + 6.33$$

$$\text{length of first chord } q = (46 + 20) - (46 + 6.78) = 13.22 \text{ m}$$

$$\text{length of last sub-chord } C_1 = (56 + 6.33) - (56 + 0) = 6.33 \text{ m}$$

$$\text{Number of normal chord } N = 56 - 47 = 9$$

$$\text{Total number of chord } n = 9 + 2 = 11$$

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Coordinate of T_1 and T_2

$$\begin{aligned}\text{Bearing of } \Pi_1 &= \alpha = 180^\circ + \text{bearing of } T_{11} \\ &= 180^\circ + 78^\circ 36' 30''\end{aligned}$$

$$\begin{aligned}\text{Bearing of } \Pi_2 &= \beta = \text{Bearing of } \Pi_1 - \phi \\ &= \text{Bearing of } \Pi_1 - (180^\circ - \Delta) \\ &= 258^\circ 36' 30'' - (180^\circ - 32^\circ 40') \\ &= 111^\circ 16' 30''\end{aligned}$$

Coordinate T_1

$$\begin{aligned}\text{Easting of } T_1 &= E_{T_1} = \text{Easting of } 1 + T \sin \alpha \\ &= 1058.55 + 102.57 \times \sin 258^\circ 36' 30'' \\ &= E = 958.00 \text{ m}\end{aligned}$$

$$\begin{aligned}\text{Northing of } T_1 &= N_{T_1} = \text{Northing of } 1 + T \cos \alpha \\ &= 1045.04 + 102.57 \times \cos 258^\circ 36' 30'' \\ &= N = 1024.78 \text{ m}\end{aligned}$$

Coordinate of T_2

$$\begin{aligned}\text{Easting of } T_2 &= E_{T_2} = \text{Easting of } 1 + T \sin \beta \\ &= 1058.55 + 102.57 \times \sin 111^\circ 16' 30'' \\ &= E = 1154.18 \text{ m}\end{aligned}$$

$$\text{Northing of } T_2 = N_{T_2} = \text{Northing of } 1 + T \cos \beta$$

$$\begin{aligned}&= 1045.04 + 102.57 \times \cos 111^\circ 16' 30'' \\ &= N = 1007.812 \text{ m}\end{aligned}$$

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Tangential angle

$$\delta = 1718.9 \frac{C}{R} \text{ mint}$$

$$\delta_1 = 1718.9 \frac{13.22}{350} = 64.925'$$

$$\delta_2 \text{ to } \delta_{10} = 1718.9 \frac{20}{350} = 98.223'$$

$$\delta_{11} = 1718.9 \frac{6.33}{350} = 31.088''$$

Deflection angle

$$\Delta_1 = \delta_1 = 64.925' = 1^{\circ}04'5''$$

$$\Delta_2 = \Delta_1 + \delta_2 = 64.925' + 98.223' = 163.148' \\ = 2^{\circ}43'04''$$

$$\Delta_3 = \Delta_2 + \delta_3 = 163.148' + 98.223' = 261.371' \\ = 4^{\circ}21'22''$$

$$\Delta_4 = \Delta_3 + \delta_4 = 261.371' + 98.223' = 359.594' \\ = 5^{\circ}59'36''$$

$$\Delta_5 = \Delta_4 + \delta_5 = 359.594' + 98.223' = 457.817' \\ = 7^{\circ}37'38''$$

$$\Delta_6 = \Delta_5 + \delta_6 = 457.817' + 98.223' = 556.040' \\ = 9^{\circ}16'40''$$

$$\Delta_7 = \Delta_6 + \delta_7 = 556.040' + 98.223' = 654.263' \\ = 10^{\circ}54'16''$$

$$\Delta_8 = \Delta_7 + \delta_8 = 654.263' + 98.223' = 752.486' = 12^{\circ}32'28''$$

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$$\Delta P = \Delta_8 + \delta_8 = 752.486' + 98.223' = 850.709' \\ = 14^\circ 10' 43''$$

$$\Delta_{10} = \Delta_9 + \delta_{10} = 850.709' + 98.223' = 15^\circ 48' 56'' \\ \downarrow \\ 948.932'$$

$$\Delta_{11} = \Delta_{10} + \delta_{11} = 948.932' + 31.088' = 980.020' \\ = 16^\circ 20' 00''$$

Check = $\Delta_{11} = \Delta_{1/2} 16^\circ 20'$ (oleg)